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اثر فلسفة العلم المعاصرة على (العمـارة<br>القسم المعماري-كلية الهندسة-جامعة بغداد<br>بكالوريوس هندسة معمارية<br>د.أريج كريم مجيد السدخان-أستاذ مساعد<br>علاء عبد الرزاق كريم

ملخص البحث
يتتاول هذا البحث المو اقف الفكرية العامة للعلاقة بين فلسفة العلم المعاصرة و العمارة،و مناقشتها ضــمن طروحات كل من K .Popper ، و التي تم بلورتها ضمن مفردات أساسية و فر عية شملت ما يأني: الموقف من النظرية النفسية، الموقف من نظرية المعرفة،الموقف من المجتمع،،الموقف من التاريخ.
وقد تم تعريف جو انبها بضوء المعرفة المرتبطة بها و المطروحة في الار اسات الفلسفية العلمية المعاصرة
و المعمارية. و بيان القيم الممكنة و المرتبطة بمفردتي الموقف من المجتمع و الموقف من التاريخ لبعض الجوانب
المشتركة بين طروحات Popper و الو اقعية الجديدة و طروحات Kuhn و العقلانية الجديدة ، فقد ثم النوصل إلى
بعض الجو انب المشتركة بين طروحات Popper و طروحات الو اقعية الجديدة و طروحات Kuhn و العقلانيــة
الجديدة ، شملت الأسس الفلسفية و موققهما من النقاليد ، فضـلا عن طبيعة المر اجع المعتمدة و طبيعة التعامل مـــع
النقاليد وفي ضوء ذللك تم بلورة مفردة ، عرفت (بالموقف من التنيار ات المعمارية ) ارتبطــت بمفــردات فرعيــة
عرفت بضوء جوانب اكثر تفصيلية و المتعلقة بالموفق من العمارة و أهدافها و الثقاليد و طبيعة المر اجع التي يتم محاكاتها و موقفهما تجاه نظريات العمارة و ماهية المعاني و الأفكار التي يعبر عنها المصمـ الكلمات الرئيسية: العمارة ، فلسفة العلم ، المجتمع و العمـارة ، تاريخ العمارة .

## Research abstract

## THE EFFECT OF CONTEMPORARY SCIENCE PHILOSOPHY ON ARCHITECTURE

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#### Abstract

The research tries to investigate the effects of Contemporary Science Philosophy on Architecture. The research depends on contemporary Science Philosophy of K.Popper and T.Kuhn. The procedures of the research contain the construction of comprehensive theoretical framework that includes the influence of contemporary of Philosophy of Science on Architecture in the following level which contains the general thought position, which includes (The position of Psychological Theory, knowledge Theory, the society, the history and the position of Architecture views). The conclusions of the research focus on the theoretical framework that depends on the previous views of K.Popper and T.Kuhn which reflected on Architectural views.


## KEY WORDS

## Architecture, philosophy of science, society and architecture, history of architecture.

(لمقدمة
يتتاول البحث وصف المو اقف الفكرية العامة لفلسفة العلم و انعكاس تأثنثر ها على العمارة.وقد تطلــبـ وصــفـها النوجه نحو الار اسات الفلسفية العلمية والمعمارية بغية استكثاف الأطر النظرية الكامنة فيها ،ث بلورة الطروحات ضمن مفردات ثانوية اكثر وضوحا فضلا عن استخلاص قيمها المدكنة. وقد تم مناقشة المفردات الأساسية للإطار النظري من خلال استكشافها في الدر اسات الفلسفية العلمية أو لا،ثم معماريا من خال نقصي المو اقف العامة في الطروحات المعمارية ،ولغرض تعزيز القاعدة النظرية وبناء إطـــار ا نظريا شاملا ،كما نوجه البحث إلى الار اسات المعمارية المتخصصة لاستكثشاف خصوصية الأفكار و المفاهيم التي

تعكس الجو انب المشتركة و المتباينة بين فلسفة العلم و العمارة.
سيقتصر البحث على نتاول الطروحات الفلسفية العلمية لكل مــن T.Kuhn\&K.Popper،لأهميتهــا علــى المستوى الفلسفي العلمي ،فلو استقصينا ناريخ فلسفة العلم المعاصر و عدنا إلى ستينات القرن العشرين لوجـــنـاهما من أهم فلاسفة العلم المعاصرين الذين تمكنو ا من خلال طروحاتهم ،من قلب نظرية المعرفة العلمية رأســـا علــى عقب فضلا عن حل معضمات وخصومات فلسفية كانت قائمة،فقد جاءPopper بمشرو ع( الفرضي-الاســتدلالي (الذي يمكن أن يستو عب العلم،و اقترح Kuhn نموذجا معرفيا يعمل العلم من خلاله كنشاط لحل الألغاز إلى حين حدوث الانقلاب في النموذج (حمدي،ص15). طرحت فلسفتيهما صر اعا فلسفيا علميــا ألقى بضلاله على مبحث فلسفة العلم المعاصر ،من خلال بروز طروحا ت تقف إما موفف المؤبد لا حدهما منتأثر ا ومستلهما لمبادئي طروحاته،أو موقف الضد من مو اقف أخرى (السابق،ص18).
معماريا،فقد بدأت ملامح التأثز في هذه الطروحات الفلسفية العلمية من خـــالا تبنــي بعــض المنظــرين و المصمميين المعماريين لهذه الطروحات

فلسفة العلم
يعرف ( د. احمد فؤاد باشا ) فلسفة العلم :بالمبحث الجدبد الذي أضافه المحدثون إلــى مباحــث التفكيـر
 نظرة شاملة إلى الكون من خلال الربط بين سلوك الظو اهر التي يتعامل معها الإنسان (باثشاص 63) ،ويعرف
 و الإنسانية ويهدف إلى فهم مكانة العلوم في حضـارنتا (د.مهران ,ص 10 )،ويعرفها (د.الجابري ) في كتابه (مــــل إلى فلسفة العلوم ) بأنها المبحث الذي يهتم باسنقصـاء الحقيقة وتكوين الأحكام الثاملة و تبنــى النـــــاذج الفكريـــة وخلق الصور الذهنية عن العالم المحيط (الجابري،ص20).
ويمكن التفلسف في العلم من وجوه أربع حسب ما تطرحه أدبيات العلم المعاصر وهي:
در اسة علاقة العلم لكل من العالم والمجتمع ( العلم من حيث هو ظاهرة اجتماعبة ). محاولة وضع العلم في المكان الخاص به ضمن مجموع القيم الإنسانية.
(8) مجلة المهنسة

- الرغبة في تتبيد فلسفة للطبيعة انطلافا من نتائج العلم. - التحليل المنطقي للغة العلمية.(محمود،ص38). كما تطر ح أدبيات العلم المعاصر نوجهين رئيسين في فلسفة العلم هما:
- فلسفة العلم (لخاصة

ينطلق أصحاب هذا النوجه من كون القضايا و المشاكل المبدئية أو المنهجية التي تخص علم من العلوم قــــــ لا تخص بالضرورة علما أخر بل العكس في نظر هم هو الصحيح، فمشاكل الرياضيات ليست هي مــشاكل العلـوم الإنسانية و هكذاهو ان محاولة الجمع بين قضايا العلوم المختلفة في إطار أو نسق فلسفي علمي واحد هو في نظر هم - عمل فلسفي -لا يمكن الاسنفادة منه في حل المشاكل الدقيقة الخاصة، لذا فهم يحرصون على أن تحنفظ الفلسفة العلمية بطابعها العلمي الخاص و عدم التقيد بأي نظرة فلسفية عامة ، فكان فلسفة العلم في نظر هم لا تختلف عــن الميثودولوجيا ألا بقدر ما يكون التحليل اكثر عمقا و النقد اكثر صر امة .(الجابري ،ص 50 ). - فلسفة (لعلم العامة

يرى أصحاب هذا التوجه ، أن فلسفة العلم الخاصة ذات نزعة ضيقة , ويطرحون نظــرة مغـــايرة أخــرى فالمشاكل التي تعترض علم من العلوم كثير ا ما نكون هي نفسها التي تعترض علما أخر، علاوة على أن العلــوم نفسها منداخلة وبينها علاقة لا يمكن تجاهلها .لذا فالنوجه السائد و الذي اصبح حقبقة و اقعية هــو اللتركيــز علــــى
 العلمية الخاصة لكل علم كلن تكون مثمرة، إلا إذ تم تحليلها و النظر أليها من عدة زو ايا، فالمعالجـــة المنطقبــة لا

نكفي بل لابد من اللجوء إلى علم النفس وتاريخ العلوم وعلم الاجتماع .(السابق ، ص 50 ). يتبنى البحث در اسة تأثنير طروحات أصحاب هذا النوجه على العمارة.

## فلسفة العلم وطبيعة موضو عاتّها

يطرح Feigl \& Brubeck في كتــاب(Readings in Philosophy of Science)الجو انــب التـــي تشتملها فلسفة العلم والتي نتعدى نطاق تحليل لغة العلم لتشمل : - انطولوجيا العلم : البحث في كشف طبيعة الوجود اللامادي في القضايا الميتافيزيقيــة المرتبطـــة بـــالتطورات و المفاهيم العلمية.
ابستيمولوجيا العلم : البحث في نظرية المعرفة العلمية بجو انبها الثلاث ( إمكان المعرفة ومصـادر ها وطبيعتها). - اكسيولوجيا العلم : البحث في القيم و المثل العليا ومدى ارتباطها بالعلم وخصـائص الثفكير العلمي. هسايكولوجيا العلــم :تبحث في العمليات اللفسية و العقلية التتي تتعلق بالكثف العلمي وما يقترن بها من القـــدرات الإبداعية و الخيالية لحل المشكلات العلمية .

- سوسيولوجيا العلم : تبحث في التفسير الاجتماعي لتطور النظريات العلمية ومدى تقبل المجتمع لها بالإثــــارة إلى أسلوب التنظير العلمي ونمطه الذي يعكس الصيغة السائدة في مجتمع مـا ،وتلعب المعايير اللقافيـــة و القــيم السلوكية في التأثبر على تحديد الاتجاهات العقلية و منهاالتفكير العلمي و الفلسفي .(Feigl \& Brodbeck,p47 ).

ويقول Laland في معجمه الفلسفي أن فلسفة العلم ترتبط بالار اسة النققية لمختلف العلوم، لتحديد اصــلها اللنطقي ( موضوع الابستمولوجيا) ودر اسة المناهج العلمية ( موضوع الميثودولوجيا ) و التي نتثكل جــز اللنطق ( الجابري ،ص 18 ) .كما أن المنهج العلمي هو جملة العطليات العقلية والخطوات العطلية التي يقوم بهـــا العالم من بداية بحثه حتى نهايته من اجل الكثّف عن الحقيقة و البر هنة عليها وهي در الـي
 20).ويرىPierre Bont أن تاريخ العلم هو الـقدمة الطبيعية لفلسفة العلم وميز أربع أنواع منه وهـــــي ( التـــاريخ الوثائقي , تاريخ الأخطاء , الناريخ المكاني , الناريخ الفلسفي للعلم ) ( الجابري،ص28-40 النارئ ).
مما سبق يمكن استخلاص المو اقف الفكرية العامة والتي تصو غها أثنكال الارتباط الأنفة الأكر وهي كالأتي : - الموقف من نظرية الوجود العلمية ( انطولوجيا العلم ). - الموقف من نظرية المعرفة العلمية (ايستمولوجيا العلم) .

- الموقف من نظرية القيم العلمية (اكسيولوجيا العلم ). - الموقف من النظرية النفسية العلمية ( سايكولوجيا العلم ). - الموقف من النظرية الاجتماعية العلمية ( سوسيولوجيا العلم ) . - الموقق من المنهجية العلمية ( ميثودولوجيا العلم ). - الموقف من تاريخ العلم. وسيتم مناقثة كل من الموقف من النظرية النفسية العلمية والموقف من نظرية المعرفة العلمية و الموقف من
 الفلسفية العلمية ومن ثم استكشافها على مستوى العمارة. - فلسفة العلم والعمارة (المو اقف الفكرية العامة) - الموقف من النظرية النفسبية

يرى Fiagl \& Broadbeck أن فلسفة العلم تبحث في سايكولوجيا العلم، أي العمليات النفسية و العقلية التي

 في كتابه(The Structure of Scientific Revolutions) فلسفته بأنها جـشتنالتية (Gestalt) ( Kuhn,p78) ،

 كل من Kuhn Popper ، فعند الأول نهط التنير عقلاني أو على الأقل قابل لاعادة الإنشاء عقلانيا و يقع ضمن عوالم منطق الاكتثتاف العلمي ، أما Kuhn فانه لا يوجد أي تفسير عقلاني معين لظهور الأزمة فــي النظريــة الأساس و هي عنده (أي الأزمة) حدث سايكولوجي و هو نوع من الذعر الجمعي (Able,p20)

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 السايكولوجي الاجتماعي للاستكشاف، لذا فان التغير العلمي نوع من التنير الديني الخاضع لقوى الإفناع للـــنين لا يسعون إلى معاكسات جديدة (Ibid,p209).

 النظرية من مجالات علمية أخرى مثل (الفلسفة التفاعليـــة (Transactional Philosophy)(Tewey) و مفـــاهيم علم الاجتماع التي جاء بها G. meed و يعتمد علم النفس التفاعلي على بعض الافتر اضات منها :-- علاقة الفرد-البيئة هي علاقة ديناميكيك - أن الخيال الذي يحمله الثخص عن البيئة يعتد على التجربة فضلا عن النوجهات و الدو افع الآنية الحاضرة و أن الخبرة السابقة تحضر للفرد في الحالة الآنية لموضوع معين.

- التغير الادر اكي محكوم بالتوقعات و التفضيلات و بالتالي فان المعلومات التي يكتسبها الفرد نكون ذات طبيعة احتمالية يتم اختبار ها و تفضلها ثم تأكيدها خالل الفعل و المعلومات نكون ذات خصائص رمزية و معنويــة .(Lang,p76)
أما بالنسبذلاKuhn فيرتبط ( بعلم النفس الجشتالتي) وهو على النقيض من علم النفس النفاعلي، يعد أن ما
 العقل ، و يخضع تكون الكليات إلى الملكات الغريزية للأفــر اد، و التــي تنكــن مــن خلـــق أثـــكال بــسيطة و متعامدة و مقفلة أو متكاملة (Lang,p80 ) و تنترض نظرية (الجشتالت) انعز ال الفرد عن بيئته و عــن نـن نــشاطه

 . البصرية و هي (قانون التقارب ،التماثل ، الهيئات المغلقة ، التنرج ، الحركة العام ،و قانون الخبرة) (Ibid,p84) . يتبين مما سبق ، أن النظرية النفسية التي يعتمدها Popper في تحيله لمنطق الاكتثشاف العلمي و الجاتب الإبداعي فيه هي ذات نزعة فردية براغماتية قائمة على أن الذات هي المؤثرة في الموضوع و المحدثـــة فيــهـ التغيير نتيجة الجدة المتتامية في الإبداع المعرفي عند الذات ، أما Kuhn فالنظرية التي يعتمــدها ذات نزعــة
 الثابت (النموذج عند Kuhn) و في حالة تغير النموذج (الموضوع ) يحـث نوع من الذعر الجمعي ، و الـــي . يمه لاكتشاف نموذج جديد
إما على مستوى استنلاص المفردات الفرعية المتعلقة بالموقف من النظرية النفسية فيكنن أن نصوغها
كالآتي :
- الموقف من حيث الأسس الفلسفية للنظرية النفسية :أما علم الــنفس التفـــاعلي أو علــم الــنفس الجشتالتي.
- من حيث نوع التغير في الاكتشاف العلمي :أما التغير عقلاتي:يقع ضمن عوالم منطــق الاكتـشـاف العلمي.أو التغير الديني : ضمن عالم السايكولوجي الاجتماعي.


## - (لموقف من نظربـة (المعرفة

تتاولت الزنكة في بحثها الموسوم ( الفلسفة الوضعية - تاريخ نظريات العلم ) أفكار Popper و علاقتهــا بالتجريبية المنطقية ، كون الأخيرة حاولت ردم الهوة بين العقلانية و التجريبية على أسس مثالية ذاتية ، نوحد بين الطريقتين المتتافستين بإيجاد الفلسفة العلمية (الزنكــة ، ص 166 ) ،وتقول الزنكة أن Popper هو أحد الذين طوروا

 يكفي ، و إنما يجب دحضه و الذي يقابل ما يسمى بالتحقق التجريبي عند الفلاسفة ( الــسابق ، ص 168 ) ،تتـــاقش
 بينها ، مركز ا على ظهور انطباعات جديدة في التطبيق ومن ثم إلى الخطوة التي نقرر فيها فكرة نظرية موثــوق بها بسبب الاستخدام لها في خطة عمل أو في تجربة( السابق ، ص 168 ) , ينعكس ذلك ضمن منهجية ( فرضـــية - استد لالية) يطرحها Popper ضمن منهجه الذي يتخذ من مبدا اطر اد الحوادث مصادرة منهجية ، هذا المنهج لا يفسر حو ادث أو ظو اهر بقدر ما يفسر قو انين و يكتشف ظو اهر جديدة ، يقوم هذا المنهج على ثلاث خطوات :-

البدء بتعميمات استقر ائية.

- افتر اض فرضٍ مفسرِّ (غالبا ما يكون مشحون بصيغ رياضية مجردة لا نقبل التحقيق التجريبي المباشر) • - محاولة استتباط ما بلزم عن تللك الصيغ من نتائج و اسنتتاج ما بلزم عن هذه من نتائج أخرى حتى نصل إلى نمط من النتائج يمكن التحقق من عدم صحتها بالتجربة (زيدان ، ص127)، وقد شبه أحد المنطقيين الفرنسيين هذه المنهجية بالصعود من مجال التجربة إلى عالم العقل ثم العودة إلى عالم الو اقع ، لكي نضمن الصلة بين المعقول و الو اقع (السابق ،ص 130). أما بالنسبة إلى موقف Kuhn فتتاقش الزنكة طروحات الأخبر في كتابه (تركيب الثور ات العلمية،1962 ) ، موضحا أن الفكرة الأساسية فيه هي ( ميزان التصريف ) المبنية على أساس أن العمل التجريبي في العلم مليء بالتفكير النظري ، و إن العمل النظري توجهه الأفكار العامة ، طارحا مكونات أربعة لميزان النصريف:
- التعميمات الرمزية :- بديهيات و مبادئ نظرية علمية معينة. - العنصر ألديتا فيزيقي الموجه :- صورة عامة عن الكون ( وجهة النظرية الفكرية ). - الجانب الطر ائقي :- مكونات القيم (يرنبط بالنو اميس الإجر ائية في سياق البحث ).
 متل ( كتاب القو اعد ) لنيوتن و( اصل الأصناف ) لدارون ( الزنكة ، ص 192 ،1981).

نتيجة مو ازيين التصريف هي إنتاج النماذج الفكريةParadigms و يعتمد على التحقيق الفلسفي في تأكيــــ
هذه النماذج الفكرية.

| (1) | مجلة الهنسة | كانون الأول 2006 | المجلد 12 | العدد 4 |
| :---: | :---: | :---: | :---: | :---: |

الاختلاف بين Popper و Kuhn هو في منهج الاختبار و مصدرية الفرض ، فعند Popperالاختبار يعتمد ( التكذيب )، أما عند Kuhn فانه يقدم نقده لهذا المبدأ و يستخذم منهج ( التحقيق ) و يصفه كونه انتصـار للنماذج

 بالنسبة للفرض فانه عندPopper ينشا بالحس، أما عندي
 مجموعة الأمتلة حسب مو ازيين التصريف وضمن مرطلة توسيع نطاق الفرض ) هو هكذا يتم صــياغة (النــــاذ الفكرية ) و التي يصنفهاKuhn إلى ثلاثة أثنكال هي :-

## نماذج فكرية اعتيادية ، نماذج فكرية تفصيلية ، نماذج فكرية ثورية الـورية.



- (Ibid ,p209) (الشاذ

يتبين مما سبق ما يأتي :-

- أن نموذج Popper ينطلق بالمشكلة من العالم النجريبي بصياغة نظرية ثم يتحقق من صحتها عقلانيا ومنطقيا في عالم الفكر ضمن نموذجه التكذييي ( صياغة التخمينات ، الحـول المفترضـــــــة ) وبالتـــالي اختبار مدى صحتها و ملاءمنها لتصو غ الناتج النهائي ذا الصفة التحويرية لغرض إزاحة الـيا الفكرة ، أما فانه ينطق بالمشكلة من الجانب النظري ضمن (اللتوجه العام ) من العــالم التجريبــي و يــتّم اختبار ها تجريييا من خلا الإسناد النظري و التجريبي خلال مرطلة توسيع نطاق الفرض ( مجموعة الأمتلة ضمن موازيين التصريف ) المؤكد للحل المبداي و الذي يطرحه ضمنيا النموذج ،أما في حالة الاختلاف فيتم عزل القرينة ويتم معا لجتها مسنقبلا ضمن العلم الشاذ، ليطر ح النتاج مؤكدا للنمط العام (الجو الفكري السائد) و مطور التفاصليه على مستوى التنظير و التطبيق .

 تقليدي في موقف معين جديد و هكذا تتمو المعرفة الفلسفية العلمية
 يتمتل في العلم الثاذ أي الحقائق التي لا تنفق مع النموذج السائد و التي تبدا بالظهور في اللحظة التي


 الثشاذة و تركيب بعضا منها ملائمة للموقف الجديد ، بالتالي سيكون الموقف ذا صفة نور ون وية في التنيير على اعتبار أن أساس صياغة النماذج وفقا لموازيين التصريف هو المبدأ العام و النواميس الكونيــــة

السائدة مرور ا بالنظريات المفسرة و النقاليد و القو اعد الجزئية، فتتقلب الأفكار رأسىا على عقـبـ، أذن فالتغير ثوري ضمن نظام معرفي متخصص و هو تعاقبي بين العالم السوي و الثاذ.

## -العمـارة و نظر بـة (المعرفة

معماريا و ضمن الطرح الفكري للتجريبية الجديدة ، نشر G.Cullen طروحاته القائمة على تبنــي مبــادئ تجريبية تسنتد على فهم العلاقة بين الأجر اء كفن مواز لفن العمارة ، و كانت وسيلته إلى ذلك التتـــابع البــصري ضمن البيئة لانتاج الكل من خلال المفاهيم الآتية:-
التتابع البصري :- الذي يتم تحفيزه بوجود قيم فيزيائية أساسية و قيم حيـة ثانوية ناتجة من تجــاوز - العناصر المتتاقضة مع بعض

- المكان: الذي يعني الشعور بين الوجود في مكان محدد و بين الشعور بالوجود في مكان أخر مقـــارب و مساوي له بالقيمة خارجه.
المحتوى :الذي يمثل الطر از و عناصره و الذي يمكن بواسطته ربط نو عين من العو امـــل :العو امــل الإنسانية التي تتضمن شروط المشاعر و الأحاسيس الناتجة من العلاقات الإنسانية،و العو امل الفيزيائية التي تتضمن الثنكل الحقيقي و نرنيب بنية المكان الذي يقطن فيه الإنسان ( Norris,p45 ).
 و غير هم) ، فضـلا عن المعماريين ضمن نتاجا تهم المعمارية متل (R.VEnturi, F. Spoerry) . فعلى ســبيل المثال قام F. Spoerry بمحاولة تجريبية تصورية مميزة لتصميم ( Port Grenond) اعتمادا علــى الـــنهج
 و الخطا،فضلا عن محاو لات إجرائية بر اغمانية أخرى من خلال تنيير الاتجاهات و إعادة ترتيب الأجزاء ضمن
 على ما تضيف إليه نتائج التجربة التي لعبت فيها الخبرة الذاتية و الششاعر الحسية و البصرية الدور الأساسي في
 و البيئات الحضرية و تمكن من استقر اء مئتّان وثلاث وخمسون نسقا من العالاقة بين الأجزاء و الكــل ،لتــشتمل المستويات التصميمية كافة (Ibid,p152). أن المقدمات الثكلية للتجرييية الجديدة هي احتمالية تعرض للتساؤل والتتحيص و التجربة على اعتبــار أن المعرفة الإنسانية الحقققية ، حتى أن وجدت فهي معرضة للتعديل و التغيير حتى في اكثر القضايا الرياضية دقـــة

 أما بالنسبة للطروحات الفكرية للعقالنية الجديدة و التي بدأت بالظهور خلال الخمسينات و الــتينيات مـن القرن العشرين و تبلورت في السبينات على يد Rossi و الأخوان Krier و آخرين ممن دعوا إلى إعادة أحياء الهفاهيم العقلانية (العزاوي ، ص 47) ، فقد كانت اغلب نوجهاتهم تعيد إنثارة الجدل حول القيم الإنسانية و أن طريقة النفكير العقلانية و التي تجسدت بالحول الهنسية ، أنتجت بناء ا على افتراضات تنؤخذ كبديهيات قبلية مسلم بها،

تمتل بالتالي حقائق و اضحة بذاتها و غير قابلة للتحليل و الاستفسار ، فتولد منظومة من الافتر اضات تعــود إلــى نتائج معينة بالاستدلال العقلي تعطي حقائق عن الو اقع الموجود ، فيكون بالتالي معيار ا للحقيقة ليس الخبرة الذاتية و لكن الثبات المنطقي في البناء الفكري .
و كانت الأشكال الأساسية المعمارية العقلانية تمتل بديهيات لا يمكن الاستغناء عنها كما لا يمكن إهــــال النتائج المستخلصة منها بالاستدلال المنطقي ، و هي نتائج لا تخضع لمقياس التجربة و لكن بالكيفيــة التــي يـتّ استدلالها من المقدمات ، و قد حاولت العقلانية الجديدة في طروحاتها إعادة الإشارة إلى المبادئ الأساسية للرو اد العقلانيين باعتبار الأشكال الأساسية الكاملة و نركيباتها تعكس بوضوح ذاتي غير قابل للبحث و السؤ الل ، الحقيقة الموضو عية لماهية العمارة المطلقة ( العزاوي ص 176 ).
يتبين مما سبق التو افق من خلا بـض الجو انب المشتركة بين موقفPopper وطروحات التجريبية الجديدة و موقفKuhn وطروحات العقلاهية الجديدة في العمـارة من نظريـة المعرفة ،خصوصا من حيث طبيعة البنـــاء الفكري والمقدمات الثشكلية للمعرفة ،فضلا عن طبيعتها ومنهجيتها المعرفية . كما يمكن أن نصوغ (المفردة المتعلقة بنظريـة المعرفة العلمية (ضـــمن فلــسفة العلـــ) ويــــــلتو افق مـــع الطروحات الفكريـة المعمارية كالأتي :-
المفردة الأساسية (الموقف من نظرية المعرفة):تشتتمل على المفردات (الفرعية الآتية :-- من حيث طريقة البناء الفكري : أما (معرفة تجريبية ـثم حسية و نظريـة عقلانية ـثم معرفة تجريبيــة جديدة) أو (معرفة عقلالية نظرية - ثم تجريبية (اختبار) -ثم معرفة عقلاهية جديدة). - من حيث المقدمات الثكلية للمعرفة: أما (معرفة احتمالية: معرضة للتعديل و التنيير) أو( يقينية مطلقة، تعكس الحقيقة (الموضوعية لماهية العمارة).

- من حيث جزئية وكلية المعرفة: أما معرفة جزئية :أهمية للجزء ضمن الكل معتمــدة علـــى التـــأثيرات العاطفية النفسية. أو كلية: التركيز على الكل من خلا الأثنكال الأساسية الكاملة التــي تعكــس مـاهيــة

العمـارة.

- من حيث المنهجية (لمعرفية : أما (تخمين - تحليل تكذيبي - تخمين جديد متغاير)،أو( تركيب -تحليـل إسنادي-تثثيت التركيب المعدل).
- الموقف من المجتمع

تصف الزنكة اقتز ان فلسفة العلم بثلاثة حقول هي ( منطق العلم - نظرية نمو المعرفة العلمبة ، نظريـــة العلم في المجتمع) ، وترى أن هناللك نوجهين في نمو العلم (داخلي و خارجي) و هما من ابرز ســمات النوجــهـه المعاصر في العلم ، الحقلين الأخيرين اصبحا مركز الاهتمام منذ ستينات القرن العشرين و خصوصـا مــــــا قدمـــهـ من نماذج تعتمد أساليب وصفية تستخدم تاريخ العلم ،فضلا عن سوسيولوجيا العلم و حتى الآن (الزنكة،ص 181).
وتتاقش الزنكة في بحثها الموسوم (فكرة الثورات العلمية) النوجهين السابقين موضحة أن هناللك جانبين فــي
فلسفة العلم هما :

خارجي: يتعلق بعملية النمو في المجتمع و يرتبط ارتباطا وثيقا بالنكنولوجيا و الإنتاج و النحول الاجتماعي داخلي: يتعلق بنمو المعرفة العلمية ضمن مجالها المعرفي. و على هذا الأساس يصنف نوجهين لفلسفة العلم إحداهما خارجي يصف نـــو العلـــم كإحــدى العمليــات الموجودة في المجنمع ،و الآخر يركز على المنطق الداخلي للتطور العلمي فهو نوجه داخلي(السابق ،ص188). تعتتد الفكرة الرئيسية في نموذج Popper على التخمين المتعدد القائم على الحدس الذاتي و تصف الزنكة فلــسفته الاجتماعية بأنها (مفتوحة) تؤمن بالتحول الاجتماعي ومو اكبة التطور ات و التغير ات الآنيــة (الـــابق ،ص 190 ). و بالتالي فأنها تشجع على التتامي المعرفي وفقا للمؤثرات الخارجية ، لذا يمكن القول أن توجه Popper هو ذاتي خارجي
أما بالنسبة لـ Kuhn فان الفكرة الرئيسبة في نموذجه هي إن المعرفة العلمية تعتمد على الإجماع في الر أي ضمن ما يصفه ب (العمليات الاجنماعية في المجتمع العلمي ) في ميزان النصريف ، و تتطور هذه المو ازيين تبعا
 داخلي يتميز بكونـه محافظ و عقلاتي و يؤكد على التتامي المعرفي المستقل(المؤثرات داخلية في نمو المعرفـــة

تو الت الكتابات النققية في مجال العمارة منذ الخمسينات مطالبة بالرجوع إلى الـمقياس الإنــساني و حقــوق الفرد على اثر ما خلفته الفلسفة الاجتماعية التي انطلقت من الحركة الحديثة وأسلوبها الــذي وصــفه Kaufman (فرض وجهة نظر الحكومة الجديدة للمجنمع على كافة المجالات ،لأعادة هبكلة المجتمع بشكل موحد منظم و سهل الإدارة ، وعدم اخذ اللغة المحلية بنظر الاعتبار ،و معارضـــة كافــة التتظيمــات الثقلليديــة)(Kaufman,p75). و
 الصناعة الغربي، مما دعى المعماريين و المنظرين إلى نقسيم المجتمع إلى عدة أذو اق عامة و نقافات ذو فية ثانوية ، كما دعوا إلى تفضيل التعددية واستعمال العناصر الثكلية المرتبطـــة بالعمـــارة المحليـــة و التــي حـسبـ رأي

- تعزز التلاحم الاجتماعي وتجلب الاستقرار للمجتمع (Ibid,p155) Kaufman وفي بداية الستينات حدث ثور ان فكري و ضغوط لخلق عمارة تعدل الصفة المنفردة للعمارة الحديثة فوجــدت عدة طرق لتحقيق ذلك منها (Schulz,p8):
 الاجنماع في الخمسينات انتقنوو ا فكرة سيطرة المعماري و دعو ا إلى المشاركة في التصميم (Scott,p42). البحث عن لغة تعبيرية تستجيب للمنطلبات الاجتماعية و تطلّع على اللقافات الذوفية و التي تبنى مــن اجلهـــا العمارة ور ائدها R.VENTURI).
. C.Alexander محاو لات الأسلوبية العلمية و لظهور مبادئ أساليب التصميم ور ائدها كما ظهرت العديد من النز عات ذات النوجهات الاجتماعية الجديدة منها :
- (النكاملية في اليابان التي طور ها Kara Kawa التي تقوم على التحايش بين التكنولوجيا و النقاليد و الإنسان , كو كان من خصائصها و من وجهة نظر فلسفية هي تساوي النقافات و العمل بعيد عن الانتقائية. - (العقلاهية الجديدة : القائمة على فكرة النمط Type و النظرة المثالية للأشكال و المحلية و التي تبلورت بالضد (Jencks,p130). من الوظيفية و الو اقع الاجتماعي الإقليمية : في بداية اللبعينات وهي تحترم الثقافات المحلية و المناخ و فــي بعــض الأحيــان النكنولوجيــ - (Ibid,p8 )
 من منطلق اجنماعي ، وتبعا لذلك ووفقا لما طرحه المنظرون المعماريون أمثال (Stern,Jencks) ومـــن خــــلا المحاو لات النقدية المستمرة و نتيجة للتحليلات الأساسية ، طرح تصنيف للتوجهات المعماريـــة المعاصــرة وفقـــا لاستحقاقات النظرة المعاصرة إلى المجتمع وهي كالأتي(kaufman,1982,p8) :الو اقعية الاجنماعية ، التخطيط الاجنماعي و معارضة النظام، الانتقائية الر اديكالية و السميولوجية، العفوية و مدينة التعارضات ، التز اثثة الراديكالية و التفكير المتدرج، الحفاظية و إعادة التأهيل والأحياء. وممـا سبق يمكن أن نستخلص الفقرات الفرعية المرتبطة بمفردة الموقف من المجتمع ، التي يمكن تبويبها وفقا لما يأتي :-
- من حيث طبيعة التوجه الاجتماعي : أما خارجي يتعلق بعملية النمو في المجتمع و يــرتبط ارتباطـــا وثيةــا بالتحول الاجتماعي و التغير التكنولوجي أو داخلي : يتعلق بالنمو المـرفي ضمن المجال الواحد . - من حيث الأسس الفلسفية الفكرية :-أما اجتماعي و اقعي: يعكس الطروحات الفلسفية الو اقعية . أو اجتماعي عقلالي : يعكس الطروحات الفلسفية العقلانية. -الموقف من النتاريخ
تعددت معاني التاريخ المرنبطة بفلسفة العلم إذ تمايزت أربعة أنو اع شملت حسب Pierre Bont : - التاريخ الوثائقي :جميع النصوص المتعقةة بمنهجية العماء. - تاريخ الأخطاء: جمع سلسلة النظريات و الفروض العلمية التي تم وصفها خلال مختلف العصور • - التاريخ المكاني :البحث عن وطن للاكتثافات العلمية الكبرى ، لتتبع التيارات الجديدة التي تتنـا عنها و الذي يشكل الخصوصية العلمية أو الأصالة الفكرية لشعب ما الكامنة في طر ائق العمل التي يعتمدونها و العادات و الميول العقلية السائدة.
التاريخ الفلسفي للعلم : التاريخ الذي يربط الاكنشافات أو التيارات العلمية لا بمختلف الفلسفات الميتافيزيقية التي استتدت عليها ، بل بالفكر العلمي و بتطور العلم ذاته (الجابري،ص40 ). هذه المستويات من تاريخية الفلسفة العلمية تعكس الكيفية النتي نتصور بها تطور الـفاهيم و طــرق التفكيـر العلمية . هل هو (تطور منصل) أي بناء يشبد باستمر ار لبنة فوق لبنة . أم هو تطور منقطع (منفصل) بناء يـشيد ويعاد نتيده باسنمر ار ، يعلق د.الجابري على أن وجهة النظر اللسائدة اليوم قائمة على (الانفصـال) وهي تــــرى أن تطور المعرفة العلمية لا يستتد دوما على نفس المضامين التي تحملها المفاهيم و التطور ات العلمية في عصر من

العصور أو فترة من فتزات تطور العلم بل انه تطور يستند على إعادة بناء المفاهيم و التصور ات و النظريــات العلمية و إعادة تعريفها و إعطاءها مضمونا جديدا، أن تاريخ العلم ليس تاريخا استاتيكيا ، بل هو تاريخ ديناميكي ثوري يمتاز بخاصية نوعية . (الجابري ،ص 44).
و قد أكد كل من Popper و Kuhn على الاهتمام بالمسار الديناميكي الذي اكتسبت به المعرفة العلمية ،اكثــر من النزكيب المنطقي لنتائج البحث العلمي مؤكدين على الأهمية المركزية في الرجو ع إلى تاريخ العلم بـــستوياته المختلفة ، وقد أكد كل منها على النققدم الثوري للعلم بدلا من النققدم بالنمو (Kuhn,p18) و النتاؤل ما هــو الفــرق بين موقفيهما من النقاليد ؟
تناقش الزنكة في بحثها الموسوم (النظريات الأخرى في العالم) المقارنة بين Popper و Kuhn و واصفا مبدا الأول بالتخلص من الأخطاء و المرتبط بنموذج يصف نمو العلم على انه تحويرات متفرقـــة لاجــز اء المعرفـــة (الزنكة،ص 228) إذ نرفض نظرية Popper التبدلات الو اسعة النطاق ( الثورات في العلم ) فلا يؤمن ألا بالتحوير و النمو من خلال النطور ، و يصف (الزنكة) الفرق بينهما من خلال تأكيد Kuhn على الدور الإيجابي للنقاليد في نمو العلم ، بينما يؤكد الأخر على أفكار النقاليد (السابق،ص 233).
أي أن Kuhn ينظر إلى التاريخ من وجهة نظر صــورية تجـسيدية ( وهــي نظــرة مقيــدة بالتقاليـــ و بالمستوى الفيزيائي الوجودي) ، أمـا Popper فيركز على وجهة نظر التمثيل المعنوي للتقاليد ( المـستوى ( المـي

## الفكري المعنوي ) وهي نظرة منفتحة. <br> -العمارة و التاريخ

برز التنباين على مستوى العمارة بشكل واضتح خصوصـا على مستوى اللتوجهات المعماريـــة و المتعلةــة بمو قفها من النقاليد ، إذ برز نوجهين مختلفين في وجهات النظر المفسرة للتقاليد و بالتاللي إفر از ها لصيغ مختلفــــة للتعامل معها و التي يمكن تبويبها كالأتي : النوجه المحافظ : يتقبد بالثقاليد ر افضـا تنيير ها و متنبنياً صيغة الاستتسان - اللوجه التحرري: نادى بضرورة التحرر من قيود النقاليد و أيد تغيير هاو تعديلها ،إذ تبنـى صــيغة ( المحاكاة) .هذا التوجه الثناني برزت فيه على مستوى العمارة و جهات نظر مختلفة تمتلت بـــوقفي تياري الو اقعية الجديدة و العقلانية الجديدة،و التي عكست في مو اقفها بعض الجو انب المــشتركة بينهـــا وبين موقف طروحات فلاسفة العلم Popper وKuhn من التاريخ ، كما سيتضح من الآتي :يرى Rowe في ضوء الطروحات النقدية المكثقة للعمارة الحديثة التي استهوفت طر ح حلول بديلـــة اكثــر تكاملا و شمولية ، تصدي التيارات لا براز مشاكل العمارة الحديثة المتمثلة باستبعاد الماضي و نقاليده و مطورين نظريات و صيغا للتعامل معه, مستحضرين نظريات العلوم الإنسانية و خاصة علم التاريخ و اللغـــة و الاجتمـــاع لتطوير نظرياتهم الخاصة في تفسبر العمارة و تحدبد أهدافها (Rowe,p170) ،و يــرى Broadbent أن التيــارين طرحا أسساً فكريةً فسرت العمارة بمنظور جديد، فكلاهما لم يرفض فكرة النتبرير العقالانــي المنطقــي لأشـــكال العمارة و إنما اوصى تضمينها جو انب أخرى محنوية و إنسانية ، فتيار الو اقعية الجديدة فسر العمـــارة بمنظـور و اقعي جديد متأثز ا بمبادئ الفلسفة الو اقعية السائدة في المجتمع الأمريكي و التي من وجهة نظر البحث كما ســبق

تعكس طروحات الفلسفة الاجتماعية التي نادى بها Popper في فلسفته حول المجتمع المفتو ح في كتابه (المجتمــعـ المفنوح و أعداءه) و المرتبطة بنظريته الفلسفية العلمية (الزنكة ،ص 230 ) • و نيار العقلانية الجديدة الــذي فــسر العمارة بمنظور عقلاني جديد (حسب البحث عكس طروحات Kuhn الفلسفة العلمية) و التي يمند جذور ها حسب - (Broadbent,p81)، Descrates إلى Broadbent ويمكن نوضيح ابرز الأسس الفكرية التي طرحها التيارين و المرتبطة بمفردة (التـــاريخ) و المتو افقـــة مـــع

الطروحات الفلسفية العلمية بما يأتي Rowe,p159): - محاكاة و تمثيل عمارة الماضي و تقاليده لنولبد الأعمال الجديدة.

- العمارة بوصفها نتاجا حضـاريا يشبه اللغة.
- العمارة بوصفها ظاهرة مستقلة ، لغة تعبر عن ذاتها مبررين ذلك (كون لغة الأشكال الـــابقة تمثــل عو الم قائمة بحد ذاتها عبر الإنسان من خلالها عن عالمه) لذا فان إعادة تتكيل هذه اللغـــات الــسابقة . يمكن من نوليد لغات جديدة
- خلق عمارة تخاطب الإنسان بلغة بليغة معبرة تحقق الانتماء و التو اصل الحضاري ، عمارة تتفاعل مع

النقاليد لتجادل و تتاقش ، عمارة نقارن، عمارة تفسح مجالا للتعليق عن الإنسان و عالمه. - استثمار الستر اتيجيات النقدية في التعامل مع النقاليد كالاستعارة و إعادة التعريف و المقارنة الجدلية. مما سبق يمكن أن نتبين مـا يأتي :
أن الطروحات الفكرية (لمعمارية تعكس الثو افق مع الطروحات الفلسفية العلمية فمثّلا :
محاكاة عمارة الماضي و خلق عمـارة تعبر عن الاتتماء و التو اصل الحضاري ترتبط بالمـنـى المكـــــتي للتـــاريخ
 ترتبط بـالمعنى الوثائقي للتاريخ الفلسفي العلمي ، أما المستويات النقدية السابقة سواء في الاستراتيجيات أو في خلق العمارة التي تخاطب الإسلان و تفسح مجالات النقد و التغير فأنها ترتبط بالمعنى اللفلسفي العلمي للتاريخ ). أما على مستوى استخلاص المفردات الفرعية و المرتبطة بمفردة الموقف من التاريخ فيمكن بلورتها كما يأتي : (المفردة الرئيسة : الموفف من التاريخ

المفردات (الفرعية:

- (الموقف من حيث أسلوب التعامل مـ الثقاليد:أما وثائقيا أو أخطاءيا أو مكانيا أو فلسفيا. - الموقف من حيث العودة إلى التقاليد(يستثمر التقاليد و انظمتها التعبيرية في توليد أعمال جديدة) • و يشمل: 1- الموقف من حيث خصائص المراجع المحتمدة : أما فكرية معنوية أو فيزيائية مادية. 2- الموفق من حيث نوعية (طبيعة ) المراجع المعتمدة :أما مرجعية داخلية : تركز على المصادر المرجعية من داخل الحقل العرفي أو مرجعية خارجية : تركز على المصادر المرجعية من خارج الحقل المعرفي. تم في الفقر ات السابقة اسنكثشاف الأطر النظرية الكامنة في الطروحات الفلسفية العلمية و المعمارية واستخلاص بعض الجو انب التقصبلية المتعلقة بالمو اقف الفكرية العامة ،مشبرة في بعض قيمها إلى الجو انب المــشتركة بــين الأسس الفكرية لفلسفتي العلم عند Popper و Kuhn و الأسس الفكرية لتياري الو اقعية الجديدة و العقلانية الجديـــدة

من خلال مرجعيتهما خصوصـا ما يتعلق بمو فقهما من النظريات الاجنماعية أو موقفهما من النقاليد،مما دفع البحث لللوجه نحو الار اسات المعمارية المتخصصة لاستكثاف المو اقف الفكرية للتيارين. - المو اقف الفكريةة للو اقعية الجديدة و العقلالية الجديدة في العمـارة 1984/Scott طروحات -
ناقشت هذه الار اسة مجمو عة من المفاهيم بعضها عام والآخر خاص وفيما يخص المفاهيم العامة ، قارنت الار اسة بين تياريي الو اقعية الجديدة و العقلانية الجديدة موضحة اثتنر اكهما بمبدأ موحد (العودة إلى النقاليد) ، واختلافهما في طبيعة تلك العودة. (Harvard ,p6) وكالأتي:تنظر الو اقعية الجدبدة إلى التاريخ بوصفه مسنودعاً للصور الثكلية ويدمج نقالبد العمارة مع نقاليد أخرى مستمدة من مصادر خارج حقل العمارة ، بينما نميل العقلانية الجديدة في نظرنها إلى التاريخ بوصفه سلسلة متصلة من النتاجات تسنتبط من خلالها قو اعد و مبادئ العمارة (Harvard,p7) .أوضحت الار اسة خصوصية تيار العقالنية الجديدة في عودته إلى النقاليد بإبر از مفهوم النمط ( Type ) ومفهوم النحو لات النمطية مؤكدة على اسنتمار هذا المفهوم في التعامل مع النقاليد معتمدة على استثمار قو اعد التجميع و الثتركيب التي تميز أنماط الأبنية السابقة باعنبر ها أسسا كلية تخلق بموجبها الأشكال الجديدة ( Ibid,p7) فضلاً على اعتماده على الإسناد و الإشارة و الثلميح إلى أشنكال مسبقة ذات طابع فكري، ومن خلا ذلك التلميح إلى التصورات الفكرية عن الأشكال يكمن - ارنباط هذا المفهوم بالجو هر ويسمو فوق الممارسات الفردية (Ibid,p7) كما أثنارت الدر اسة إلى أن العقلانية الجديدة تستثمر فكرة النمط الفعال في نوليد نتاجا ته الحالية مبيناً أنها نكون مستمدة من نظريات معمارية سابقة ؛ تستثمر القدرة العالية للنمط على التحول ونوليد أنماط جديدة. ويتضح مما سبق أن ابرز الجوانب التي ركزت عليها الاراسة تمحورت حول جانبين رئيسيين هما مبدا العودة إلى التقاليد وطبيعة تلك العودة التي عرفت في ضوء جوانب اكثر تفصيلية. 1985/Colquhoun طروحات -
اهتمت هذه الار اسة بمناقثة التغير الحاصل في أنظمة النعبير، واوضحت خصوصبة الحقبة المعاصرة مقارنة بالحقب السابقة ( الكلاسيكية و الحدبثة ) ،فقد برزت من خلال المناقثة مجمو عة مفاهيم : استتمرت في نوضيح التباين في أنظمة التعبير التي شملت ( طبيعة الأشكال المستخدمة،طبيعة المعاني المرتبطة بها ، كيف تذرك تلك المعاني ) وفي ضو ءها طرحت خصوصية الحقبة المعاصرة وكما يأتي : تعمقت هذه الدر اسة في توضيح الاختلاف بين العقلانية الجديدة و الو اقعية الجديدة مستتدة إلى جانبين أساسيين هما : الجانب الأول،شمل كيفبة استثمار الأنظمة التعبيرية السابقة ، ومميزات النظام التعبيري الجديد ، وفي ضو ءه ، وصف تيار الو اقعية الجديدة ، كونه يستثمر الأنظمة التعبيرية السابقة كرموز مجز أة كالسقوف و النو افذ والأعدة ، أما نيار العقلانية الجديدة فقد عرف كونه سيستثمر الأنماط السابقة ويركز على الأنماط العامة - و الجانب الثثاني اوضحت الدر اسة من خلاله خصوصبة تيار الو اقعية الجديدة مبينة بان نظامه التعبيري الجدبد لا ينقيد بحقل العمارة بل أن رموزه منتو عة معمارية وغير معمارية ،اذ تحددها العو امل والظروف الخاصة بكل مشروع • في حين نجد اقتصـار أنظمة التعبير في الحقلانية الجديدة على حقل العمارة المستقل ذاتياً وباستثماره

| (3) | مجلة الهنسة | كانون الأول 2006 | المجلد 12 | العدد 4 |
| :---: | :---: | :---: | :---: | :---: |

لرموز تفهم معانيها ضمن إطار فكري يهذف إلى استرجاع العمارة باعتبارها تجربة جماعية

- ( Colquhoun,pp195-199 )

يتضح ما سبق أن أهم الجوانب التي وردت في وصف صيغ التيارين تمحورت حول جاتبين هما : كيفية استثمار الأظظمة التببيرية السابقة ( التقاليد ) ومميزات النظام التعبيري الجديد ، وقا وضح كل منهما في ضوء جو انبه التفصيلية .
1988/Rowe طروحات -
ناقشت هذه الدر اسة المفاهيم المرتبطة بالو اققية الجديدة و العقانية الجديدة على مستويين ،تبنى المستوى الأول مناقثة المفاهيم المشتركة التي اعتمدو ها شملت مو اقفهم تجاه النواحي الثالية : (نو عية المر اجع التي تتتمد في خلق التصاميم ، ماهية العمارة وأهدافها ، نو عية المناهج المستثمرة في خلق التصاميم ) ؛ في حين اعتمد المستوى الثاني على مقارنة صيغ التُعامل مع الانقاليد في كل منهما وتناول صيغتين رئيسيّين هما :( صيغة المعالجة اللنوية و التي تستثمر ها الو اقية الجديدة ، وصيغة النمط التي تستنمر ها العقلانية


 كالاقتباس و إعادة التنريف والجدل و المناظرة ( Rowe.p.P.150-155 )، أما بالنسبة للمستوى الخــاص و المتعلقــة بالمعالجة اللنوية و النمط حيث وضحت الار اسة صيغة المعالجة اللغوية من خال ممارسة المعماري بالثشكل آلاتي : استعارة و اقتباس عناصر رمزية مستقلة خارجة عن نطاق العمل ، تقحم فيه بقصد معين ، أما لتعديله
 الصيغة من خالل ممارسات المعمار A. RossI من خلال استتماره مفهوم النهط بوصفه تصور أ فكريأل للعالاةــات




ويتضح مما سبق أن طروحات Rowe تركز على جانبين أحدهما مرتبط بصيغ التصميم فيهما ، فبصض الجو انب ارتبطت بمو (قف مشتركة يؤمن بها معماريو التيارين شملت ثلاث أمور رئيسية هي: (نوعية الميا المصادر
 بعليات أسساسية يعتمدها المصمم كالاقتباس و الاستعارة و الإقحام في حالة المعمار Venturi ، و النمطوقواعد

ناقشت ابرز مديزات التيارين وعلى مستوى عام و تفصيلي : ففي المستوى الأول برزت مميز ات الو اقعية الجديدة من خلال ما يأتي : ( استثمار العالم الو اقحي مصدر ا للأشكال و الأفكار ، النوجه الو اقعي الذي يستتد على عناصر موجودة في الو اقع ، معالجة الأشكال بمنظور نسبي ، التحويل و التغريب و التهكم على الأشكال السابقة) ،أما لالـا لالـا العقالنية الجديدة فوضحت مميز اتها من خلال استثمار مفهوم النمط واسترجاع الاور المهم للأنماط التاريخية (أما على المستوى التقصيلي ، فقد وضحت من خلال مميز ات ابرز مؤسسي التيارين ، فقد وضح KLOTZ خصوصية المعماري R. VENTURI بإبر از الجو انب الآتية :(النظرة الو اقعية للعمارة واستثمار ما موجود مسبقاً وتعديله وتطويره ، استثمار نتاجات حضـارية مختلفة كمصادر للأفكار ، اعتماده على أسلوب التلميح و التداعي الفكري، استثماره لمفهوم البناية كسقيفة مزخرفة ، التخاطب بالصور المجازية ، دعوته لاستثمار مفاهيم اللتو ع و التعددية و النتاقض و الغموض . كما وضحت خصوصية المعمار A. ROSSI من خلال ما يأتي :(استر جاع الأنماط الأولية و البدائية للأبنية ، البحث عن قواعد عامة تلائم عدة مشاريع، نقبل الأشكال البسيطة و الاعتر اض على تجريدهامن المعاني و الرموز التاريخية).( KlotZ,P214).
يتضح من هذه الطروحات ، بأنها تضمنت جوانب مختلفة في توضيح صيغ التباين ؛ فبالنسبة للو اقعية الجديدة ، برزت مفاهيم متتوعة ارتبطت بمصادر الأشكال و الأفكار ومفاهيم مثل النسبية الو اقعية والاتصال من خلل العمـارة والتخاطب بالصور المجازية ؛ أما العقلالية الجديدة فبرزفيها التاكيدعلى فكرة النمط واستثثمار الأنماط

## 1988/JENCKS طروحات

وضحت طروحات JENCKS ممارسات مؤسسي النيارين من خلا جانبين رئيسيين هما :مفاهيمهم وخصائص نتاجاتهم كما يأنتي : بالنسبة للمفاهيم ، وضحJENKS مفاهيم المعماري R.VENTURI ممثل تيار الو اقعية الجديدة بالثكل الآتي: (الدعوة إلى استثمار النتاجات التاريخية مصدر أساسي في خلق الأعمال الجدبدة ، استثمار الأفكار المتاصلة في النقالبد السابقة كالغوض و النوتر ، ضرورة نضمين الأعمال المعمارية شفرات مختلفة نخاطب عامة الناس فضلاً عن

- (Jenks,P115) • (خاصتهم)

أما العقلانية الجديدة فشملت المفاهيم الآتية: (استثمار نظرية الذكريات المتر اكمة الجماعية و التي تقوم على تذكر الأبنية المهمة من خلا الخبرة و نر اكم المعرفة). (Ibid,p 116) ،ويوضح JENKS خصـائص نتاجاتهم ، من خلال التركيز على الخصائص المميزة لأعمال VENTURI و المتمتلة بــ ( امتلاكها خاصية الإشـارة المزدوجة ، استثمار ها لخاصية الدحاور المنحرفة وخاصية اللانتاظر ، و النوازن الديناميكي للعناصر وخاصـة الإدغام ،وخاصية التزيين و النشويه للأشكال البسيطة (Ibid,p 117) ،فضلا عن الإشارة إلى الخصائص الممبزة لنتاجات A. RoSSI و المتمتلة بــ ( الإشارة إلى معالم المدينة النقليدية الكلاسيكية وتبسيطها ،استرجاع التنظيمات الكاسيكية المحدثة بأسلوب معماريّ الثورة الفرنسية أمثال LEDOUX (Ibid,p118) . ( ) .

| (1) | مجلة الهنسة | كانون الأول 2006 | المجلد 12 | العدد 4 |
| :---: | :---: | :---: | :---: | :---: |

تبين من تحليل الطروحات السابقة ، للكثنف عن ابرز الجو انب التي وصفت في ضو هها التيارين ، بأنها طرحت جو انب كثيرة ومتتوعة شملت : المفاهيم و المبادئ التي ينبناها معماريو التيارين ، مميز ات أنظمتهم التنبيرية ، كيفية الستثمار هم للالقاليد ، تعبير هم عن معان معينة ، أسلوب إثشارتهم إلى الثقاليد ، و عمليات التحويل للأشكال السابقة . وبعد التنرف على هذه الجو انب التي اعتمدتها الطروحات السابقة يمكن تحديد مجمو عة من الاستتتاجات حول طبيعة هذه الجو انب و المعرفة المرتبطة بها و كالأتي : - أن الجو انب التي تطرحها الدر اسات متباينة ومتتوعة .

- لـ تتبلور هذه الجو انب في مفردات و اضحة ومحددة يمكن اعتمادها مباشرة وبالتالي تتكيل الإطار في المر حلة الأخيرة .

فالتباين في نو عية الجو انب المعتدة ، برز من خلال تكر ار جو انب محددة في معظم الار اسات و اقتصـار ذكر جو انب أخرى على بعض الدر اسات فقط ، وعلى سبيل المثال فقـ وصفت معظم الار اسات المفاهيم و المبـــادئ
 مفردات واضحة ومحددة فقـد برزت بشكل و واضح في جميع الطروحات حيث اتصفت بعموميـــة الطــر حـو وتــــاخل اللفاهيم مويكن استخلاص المو اقف الفكرية للو اقعية الجديدة و العقالنية الجديدة كما يأتي: - استخلاص المو اقف الفكرية للو اقعية الجديدة و (العقلالية الجديدة المو اقف الفكرية المشتركة
 يميز العمارة نتاجاً حضارياً كاللغة ، تعكس معاني وأفكار وتعبير عنها باستثمار قار ات اللغة التتبيرية و الجدلية ، فدر Colquhoun قارنت النظام التعبيري للتيارين وميزته عن نظام العمارة الحديثة مبينة استثمار هم لفكــرة الثشكل الرمز في التعبير عن معاني خاصة بينما يستثمر تبار العمارة الحدبثة الثشكل المجرد في التعبير عن معــانٍ عامة، و دراسة Rowe بينت بان التيارين يستثمر ان قـرات اللغة التنبيرية البلاغية وفــن المنــار الظرة و الجـــل لتحقيق أهداف أساسية للمجتمع كالتخاطب و التناعل الإيصال ، يتضح من هذه الطروحات بان التيان التارين يـشتركان في مبدا موحد يشبه العمارة باللغة ويستشمر قـرا اتها التعبيرية - الموقف تجاه استثمار التقاليـــ : عرفت معظم الطروحات صيغ التيارين ، بكونها تؤيد التقاليد السابقة وتستتمر أنظمتها الرمزية في توليد أعمال جديدة ، فطروحــات (Klots,Jencks,Colquhoun،Scott) أثنــارت إلــى
 طروحات Rowe فقـ أضافت بان هذا المبدأ يستثـمر لتحقيق أهداف مهمة كالثو اصل و الاستمر ارية الحـضارية و الفهم العام المشترك . - الموقف تجاه المراجع المعتمدة : عرفت الطروحات صيغ التيارين كونها تعتمد العمارة كمرجع أساسي تتولا منه الأعمال الجديدة فقـ أثنارت دراسة ( Scott) إلى اثنتر اك الثتارين في مبدا موحد يعتبر العمارة مرجعاً أساسيا ولكنها ميزت تيار الو اقعية الجديدة بكونها تستثمر مصادر أخرى إضافية . ألما Colquhoun فقد أكدت على تتوع الرموز في تيار الواقية الجديدة بين رموز معمارية و غير معمارية واختصار ها على الرموز المعمارية في تيار

العقلانية الجديدة ، من ناحية أخرى قارنت طروحاتRowe بين مر اجع التيــارين ومر اجـــع العـــــارة الحديثـــة فالأخيرة تستثمر مصـادر من خارج حقل العمارة كالطبيعة أو النكنولوجيا - الموقف تجاه نوعية المناهج والمتراتيجيات المعتمدة في خلق الأعمال ؛ يستثمر التيارين وفقــاً للطروحــات اللسابقة سترتيجيات لغوية نقدبة ، فقد وصف استر اتيجيات التيارين بأنهما يـستتثمر ان ســترتيجيات نقديــة مثـــل ( الاقتباس و إعادة التعريف و الجدل و المناظرة ) ،

- المو اقف الفكريـة المتباينة :

استتد نوضيح المو اقف المتباينة إلى استخلاص القضايا التي نوقشت بصددها هذه المو اقف وبشكل عام يمكن تحديد ابرز المو اقف التي اختلف فيها التياران بالنقاط الآتية :

- الموقف تجاه النظريات الفلسفية : تبرز المو افق الخاصـة للمصمم في تبنية نظريات فلسفبة معنية دون غير هــــا تتعكس بالضرورة في نظرياته المعمارية فتيار الو اقعية الجديدة يتأثر بمبادئ الفلسفة الو اقعية و التجريبيـــة و هـــي الفلسفة الأكثر شيو عاً في المجتمع الأمريكي ، أما تيار العقالينـة الجديدة في إيطاليا فقـــد تـــأثر بمبــادئ الفــــسفة . Descarts العقلانية ومؤسسها الفيلسوف و الفيزيائي الفرنسي . الموقف تجاه نظريات العمارة : تبرز المو اقف الخاصة للتيارين في النظريات التي طرحها ابرز رواد التيــار وخاصة المعماريان Rossi\& VENTURI ، فبر غم الاشتر اك في قضـايا محددة عكست نظريـــاتهم اختلافــا فــي الدفاهيم ، فقد استثمر VENTURI وجهة النظر النسبية في تفسير العمارة مؤكداً أهميــة التفاصــيل و الأجــز اء ROSSI وخاصة العناصر الزخرفية و التزيبينية طارحاً وجهة النظر التتي تفسر العمارة كونها ابنية مزخرفة، أهـــا فقد عكست طروحاته نظرة شمولية كلية ارتبطت بالمدينة ونز اكيبها و بنيتها ،وبرز في طروحاته مفهـوم الــنـط وتحو لاته عبر الزمن كمفهوم أساسي
- طبيعة الأفكار و المعاني المقصودة في العمل : وصفت بعض الطروحات السابقة صــيغ التيــارين بكونهــا تستتمر رموز النقاليد وتعبر من خلالها عن معان جديدة ، ويتضح من هذه الطروحات بان الهـف الرئيسي من هذه الصيغة هو نوليد معان جديدة من معان سابقة فطروحات Colquhoun أوضحت بان رموز ومــــان تيــار الو اقعية الجديدة لا تتحدد بحقل العمارة ونستثمر رموز معمارية وغير معمارية بينما تقتصر رموز نيار العقلانيــة الجديدة على حقل العمارة فقط ، لقد بينت هذه الطروحات بان تحديد هذه الرموز و المعان يعتمد على الظــروف
 فقد وصفت المعاني المنعكسة في أعمال نيار العقلانية الجديدة بكونها معان تخـص العــــارة و أنماطهــا البنائية ووضحت أنو اعها في ثلاث هي : (معان سابقة وموروثة ومكتسبة ومنسوبة إلى تلـــك الأنمـــاط ، معـــان مرتبطة بأجز اء تلك الأشكال السابقة ، معان جديدة يقترحها المصم وتتتج من إعادة تجميع الأجز اء و العناصــر - في نسق جديد) وفي ضو ء ما سبق، يمكن توضيح المفردات كما في الجدول(1) الآتي :

جدول (1) يوضح المفردات الرئيسية و الفرعية المرتبطة بالمو اقف الفكرية للو اقية الجديدة و العقلاهية الجديدة

| القبم الممكنة | الفقر ات الفر عية |  | المفردة الرئيسية |
| :---: | :---: | :---: | :---: |
| العمارة لغة تعبير و تخاطب ، أهدافها تلبي متطلبات معنوية ومادية أهمها التو اصل و الاستمرارية الحضارية | 1. تجاه العمارة وأهدافها |  | الموقف الفكري للو اقعية الجديدة و العقلاهية الجديدة |
| العمارة هي المنفعة و المتاتة ، أهدافها:تلبية حاجات الإسان المادية |  |  |  |
| موقف مؤيد للتقاليد مزيحاً لها | 2.تجاه التقاليد |  |  |
| موقف مؤيد للتقاليد مؤكداً لها |  |  |  |
|  | 3.تجاه المراجع التي يتم محاكاتهم |  |  |
| مراجع خارجية ( مراجع من خارج العمارة .الطييعة / العاس ) <br> التكنولوجيا). |  |  |  |
| مناهج العلوم الإسانية /مفاهيم النقد الأدبي / جدل ومقارنة | 4. تجاه نوع المناهج و الاستر تيجيات |  |  |
| مناهج أخرى |  |  |  |
| تتبنى مبادئ الفلسفة الويا | 5.تجاه النظريات الفلسفية |  |  |
| تتبنى مبادئ الفلسفة العقالهاية |  |  |  |
| التركيز على معاني الأجزاء ( تزيين وزلخارف ) | 6.تجاه نظريات العمارة |  |  |
| التركيز على معاني الكل ( أنماط) |  |  |  |
| التعقيد و التناقض في |  |  |  |
| العمارة و اسطة لنقل الملا |  |  |  |
| (العمارة تغني الحياة |  |  |  |
| عو امل ذاتية تخص المصم | ماهية |  |  |
| عو امل موضو | اللعو امل |  |  |
| المشروع | المحددة |  |  |
| الجهة المستفيدة منه | للمعاني <br> والأفكار |  |  |

-الجو انب المتعلقة بفلسفة العلم عندPopper و Kuhn والو اقعية و العقلاهية|لجديدة في العمارة: تضمنت الفقرات السابقة بعض الجوانب المشتركة بين طروحات Popper والمو اقف الفكرية للواقعية

الجديدة،وبين طروحات Kuhn و المو اقف الفكرية للحقلانية الجديدة،و التي يمكن توضيحها بالمناقشة الآتية:
 الو اقعية الجديدة و طروحات Kuhn و العقانية الجديدة ،تتمتل في الموقف من العودة إلى النقاليـــ، خصوصا ما يتعلق بموقفهما من المر اجع المعتمدة سواء على مستوى خصائصها أو طبيعتها،فضلا عن النت افق في

الأسس الفكرية لتوجهاتهما مع نوجهات ما بعد الحداثة و من منطلق اجتماعي ، إذ ترنبط النظريـــة الاجتماعيـــة الو اقعية المنفتحة والتي نقترب من طروحات Popper الو اقعية في كتابه (المجتمع المفتوح و اعدائه ) مع الأسس الفلسفية للو اقيـة الجديدة في العمارة ، خصوصـا ما طرحه S.Brawn في كتابه (Architecture Test in aPluralistic Socity) الاجتماعية و مطلعة على النقافات الذوقية و التي تتبنى من اجلها العمارة ،مشبر ا إلى عمارة R.Venturi كونهــا

ر رائدة في هذا المجال فضلاعن إدخال العلوم الاجنماعية في العمارة ضمن الفضاء و المكان،(Scott,pp42-50) أما بالنسبة إلى طروحات Kuhn وتطابقها مع طروحات العقلانية الجديدة في العمارة،فقد أثنارت Scott اللى النز عات ذات التوجهات الاجتماعية الجديدة و التي احدثت ثوران فكري في الستينات من القرن العشرين ومنهــا Stern\&Jencks العقلانية الجديدة القائمة على فكرة النمط و النظرة المثاللية للأشكال المحلية ، فضلا عن ما قدمه من در اسة نقديـة طرحا من خلالها بعض النز عات ذات التوجهات المحا فظة (التنر اثية الردايكاليــة ،الحفاظيــة ، إعادة التأهيل و الإحياء) و التي تعكس الأسس الفكرية للو اقعية الجديدة في نظرتها المحافظة إلى المجتمع ،و التــي تتطابق مع ما تطرحه (الزنكة) حول فكرة اللوجه الداخلي في نمو العلم ، كونه متعلقا بنمو المعرفة العلمية ضمن مجالها المعرفي و التي تتعكس من خلال(ميز ان التصريف)مما يضفي عليها الصفة المحافظةو المستقلة عن المجتمع


مخطط (1) يوضح الجو انب المشتركة بين طروحات Popper و الو اقعية الجديدة و طروحات Kuhn و العقلاثية الجديدة

ومما سبق يمكن أن نبلورمفردة تتعلق بالمو اقف الفكريةالعامة تتمنّل بـ(الموقف من التيارات المعمـارية)كما يأتي:

| (18) | مجلة الهنسة | كانون الأول 2006 | المجلا 12 | العدد 4 |
| :---: | :---: | :---: | :---: | :---: |

الجدول(2) الفقرات الفرعية المتعلةّ بالموقف من التيارات المعمارية

| القيم الممكنة | (الفقرات الفرعية | (المفردة الرئيسية |
| :---: | :---: | :---: |
| تيار الو اقية الجديدة | من حيث نوعها | الموقف من التيارات المعمارية |
| تيار العقلانية الجديدة |  |  |
| تتبنى مبادئ الفلسفة الو الو | من حيث موقفها من |  |
| تتبنى مبادئ الفلسفة العقلاهية | النظريات الفلسفية |  |
| موقف مؤيد للتقاليد مزيحاً لها | من حيث موقفها من |  |
| موقف مؤيد للتقاليد مؤكداً لها | التقالبي |  |
|  | من حيث موقفها من |  |
| التركيز على معاني الكل ( أنماط) | نظريات العمارة |  |
| مراجع داخلية( العمارة وتقاليدها هي المرجع الأساس) و مراجع خارجية ( مراجع من خارج العمارة .الطبيعة / هر الرا (التكنولوجيا) | من حيث موقفها من المراجع التي يتم محاكاتهم |  |
| مراجع داخلية( العمارة وتقاليدها هي المرجع الأساس ) |  |  |
| عوامل ذاتية تخص المصم | من حيث ماهية العو امل |  |
| عوامل موضوعية تخص المشروع | المحدة للمعاني والأفكار |  |
| عو امل ذاتية وعو امل موضنو |  |  |

وبعد مناقثة الجو انب المشتركة بين الطروحات الفلسفية العلمية والمعمارية، يمكن أن نلخـص المو اقــ
الفكرية العامة كما في الجدول الاتتي:
يوضح الجدول (3) المو اقف الفكرية العامة و الثمردات الفرعية المرتبطة بها و القيم الممكنة

| القيم الممكنة |  | الفقرات الفرعية | المفردة الرئيسية |
| :---: | :---: | :---: | :---: |
| علم النفس التفاعلي | من حيث الأسس الفلسفية | الموقف من النظرية | المو اقف الفكرية |
| علم النفس الجشتالتي | النفسية | \|النفسية | العامة |
| تغير عقلاهي يقع ضمن عو الم منطق الاكتشاف العلمي | من حيث نوع التغير في الاكتثشف |  |  |
| تغير ديني يقع ضمن عو الم السايكولوجي الاجتماعي |  |  |  |
| تجربة-حسية و نظرية عقلاهية -تجربة جديدة | من حيث طريقة البناء الفكري | الموقف من نظريـة |  |
| عقلاهية نظرية -تجريبية -نظرية جديدة |  | المعرفة |  |
| معرفة احتمالية | من حيث المقامات الثكلية |  |  |
| معرفة يقينية مطقة | للمعرفة |  |  |
| معرفة جزئية | من حيث جزئية و كلية |  |  |
| معرفة كلية | المعرفة |  |  |


| أريج كريم مجيد السدان | اثر فلسفة العلم المعاصرة على العمارة |  |  |
| :---: | :---: | :---: | :---: |
| علاء عبد اللزاقة |  |  |  |
|  | من حيّ طبيعهّ التوجه الاجتماعي |  |  |
|  |  |  |  |
|  | من حيث الأسس الفلسفية الفكرية |  |  |
| عقلاهي |  |  |  |
| ويّة اجتماعية | من حيث طبيعة النزاعات المعمارية |  |  |
| علإية اجتماعية |  |  |  |
| الونائقي | من حيث أسلوب التعامل مع التقاليد |  | لوقف من التاريخ |
| الإطائي |  |  |  |
| الانكا |  |  |  |
| سفي |  |  |  |
| لفري(المعنوي) للتقاليد | من حيث العودة إلى التقاليد |  |  |
| الزيائي (المادي) للتقاليد |  |  |  |
| لخلية و خارجية | من حيث نوعية المراجع المعتدة |  |  |
|  |  |  |  |
| تخمين - تحليل تكنيبي- تخمين مغاير | من حيث المنهجية المعرفية |  |  |
| تركيب- تحليل إسنادي- تركيب معدل |  |  |  |


| تيار الو اقية الجديدة | \|من حيث نوعها | الموقف من التيارات المعمارية |
| :---: | :---: | :---: |
| تيار العقلاهية الجديدة |  |  |
| تتبنى مبادئ الفلسفة الو الو القية | من حيث موقفها من النظريات |  |
| تتبنى مبادئ الفلسفة العقلاهية | الفلسفية |  |
| موقف مؤيد للتقاليد مزيحاً لها | من حيث موقفها من التقاليد |  |
| موقف مؤيد للتقاليد مؤكداً لها |  |  |
| (التركيز على معاني الأجزاء ( تزيين وزيّا ولارف ) | من حيث موقفها من نظريات العمارة |  |
| (التركيز على معاني الكل ( أنماط) |  |  |
|  خارجية (من خارج العمارة .الطبيعة / التكنولوجيا) | من حيث موقفها من المراجع التي يتم محاكاتهم |  |
|  |  |  |
| عوامل ذاتية تخص المصم | من حيث ماهية العو امل المحدة |  |
| عوامل موضو عية تخص المشروع | للمعاني والأفكار |  |
| عو امل ذاتية وعوامل موضو عية |  |  |


| (1) | مجلة الهندس | كانون الأول 2006 | المجلد 12 | العدد 4 |
| :---: | :---: | :---: | :---: | :---: |

- ظهر للبحث أن فلسفة العلم المعاصر تهتم بتكوين الأحكام الثاملة المشتركة القائمة على التمايز النوعي الفردي لكل علم و الذي يكسب اللنتاج المعرفي الوحدة والثمولية و الجدة المتتامية، فضلا عن تبني النماذج الفكرية وخلــق الصور الذهنية عن العالم المحيط واستشعار الجمال الحسي و المطلق في النفس و الوجود. - تبين للبحث أن فلسفة العلم المعاصر فلسفة مفتوحة تؤكد على التعدد في زو ايا الرؤية للموضو ع الــــي تتركـــز دو افعه في إعادة البناء المنظم المتتامي، فضلا عن التداخل بين عالم العقل و معطيات التجربة و من ثــم إعـــادة التفسير الظرفي (الآني) اعنمادا على التداخل بين المعرفة العقلية و المعرفة التجريبية. - وفرت الطروحات والأدبيات السابقة قاعدة أساسية استثمرت لبناء إطار نظري اكثر شمولية ووضوحا ، يمكـن \&Popper من خلاله وصف تأثثير فلسفة العلم المعاصر على العمارة بشكل عام ، و تأثثير فلسفتي العلـــم عنــد . على العمارة بشكل خاص Kuhn - توصل البحث إلى بلورة خمسة مفردات فرعية ارتبطت بطبيعة المو اقف الفكرية العامة تمثلت ب(الموقف من نظرية المعرفة، الموقف من النظرية النفسية، الموقف من المجتمع، الموقف من التاريخ). - توصل البحث إلى بلورة بعض الجو انب المشتركة بين المو اقف الفكرية لفلسفة العلم عند Popper و المو اقــف الفكرية للو اقعية الجديدة في العمارة و بين المو اقف الفكرية لفلسفة العلم عند Kuhn و المو اقف الفكرية للعقلانيـــة

 أو اختصـار ها على داخل حقل العمارة ) و طبيعة التعامل مع التقاليد(التزكيز علــى الجانــب الفكــري لهـــا أو
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اثر فلسفة العلم المعاصرة على العمـارة
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علاء عبد الرزاق

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# AN APPROACH IN IMPROVING THE PROPERTIES OF SAND DUNES 

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#### Abstract

An experimental study to improve sand dunes to gain economic construction of highway using these locally available materials. The study was divided into two approaches; the first was by using different bituminous binder proportions from (2) to (10) percent, while the second was to use fine metals as reinforcement. The results show an increase in the degree of improvement as reinforcement layers and silt contents were increased. Also it was found that $8 \% 0$ f asphalt cement increase the stabilization of sand dunes.

الخلاصة أجريت در اســات مختبرية لتحسين الكثبان الرملية للحصول على مادة إنثـائية اقتصـاديةلاستعماها كمـادة انشلئية محلية في أعمـــال الطرق .قسمت الدر اسة إلى اتجاهين الأول باستعمال المحتوى الإسفلتي بنسب من (2)\% إلى( 10)\%بينما الاتجاه الثاني باستعمال شبكات التسليح تبين من النتائج إن هناك زيادة في درجة النحسين كلما زادت طبقات التسليح مع زيادة نسب الغرين.كذللك وجد أن النسبة 8\%من الإسفلت الأسمنتي قد سببت زيادة في تثبيت الكثبان الرملية.


## KEYWORDS

Sand Dunes, Local, Reinforcement, Asphalt, Triaxial

## INTRODUCTION

In south of Iraq, especially between Nasria and Basrah, sand dunes of uniform size are available in abundance and can be used for low- cost stabilizer constructions. Obviously these soils may be improved its properties and behavior in order to use it in project for strategic use as bridges, road, and building. Obviously, these roads should be constructed at much cheaper cost, using the locally available sand which are stabilized with bitumen and could be improved also by reinforced such types of soils which is one of considered methods in improvement for these in this study.

Reinforced Earth is a composite of material formed by the association of granular fill and tensile resisting elements (strips, grids or sheets) as reinforcement. This concept is totally based on the friction mobilized between the reinforcement and the soil grains surrounding it. Due to this interaction to a tensile normal load on the reinforcement mass will be transferred to a tensile force along the reinforcement. Consequently the reinforcing element will act as a tie between the particles of the fill material.

The modern technique was introduced by Vidal and earliest studied were dealt with retaining walls such as the work of Lee et al, AL-Hussainy and Perry and others. Then the advantage of reinforced earth as foundation material attracted many investigators
who studied the bearing capacity of reinforced earth slabs or subgrades, Binquet and Lee, Akinmusurg and Akinbolade.

Almost all types of sand and sandy soils have been successfully stabilized by the addition of bituminous materials like cutback emulsions or low viscosity straight run asphalt. Bituminous binders, when used as additive to non- plastic sand proved sufficient cohesion to develop resistance to displacements under wheel loads. The cementing process of sand - bitumen mixes is more effective when these are highly compacted at ambient temperature such stabilized and bitumen materials be used as sub-base or base courses for flexible pavements as studied by Singh et al (1979).

## - DUNE SAND:

The sand dunes were obtained from the dunes area south of Iraq, between Nasria and Basrah with specific gravity of (2.69) and gray in color.

## -GRAIN SIZE DISTURBUTION:

Fig. (1) gives the grain size distribution; it is mainly fine sand and has a sigmoid shape with a very well sorting.


Fig (1). Grain size distribution of dune sand

## -ATTERBERG LIMITS

Laboratory tests for liquid limit and plastic index determinations were conducted. The soil was found to be completely non- plastic in character.

## -DRY DENSITY

The maximum dry density of the dune sand as determined is $(1.7) \mathrm{gm} / \mathrm{cm}^{3}$, while the minimum dry density was found to be $(1.25) \mathrm{gm} / \mathrm{cm}^{3}$. The filling density used throughout the tests was $(1.45) \mathrm{gm} / \mathrm{cm}^{3}$ which gives a relative density of (51.9)\%. The angle of internal friction of dune sand at this density is (29) as determined from direct shear test.

## -BITUMINOUS MATERIALS

The road paving bituminous materials, as asphalt cement (85/100), RC selected for stabilization, for various reasons including their commercial and availability in
large quantity and the ease of mixing with sand. These binders were tested according Iraqi standard specification.

## REINFORCED TYPE:

The suggested type of reinforced used are fine metal wire mesh. The properties of this material are shown in table (1).
Table (1) properties of reinforcement used in the test

| Type of <br> reinforcement | Aperture size <br> $(\mathrm{mm})$ | Thickness <br> $(\mathrm{mm})$ | Tensile strength <br> $(\mathrm{kPa})$ |
| :---: | :---: | :---: | :---: |
| Fine wiremesh | $1.7 \times 1.7$ | 0.7 | 27.3 |

## TEST PROCEDURE

## STABILIZATION BY BITUMINOUS MATERIALS:

## TEST PROCEDURE:

Marshall Stability or Hveen stabilometer tests are commonly used to determine stability of sands for sand bitumen mixes as mentioned by Klarkson (1965).

Sand dunes and the selected grade of bituminous materials were heated separately to $\left(160 \mathrm{C}^{\circ}\right)$ and then mixed together in required proportion till a uniform color was obtained. Moulds of (4) cm in diameter (2.5) cm in height of Marshall stability apparatus were then prepared and tested at $\left(60 \mathrm{C}^{\circ}\right)$. Different bituminous binders in percent age varying from (2) to (10) percent by weight of sand dunes were used.

## . AGING AND CURING:

The half of specimens from each trial was subjected to aging in air at room temperature for (1), (7), and (15) days. The other half of sand - bitumen mix was subjected to curing in water for (1), (7), and (15) days. In both samples, A/C (85/100) and RC as a binder were used.

## . IMPROVING BY REINFORCED TYPES:

The samples used in the triaxial tests were (38) mm in diameter and (76) mm in length. All the samples were prepared by pouring the sand inside the triaxial mold in three layers. Each layer was compacted (using wooden tamping rod) to the required density. The reinforcing layers placed at the specified spacing provided that the uppermost and lowermost of reinforcing layers are located at half of the spacing from the top and bottom of the sample.

The conventional triaxial testing techniques as suggested by Bishop and Henkle were used in the investigation. Also to study the improvement which could be obtained in adding fine soil passing \#200? In the preparation of unreinforced and reinforced sand dune, different percentages of silt were added to the sand dune in order to investigate their effect on the strength of the reinforced soil. Table (2) is representing the main test program.

Table (2) Main test program

| Series of tests | Type of reinforcement | No. of reinforcing layers (N) | Silt content <br> $\%$ |
| :---: | :---: | :---: | :---: |
| 1ST | Fine metal wiremesh | $0,1,2,3$ | 0 |
| 2nd | Fine metal wiremesh | 0,2 | $10,25,50,60$ |

The all round pressure $\left(\sigma_{3}\right)$ was selected to be $(100) \mathrm{kN} / \mathrm{m}^{2}$ throughout the tests. A consolidated - Undrained Triaxial test were conducted. The rate of deformation was (0.6) $\mathrm{mm} / \mathrm{min}$ (chosen according to operation manual of W.Ferrance Company of Triaxial Test).

## TEST RESULTS AND DISCUSSIONS:

## Stabilization by bitumen:

The test results for marshal stability values for various sand- bitumen mixes tested reported in table (3) and represented graphically in figure (2), (3), (4), and (5).

A steady rise in the stability value is initially observed with increasing binder content up to an optimum binder content, beyond which it decrease. The fall in stability value is very sharp in the case of cutback ( Rc ). The maximum stability value is obtained at (8) percent for (A/C) (85/100) and (Rc), for one day aging (10.70 and 5.74 kN ).

From the results it is also observed that (A/C 85/100) prove to be the best binder for (8) percent of sand- bitumen mixes.


Fig (2). Marshall Stability vs. percent binder


Fig (3). Marshall Stability vs. percent binder


Fig (4). Marshall Stability vs. aging and curing of specimens (Binder A/C 85 - 100)


Fig (5). Marshall Stability vs. aging and curing of specimens (Binder R.C.)

Table (3) Effect of aging and curing Marshall stability (kN) Of Sand-Bitumen at $60^{0}$

| Stabilize <br> No. | Binder | $\%$ Binder | 1Day aging and <br> curing |  | 7Day aging and <br> curing |  | 15Day aging and <br> curing |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | aging | curing | aging | curing | aging | curing |
| 1 | A/C 85-100 | Sand +2\%Binder | 5.30 | 2.50 | 5.60 | 2.13 | 4.90 | 1.80 |
| 2 | A/C 85-100 | Sand +4\%Binder | 6.40 | 2.60 | 6.50 | 2.30 | 5.80 | 1.92 |
| 3 | A/C 85-100 | Sand +6\%Binder | 7.10 | 3.00 | 7.20 | 2.47 | 6.30 | 2.40 |
| 4 | A/C 85-100 | Sand +8\%Binder | 10.7 | 2.20 | 10.9 | 2.10 | 6.50 | 1.50 |
| 5 | A/C 85-100 | Sand +10\%Binder | 0.52 | 0.40 | 0.70 | 0.26 | 0.55 | 0.18 |
| 6 | RC | Sand +2\%Binder | 4.00 | 1.80 | 5.00 | 1.10 | 4.50 | 0.80 |
| 7 | RC | Sand +4\%Binder | 4.70 | 1.90 | 5.80 | 1.00 | 4.80 | 0.72 |
| 8 | RC | Sand +6\%Binder | 5.10 | 1.20 | 6.10 | 0.90 | 5.00 | 0.70 |
| 9 | RC | Sand +8\%Binder | 5.74 | 1.10 | 8.00 | 0.62 | 5.30 | 0.53 |
| 10 | RC | Sand +10\%Binder | 0.20 | 0.10 | 0.32 | 0.32 | 0.24 | 0.07 |

## EFFECT OF AGING AND CURING ON STRENGTH:

Aging have been increased stability for (7) days for both binder (A/C) and (Rc) [figure (2), (3)], while the curing have been decreased stability for (7) and (15) days [Figure (4), (5)] and the results were tabulated in table (2). It could be noted that for both binder the stability value increases with increasing period of aging to (7) days and stability values begun to decrease after (7) days period. Sand- bitumen mixes having optimum binder contents have shown the least - improvement of strength.

## Reinforcement OF Sand Dunes:

The relationships between stress- strain for dune sand and that provided with different layers of wire mesh reinforcement are plotted in fig. (6). It is obvious that the results of reinforced samples showed well-defined peak stress in contrary to the reinforced sand dunes, these results confirmed the results obtained by Al-Abdullah et al (1993), also it could be considered as identical with the failure criterion adopted by Akinmusuru and Akinbolade.


Fig (6). Stress-strain relationship of dune sand with different Layer of wire mesh reinforcement

The benefit of these results could be clearer if the results were expressed in term of Degree of Improvement (D.O.I.) which is the ratio of the peak deviator stress of reinforcement soil to the peak deviator stress of unreinforcement soil. It is clear that the deviator stress at failure increased with the increased of (D.O.I.), this also confirmed by ALOmari (1989). The results shows that reinforcement of the three reinforcing layers ( $\mathrm{N}=3$ ) gave largest degree of improvement for silt content equal to (0)\% as shown in Fig. (7). While the D.O.I. not much more than that for two reinforcing layers, these results could be attributed to the interaction between the soil particles and the wire mesh which helped to transmit the stress on a large area, much more that was from ( $\mathrm{N}=3$ ).


Fig (7). Degree of improvement against number of reinforcing layers ( $N$ )
The effect of adding variable percentage of silt (10, 25, 50, and 60)\% on stress-strain relationship to the sand dunes could be shown in Fig. (8). Also the variation of peak deviator stress of unreinforced and reinforced for different percent of silt with degree of improvement were shown in table (4). The optimum silt content (that gives maximum deviator stress and degree of improvement) was found to be (25)\% for unreinforced sand dunes.


Fig (8). Stress-strain relationship of unreinforced and reinforced Dune sand with different percent of silt

They can be attributed to presence of fine particles surround the reinforcing in addition to the friction mobilized between the reinforcement and surrounding soil.

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| :--- | :--- | :--- |

Table (4) Degree of improvement of dune Sand with different silt contents

| Silt content <br> $\%$ | Strength of non reinforced <br> dune sand <br> kPa | Strength of reinforced dune <br> sand(N=2) <br> kPa | D.O.I. |
| :---: | :---: | :---: | :---: |
| 0 | 108.68 | 205.5 | 1.89 |
| 10 | 115.39 | 312.42 | 2.71 |
| 25 | 122.81 | 346.68 | 3.1 |
| 50 | 133.35 | 344.69 | 2.58 |
| 60 | 142.41 | 340.25 | 2.38 |

## CONCULUSIONS:

From the basis of the last results and their discussions, the following conclusions are derived:

1. Sand dunes have no stability and could be not used for road construction purpose without stabilization and improvement and it could be improved by using fine wire mesh metal reinforcement.
2. Stability of stabilized sand dune increased as high as (10.70) kN when stabilized with bituminous materials.
3. Aging process for specimen increases the stability value over period of (7) days for both binders.
4. The degree of improvement shows an increase in shear strength at silt content of (25)\% to the reinforced sand dunes.
5. Sand Dunes could be improved by using fine wire mesh metal reinforcement. The degree of improvement showed an increasing by addition of reinforcement and is proportional with the number of reinforcing lager.

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# AN IMPROVED NEWTON METHOD FOR RADIAL DISTRIBUTION SYSTEM LOAD ANALYSIS 

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#### Abstract

: This paper presents a modified Newton method of load flow analysis for radial distribution systems. It is derived with the Jacobian matrix is in $\mathbf{U D U}^{\mathbf{T}}$ form, where $\mathbf{U}$ is a constant upper triangular matrix depending solely on system topology and $\mathbf{D}$ is a block diagonal matrix. With this formulation, the conventional steps of forming the Jacobian matrix, LU factorization and forward/back substitution are replaced by back/forward sweeps on radial feeders with equivalent impedances. The method has advantages over Newton's method in terms of speed of solution (no. of iterations), and reliability of convergence by inserting a minimization technique (Cubic Interpolation Technique). The algorithm exhibits a control of the convergence. As such the method converges for cases when conventional Newton's method and some other popular methods diverge. Two large distribution systems of 490 nodes and 722 nodes with different $\mathrm{r} / \mathrm{x}$ ratio in line impedance are used to examine the performance of the method. These tests have shown that the proposed method is as robust and efficient as the forward/back sweep method. The proposed method can be extended to the solution of three phase unbalanced representation.


الخلا صة:
يقدم البحث طريقة نيونت-رفسن مطورة لتحليل انسيابية الاحمال الكهربائية لانظمة التوزيع الشعاعية. الطريقة المقترحة في
البحث اعتمدت على ان مصفوفة الجاكوبين نكون بشكل (UDUT) حيث ان مصفوفة [ U
علوية ثابتة تحتمد على طوباغر افية المنظومة بينما مصفوفة [D] تمتل مصفوفة قطريـة. من خلال هذه الصيخة، فان
الطريقة النقليدية لاعداد مصفوفة الجاكوبين وهي طريقة التحليل العلوي-السفلي ( LU ) و التعوبض ( forward/back )
قد استبدلت بطريقة ( back/forward sweeps) على المغذ يات الثـعاعية بممانعات مكافئة.
(الحل ( عدد العمليات النكرارية ), ووثوقية الوصول الى الحل من خلال استخدام تقنية التضئيل واستخدام عامل التصحيح
( ( ) . ان خوارزمبة الطريقة المقترحة تقدم سيطرة على عملى الو الوصول الى الحل الموثوق لانظمة مختلفة التعقيد بينما
طريقة نيوتن-رفسن التقليد يـة وطرق اخرى شـائعة تفشل في الوصول الى الحلـ
استخدم نظامان كبير ان لتوزيع الطاقة الكهربائية و هما (490 عقدة و 722 عقدة ) ذو نسب مختلفة مقاومة/محاثة لخطوط
اللنوزيع لتقيبي اداء الطريقة المقترحة. الدر اسة اظهرت قوة و وكفاءة الطريقة المقترحة في البحث, كما يمكن استخدامها في
انظمة احادية الطور وانظمة ثلاثية الاطوار غير المتوازنـة.

## KEYWORDS

Load Flow, Radial Distribution System, Newton's Method, Cubic Interpolation Technique.

## INTRODUCTION:

A load flow study involves the determination of voltages, currents, powers, and losses at various points in an electrical network under existing or contemplated condition of normal operation, subject to the regulating capability of generators, condensers, and tap changing under load transformers as well as specified net interchange between individual operating systems. In 1967, Tinney and Hart developed the Newton based power flow solution method [1]. Later work by Stott and Alsac [2] made the fast decoupled Newton method as well as its alternatives; a standard methods for load flow studies.

The Fast decoupled Newton method works well for transmission systems, though, its convergence performance is poor for most distribution systems due to their high $\mathrm{r} / \mathrm{x}$ ratio which deteriorates the diagonal dominance of the Jacobian matrix. For this reason several non-Newton type methods have been proposed [3-5]. Their algorithms all consist of back/forward sweeps on a ladder system. The formulation and the algorithm of these methods are different from the Newton's power flow method, which makes these methods hard to be extended to other applications, such as the state estimation and the optimal power flow, in
which the Newton method seems more appropriate.
Recently, a fast decoupled load flow method has been proposed in [6]. This method orders the laterals instead of busses into layers, thus reduces the problem size to the number of laterals, and then assumes initial end voltage for all laterals. The iteration starts from the first lateral using the method proposed in [4]. The voltage mismatch obtained from this lateral is applied to correct not only the end voltage of this lateral but also the end voltage of laterals of the next layer. The algorithm converges when all voltage mismatches are within a certain tolerance. Using lateral variables instead of bus variables makes this method efficient for a given system topology, but it may add some overhead if the system topology is changed regularly, which is common in distribution systems due to switching operations.

The purpose of this paper is to derive a modified Newton method for radial distribution systems without reducing the problem size, yet, capable of achieving robust convergence and high efficiency by inserting an accelerating and controlling factor using the cubic interpolation technique[7]. Specifically, this paper aim to derive a Newton algorithm in which the Jacobian matrix is in ( $\mathbf{U D U} \mathbf{U}^{\mathbf{T}}$ ) form, where $\mathbf{U}$ is a constant upper triangular matrix depending solely on system topology and $\mathbf{D}$ is a block diagonal matrix resulting from the radial structure and special properties of the distribution system. With this formulation, the conventional Newton algorithm of forming the Jacobian matrix, LU factorization and forward /back substitution can be replaced by back/forward sweeps on radial feeders with equivalent impedances. To assist in presenting the main difference between the proposed method and other methods, the following definitions are used:
(i) Conventional Newton method: a method in which the partial derivative of the power flow equation, i.e., the Jacobian matrix elements are used to determine the search direction, and forward/back substitutions on the $\mathbf{L U}$ factors of the Jacobian matrix are used to calculate the incremental correction of the state variables.
(ii) Back/forward sweep method: a method in which the derivative of the power flow equation is not used, instead, basic circuit laws, i.e. Ohm's law, KVL, and KCL (or the generalized KCL for power summation) are used as basis for back/forward sweeps on a radial network to calculate the incremental correction of the state variables.
(iii) Improved Newton method: the proposed method in which an approximate Jacobian matrix in $\mathbf{U D U}{ }^{\mathrm{T}}$ form is used to determine the sereach direction, the linearized power flow equation based on this Jacobian matrix is used as basis for back/forward sweeps on a radial network to calculate the incremental correction of the state variables.

By means of cubic interpolation minimization technique, the algorithm exhibits an accelerating factor $(\alpha)$ to control the convergence process.

## BASIC CIRCUIT THEORY IN DISTRIBUTION SYSTEMS[8]:

For a linear, time invariant RLC circuit with a sinusoidal voltage source, the basic circuit theory can be expressed as (see Appendix I for details):

$$
\begin{equation*}
\text { Ohm's law: } \quad \mathrm{I}_{\mathrm{b}}=\mathrm{Y}_{\mathrm{b}} \mathrm{~V}_{\mathrm{b}} \tag{1}
\end{equation*}
$$

$$
\begin{equation*}
\text { KCL: } \quad \mathrm{A}_{\mathrm{b}}=\mathrm{I}_{\mathrm{n}} \tag{2}
\end{equation*}
$$

KVL: $\quad b V_{b}=0$

For fundamental frequency power flow calculations, a distribution system is always modeled as a linear, time-invariant RLC circuit. Earth is always treated as a reference node. For a radial distribution system with ( n ) nodes and without shunt branches, the number of branches is $(n-1)$. Therefore, the dimension $\begin{aligned} & \square \text { matrix } \\ & A\end{aligned}$ is $\overrightarrow{n x(n-1)}$. $\quad\llcorner$

$\mathrm{V}_{\mathrm{n} 1} \quad$ loop 1

$\mathrm{V}_{\mathrm{n} 2}$
$\mathrm{V}_{\mathrm{b} 2}$
loop 2

$\mathrm{V}_{\mathrm{n} 3}$

## Fig (1)

The independent loop for radial distribution systems can always be formed by a branch with its two shunt branches. Since shunt branches are usually neglected in modeling distribution lines, a fictitious shunt branch can be placed with branch voltage to be the nodal voltage as shown in Figure (1), and eqn.(3) can be written as:

$$
\begin{equation*}
V_{b}=A^{T} V_{n} \tag{4}
\end{equation*}
$$

Combining eqn's (1), (2), and (4), we have:

$$
\begin{equation*}
A Y_{b} A^{T} V_{n}=I_{n} \tag{5}
\end{equation*}
$$

By knowing the nodal voltage at one node, assuming it is the first node(slack bus "s") for convenience, and nodal current injections at the other ( $\mathrm{n}-1$ ) nodes, eqn. (6) can be derived from eqn. (5) for solving the remaining ( $\mathrm{n}-1$ ) unknown nodal voltages:

$$
A_{n-1} Y_{b}\left(A_{s}^{T} A_{n-1}^{T}\right)\left[\begin{array}{c}
V_{s}  \tag{6}\\
V_{n-1}
\end{array}\right]=I_{n-1}
$$

where $A=\left[\begin{array}{c}A_{s} \\ A_{n-1}\end{array}\right], \quad V_{n}=\left[\begin{array}{c}V_{s} \\ V_{n-1}\end{array}\right] \quad$, and $\quad I_{n}=\left[\begin{array}{c}I_{s} \\ I_{n-1}\end{array}\right]$

Note matrix $A_{n-1}$ is a square matrix. Since every branch is always directed away from one node and towards the other node, we have:

$$
\begin{array}{ll} 
& A^{T} \mathrm{~T}_{\mathrm{n}}=0 \\
\text { or } & \mathrm{A}_{\mathrm{s}}{ }^{T}+\mathrm{A}_{\mathrm{n}-1}{ }^{\mathrm{T}} \mathrm{e}_{\mathrm{n}-1}=0 \tag{7b}
\end{array}
$$

where $\mathrm{e}_{\mathrm{n}}$ and $\mathrm{e}_{\mathrm{n}-1}$ are unity column vectors with dimensions n and $\mathrm{n}-1$ respectively. Hence, eqn. (6) can be simplified as:

$$
\begin{equation*}
A_{n-1} Y_{b} A_{n-1}{ }^{T}\left(V_{n-1}-V_{s} e_{n-1}\right)=I_{n-1} \tag{8}
\end{equation*}
$$

$A_{n-1} Y_{b} A_{n-1}{ }^{T}$ is the Nodal Admittance Matrix. In other words, for a radial system without shunt branches, the nodal admittance matrix is formed as the product of three square matrices. If we organize eqn. (8) as follows:

$$
\begin{align*}
& \mathrm{A}_{n-1} \mathrm{I}_{\mathrm{L}}=\mathrm{I}_{\mathrm{n}-1}  \tag{8a}\\
& \mathrm{Y}_{\mathrm{b}} \mathrm{~A}_{\mathrm{n}-1} \mathrm{~T}\left(\mathrm{~V}_{\mathrm{n}-1}-\mathrm{V}_{\mathrm{s}} \mathrm{e}_{\mathrm{n}-1}\right)=\mathrm{I}_{\mathrm{L}} \tag{8b}
\end{align*}
$$

Solving for $\mathrm{I}_{\mathrm{L}}$ from (8a) is equivalent to the "Backward sweep", and solving for $\mathrm{V}_{\mathrm{n}-1}$ from ( 8 b ) is equivalent to the "Forward sweep". This observation is very important as it motivated us to der ve a Jacobian matrix in UDU ${ }^{\text {T}}$ form and a back/forward sweep algorithm for the
Newton method.

## THE IMPROVED NEWTON METHOD:

Under the following assumptions:
Small voltage difference between two adjacent nodes, no shunt branches, the Jacobian matrix for a radial system is formed as $U^{T}{ }^{\mathrm{T}}$, where U is a constant upper triangular matrix depending solely on system topology and D is a block diagonal matrix. The first assumption above is valid, since typical distribution lines are short and power flows are not high. The second assumption is not valid if there exist shunt capacitor banks, constant impedance loads, as well as non-negligible shunt admittance of distribution line models ( $\pi$-model). However, all the shunt branches can be converted to node power injections using initial and updated node voltages. In the conventional Newton method[7,9,10], the power flow problem is to solve eqn.(9) for $\Delta \theta$ and $\Delta V$ :

| H | N | $\Delta \theta$ | $\Delta \mathrm{P}$ |
| :--- | :--- | :--- | :--- |
| J | L | $\Delta \mathrm{V} / \mathrm{V}$ | $\Delta \mathrm{Q}$ |

where

$$
\begin{array}{ll}
\mathrm{H}_{\mathrm{km}}=-\mathrm{V}_{\mathrm{k}} \mathrm{~V}_{\mathrm{m}}\left(\mathrm{G}_{\mathrm{km}} \sin \theta_{\mathrm{km}}-\mathrm{B}_{\mathrm{km}} \cos \theta_{\mathrm{km}}\right) & \mathrm{m}=\mathrm{k} \\
\mathrm{H}_{\mathrm{kk}}=\mathrm{V}_{\mathrm{k}} \Sigma \mathrm{~V}_{\mathrm{m}}\left(\mathrm{G}_{\mathrm{km}} \sin \theta_{\mathrm{km}}-\mathrm{B}_{\mathrm{km}} \cos \theta_{\mathrm{km}}\right) & \mathrm{m}=1, . . \mathrm{n}, \mathrm{~m} \neq \mathrm{k} \\
\mathrm{~N}_{\mathrm{km}}=-\mathrm{V}_{\mathrm{k}} \mathrm{~V}_{\mathrm{m}}\left(\mathrm{G}_{\mathrm{km}} \cos \theta_{\mathrm{km}}+\mathrm{B}_{\mathrm{km}} \sin \theta_{\mathrm{km}}\right) & \mathrm{m}=\mathrm{k} \\
\mathrm{~N}_{\mathrm{km}}=-\mathrm{V}_{\mathrm{k}} \Sigma \mathrm{~V}_{\mathrm{m}}\left(\mathrm{G}_{\mathrm{km}} \cos \theta_{\mathrm{km}}+\mathrm{B}_{\mathrm{km}} \sin \theta_{\mathrm{km}}\right)-2 \mathrm{~V}_{\mathrm{k}}^{2} \mathrm{G}_{\mathrm{kk}} & \mathrm{~m}=1, . . \mathrm{n}, \mathrm{~m} \neq \mathrm{k} \tag{13}
\end{array}
$$

$$
\begin{array}{ll}
\mathrm{j}_{\mathrm{km}}=\mathrm{V}_{\mathrm{k}} \mathrm{~V}_{\mathrm{m}}\left(\mathrm{G}_{\mathrm{km}} \cos \theta_{\mathrm{km}}+\mathrm{B}_{\mathrm{km}} \sin \theta_{\mathrm{km}}\right) & \mathrm{m}=\mathrm{k} \\
\mathrm{j}_{\mathrm{kk}}=-\mathrm{V}_{\mathrm{k}} \Sigma \mathrm{~V}_{\mathrm{m}}\left(\mathrm{G}_{\mathrm{km}} \cos \theta_{\mathrm{km}}+\mathrm{B}_{\mathrm{km}} \sin \theta_{\mathrm{km}}\right) & \mathrm{m}=1, . . \mathrm{n}, \mathrm{~m} \neq \mathrm{k} \tag{15}
\end{array}
$$

$$
\begin{equation*}
\mathrm{L}_{\mathrm{km}}=-\mathrm{V}_{\mathrm{k}} \mathrm{~V}_{\mathrm{m}}\left(\mathrm{G}_{\mathrm{km}} \sin \theta_{\mathrm{km}}-\mathrm{B}_{\mathrm{km}} \cos \theta_{\mathrm{km}}\right) \quad \mathrm{m}=\mathrm{k} \tag{16}
\end{equation*}
$$

$\mathrm{L}_{\mathrm{kk}}=-\mathrm{V}_{\mathrm{k}} \Sigma \mathrm{V}_{\mathrm{m}}\left(\mathrm{G}_{\mathrm{km}} \sin \theta_{\mathrm{km}}-\mathrm{B}_{\mathrm{km}} \cos \theta_{\mathrm{km}}\right)+2 \mathrm{~V}_{\mathrm{k}}{ }^{2} \mathrm{~B}_{\mathrm{kk}} \quad \mathrm{m}=1, . . \mathrm{n}, \mathrm{m} \neq \mathrm{k}$
$\mathrm{G}_{\mathrm{km}}+\mathrm{jB}_{\mathrm{km}}$ is the entry of nodal admittance matrix. Since the voltage difference between two adjacent nodes is small as well as: $\mathrm{G}_{\mathrm{kk}}+\mathrm{jB}_{\mathrm{kk}}=-\Sigma\left(\mathrm{G}_{\mathrm{km}}+\mathrm{j} \mathrm{B}_{\mathrm{km}}\right)$,
for systems without shunt branches, the Jacobian matrix can be approximated as:

$$
\begin{equation*}
\mathrm{H}_{\mathrm{km}}=\mathrm{V}_{\mathrm{k}} \mathrm{~V}_{\mathrm{m}} \mathrm{~B}_{\mathrm{km}} \cos \theta_{\mathrm{km}} \quad \mathrm{~m} \neq \mathrm{k} \tag{18}
\end{equation*}
$$

$$
\begin{array}{cl}
\mathrm{H}_{\mathrm{k} \mathrm{k}}=-\mathrm{V}_{\mathrm{k}} \Sigma \mathrm{~V}_{\mathrm{m}} \mathrm{~B}_{\mathrm{km}} \cos \theta_{\mathrm{km}} & \mathrm{~m}=1, . \mathrm{n}, \mathrm{~m} \neq \mathrm{k} \\
\mathrm{~N}_{\mathrm{km}}=-\mathrm{V}_{\mathrm{k}} \mathrm{~V}_{\mathrm{m}} \mathrm{G}_{\mathrm{km}} \cos \theta_{\mathrm{km}} & \mathrm{~m} \neq \mathrm{k} \tag{20}
\end{array}
$$

$\mathrm{N}_{\mathrm{kk}}=\mathrm{V}_{\mathrm{k}} \Sigma \mathrm{V}_{\mathrm{m}} \mathrm{G}_{\mathrm{km}} \cos \theta_{\mathrm{km}} \quad \mathrm{m}=1, . . \mathrm{n}, \mathrm{m} \neq \mathrm{k}$
$\mathrm{j}_{\mathrm{km}}=\mathrm{V}_{\mathrm{k}} \mathrm{V}_{\mathrm{m}} \mathrm{G}_{\mathrm{km}} \cos \theta_{\mathrm{km}} \quad \mathrm{m}=\mathrm{k}$
$\mathrm{j}_{\mathrm{kk}}=-\mathrm{V}_{\mathrm{k}} \Sigma \mathrm{V}_{\mathrm{m}} \mathrm{G}_{\mathrm{km}} \cos \theta_{\mathrm{km}} \quad \mathrm{m}=1, . . \mathrm{n}, \mathrm{m} \neq \mathrm{k}$

$$
\left.\mathrm{L}_{\mathrm{kh}}=\mathrm{V}_{\mathrm{k}} \mathrm{~V}_{\mathrm{m}}\right]\left[\mathrm{B}_{\mathrm{km}} \cos \theta_{\mathrm{km}} \quad\right] \mathrm{m} \neq \mathrm{k} \quad[\quad]=\left[\begin{array}{l}
\quad] \tag{24}
\end{array}\right]
$$

$\mathrm{L}_{\mathrm{kk}}=-\mathrm{V}_{\mathrm{k}} \Sigma \mathrm{V}_{\mathrm{m}} \mathrm{B}_{\mathrm{km}} \cos \theta_{\mathrm{km}} \quad \mathrm{m}=1, . . \mathrm{n}, \mathrm{m} \neq \mathrm{k}$
Equations (18) to (25) shows thath matrices $\mathrm{H}, \mathrm{N}, \mathrm{j}, \mathrm{L}$ all have the same properties (symmetry, sparsity pattern) as those of the nodal admittance matrix, hence they can be formed as:

$$
\begin{align*}
& H=L=A_{n-1} D_{B} A_{n-1}{ }^{T}  \tag{26}\\
& j=-N=A_{n-1} D_{G} A_{n-1}{ }^{T} \tag{27}
\end{align*}
$$

where $D_{B}$, and $D_{G}$ are diagonal matrices with diagonal entries to be $V_{k} V_{m} B_{k m} \cos \theta_{\mathrm{km}}$ and $\mathrm{V}_{\mathrm{k}} \mathrm{V}_{\mathrm{m}} \mathrm{G}_{\mathrm{km}} \cos \theta_{\mathrm{km}}$ respectively. Therefore eqn. (9) can be rewritten as:
$\mathrm{A}_{\mathrm{n}-1}$
$\begin{array}{lll} & D_{B} & -D_{G} \\ A_{n-1} & D_{G} & D_{B}\end{array}$
$\mathrm{A}_{\mathrm{n}-1}{ }^{\mathrm{T}} \mathrm{A}_{\mathrm{n}-1}{ }^{\mathrm{T}}$
$\Delta \theta$
$\Delta \mathrm{V} / \mathrm{V}$
$\Delta \mathrm{P}$
$\Delta \mathrm{Q}$

It is also noted that if nodes and branches are ordered properly, $\mathrm{A}_{\mathrm{n}-1}$ is an upper triangular matrix with all diagonal entries to be 1 and all non-zero off- diagonal entries to be -1 . One way to achieve such an $\mathrm{A}_{\mathrm{n}-1}$ is ordering branches by layers away from the root node (source bus)[3]. This ordering scheme is adopted here. The direction of each branch is towards the root node. The node ordering is proceeded simultaneously with the branch ordering. The branch "from side" node number is the same as the branch number, as illustrated in Fig (2). The node to branch incidence matrix of Fig (2) is given in eqn. (29).


By now
we have shown that the Jacobian matrix can be formed as the product of three square matrices eqn. (28), same as the nodal admittance matrix in eqn. (8). Next, we will show that eqn. (28) can be solved by back/forward sweeps as well. Let 's define:

$$
\begin{align*}
& \mathrm{E}=\Delta \theta  \tag{30}\\
& \mathrm{S}=\Delta \mathrm{P}  \tag{31}\\
& \mathrm{~W}= \tag{32}
\end{align*}
$$

$+\mathrm{j} \Delta \mathrm{V} / \mathrm{V}$
$+j \Delta Q$
$\mathrm{D}_{\mathrm{B}}+\mathrm{j} \mathrm{D}_{\mathrm{G}}$
then
eqn. (28) can be written as:

| $W_{n-1}{ }^{T} E=S$ |  |
| :--- | :--- |
| $A_{n-1} S_{L}=S$ | (33) ${ }^{A_{n-1}}$ |
| $A_{n-1}{ }^{T} E=S_{L}$ | or: |
| (34) |  |
| W |  |

Where eqn. (34) is the back sweep, the diagonal matrix W can be inverted for each line. The diagonal in $\mathrm{W}^{-1}$ is denoted as the equivalent line impedance:
$\mathrm{Z}_{\mathrm{eq}}=\mathrm{R}_{\mathrm{eq}}+\mathrm{j} \mathrm{X}_{\mathrm{eq}}$
Where

$$
\begin{align*}
& \mathrm{R}_{\mathrm{eq}}=\mathrm{X}_{\mathrm{km}} /\left(\mathrm{V}_{\mathrm{k}} \mathrm{~V}_{\mathrm{m}} \cos \theta_{\mathrm{km}}\right)  \tag{37}\\
& \mathrm{X}_{\mathrm{eq}}=\mathrm{R}_{\mathrm{km}} /\left(\mathrm{V}_{\mathrm{k}} \mathrm{~V}_{\mathrm{m}} \cos \theta_{\mathrm{km}}\right)
\end{align*}
$$

$\mathrm{R}_{\mathrm{km}}$ and $\mathrm{X}_{\mathrm{km}}$ are resistance and reactance of line $\mathrm{k}-\mathrm{m}$ respectively. Note that matrix $\mathrm{A}_{\mathrm{n}-1}$ of non-zero entries are either -1 or 1

## 4. CUBIC INTERPOLATION TECHNIQUE $[7,9,10]$ :

It is well-known that the load flow calculation can be regarded as a nonlinear programming problem [7], [9], which determines the direction and magnitude of the solution so that a certain function $\mathrm{F}(\mathrm{x})$ may be minimized. The $\mathrm{F}(\mathrm{x})$ is the squares of the active and reactive mismatch power. By employing this formulation, the valuable property can be obtained that the solution never diverges. The value of the function $\mathrm{F}(\mathrm{x})$ becomes eventually zero if there is a solution from the initial estimate, and stays at a positive value if no solution exists. In nonlinear programming approach (Fletcher-Powell method), ( $\Delta \mathrm{x}$ ) is modified by a correction factor ( $\alpha$ ) which can be considered as an acceleration factor. The computation of $(\alpha)$ is made such that $\mathrm{F}(\mathrm{x})$ is minimized $\mathrm{F}(\mathrm{x})$. The function to be minimized is

$$
\begin{equation*}
F(V, \theta)=\sum_{k \in P Q V}^{n} \Delta P_{k}^{2}+\sum_{k \in P Q}^{n} \Delta Q_{k}^{2} \tag{39}
\end{equation*}
$$

The minimization of $\mathrm{F}(\mathrm{x})$ with respect to $(\alpha)$ in the direction of $(\Delta x)$ is a onedimensional problem. The object is to determine the correction factor $(\alpha)$ given $(\Delta x)$ and the point ( x ). The problem can be stated as that of finding a value of ( $\alpha$ ) that will minimize :

$$
\begin{equation*}
\mathrm{Z}(\alpha)=\mathrm{F}\left(\mathrm{x}_{0}+\alpha \Delta \mathrm{x}\right) \tag{40}
\end{equation*}
$$

And therefore the derivative of $(\mathrm{Z})$ with respect to $(\mathrm{x})$ is :
$\mathrm{Z}^{\prime}(\alpha)=2 \sum f(y) \frac{\partial f(y)}{\partial y} \Delta x$
Where ;
$\mathrm{Y}=\mathrm{x}_{\mathrm{o}}+\alpha \Delta \mathrm{x}$
A cubic interpolation technique is used to find ( x ) as follows :

1) A step "a" is chosen as :
$\mathrm{a}=\min \left(1,-2\left(\mathrm{~F}_{\mathrm{x}}-\mathrm{F}_{\mathrm{o}}\right) / \mathrm{z}_{\mathrm{x}}^{\prime}\right)$
Where $\left(\mathrm{F}_{\mathrm{o}}\right)$ is an estimate of $(\mathrm{F})$ at the problem optimum, $(\mathrm{Fx})$ is the value of function ( F ) at point $(\mathrm{X})$, and $\left(\mathrm{Z}_{\mathrm{x}}{ }^{\prime}\right)$ is the derivative of $(\mathrm{Z})$ with respect to ( X ) evaluated at point (X).
2) A step of size (a) is taken to arrive at point (y), $y=X+\alpha \Delta X$, and ( $Z_{y}^{\prime}$ ) is evaluated to determine whether a change of sign has occurred with respect to $\left(Z_{x}{ }^{\prime}\right)$. Such a change of sign, from negative $\left(\mathrm{Z}_{\mathrm{x}}{ }^{\prime}\right)$ to positive $\left(\mathrm{Z}_{\mathrm{y}}{ }^{\prime}\right)$ would indicate that the minimum is enclosed within these two points. If there is no change of sign, successive steps of size (a) are taken until two adjacent points that enclose the minimum are found. Let these two adjacent point be called (w) and (y) which are located at distances $\left(\alpha_{w}\right)$ and $\left(\alpha_{y}\right)$ from the original point ( $x$ ).
3) The distance ( $\alpha$ ) from ( $x$ ) to the minimum point is:

$$
\begin{equation*}
\alpha=\alpha y-\frac{(\propto y-\propto w)\left(Z y^{\prime}+r-s\right)}{Z y^{\prime}-Z w^{\prime}+2 r} \tag{43}
\end{equation*}
$$

Where ;

$$
\begin{align*}
& \mathrm{r}=\left(\mathrm{s}^{2}-\mathrm{Z}_{\mathrm{w}}^{\prime} \mathrm{Z}_{y^{\prime}}\right)^{1 / 2}  \tag{44}\\
& \text { And } \mathrm{s}=3 \frac{\left(Z_{w}-Z_{y}\right)}{\left(\alpha_{y}-\alpha_{w}\right)}+Z w^{\prime}+Z y^{\prime}
\end{align*}
$$

4) The point $\left(x_{0}+\alpha \Delta x\right)$ is accepted as the minimum point if the function $F\left(x_{0}+\alpha \Delta x\right)=Z(x)$ is smaller than both $\left(\mathrm{Z}_{\mathrm{w}}\right)$ and $\left(\mathrm{Z}_{\mathrm{y}}\right)$. If this is not true, the interpolation is repeated using the point $\left(\mathrm{x}_{\mathrm{o}}+\alpha \Delta \mathrm{x}\right)$ and either (w) or (y), chosen so that the minimum is enclosed.

This decision is based on the sign of $Z^{\prime}(\alpha)$. The cubic interpolation process is shown in fig (3).


Fig.(3) Cubic interpolation to minimize $F(x)$ with respect to $(\alpha)$ in the direction of $(\Delta x)$
The interpolation process can be simply implemented in Newton's program. Equation (41) must be evaluated for several values of ( $\alpha$ ).
When $\alpha=0$,

$$
\begin{equation*}
\mathrm{f}(\mathrm{y})=\mathrm{f}(\mathrm{x}) \tag{45}
\end{equation*}
$$

and

$$
\begin{equation*}
\frac{\partial f(y)}{\partial y}=\frac{\partial f(x)}{\partial x} \tag{46}
\end{equation*}
$$

Therefore ;

$$
\begin{equation*}
2 \sum f(y) \frac{\partial f(y)}{\partial y} \Delta X=2 \sum f(x) \frac{\partial f(x)}{\partial x} \Delta X \tag{47}
\end{equation*}
$$

from the equation $f(x)=-J \Delta x$
$\therefore$ Equation (46) becomes :
$Z^{\prime}(0)=-2 \sum f(x)^{2}=-2 F(x)$
The minus sign of equation (47) shows the direction of minimization ( $\Delta x$ ) always points in a direction which reduces $\mathrm{F}(\mathrm{x})$ that the terms $\mathrm{f}(\mathrm{x})$, which represent the power mismatches, are calculated from the Newton algorithm, the optimum ( $\alpha$ ) and the new point $\left(\mathrm{x}_{1}=\mathrm{x}_{\mathrm{o}}+\alpha \Delta \mathrm{x}\right)$ is used for the start of the next iteration. The additional requirement
of this method is the re-evaluation of the Jacobian matrix which is small, using sparsity techniques. There is no need for extra Gauss - Eliminations and back substitutions, just addition evaluation of the Jacobian.

An algorithm based on eqns. (34), (35) and finding the optimal correction factor ( $\alpha$ ) following the cubic inlerpolation technique has been developed. Figure (4) is the flow chart of the proposed algorithm. The matrix $\mathrm{A}_{\mathrm{n}-1}$ has never been formed in the program since its non-zero entries are either -1 or 1 .


## ANALYSIS BASED ON NUMERICAL EXAMPLES:

A 490-node and 722--node typical distribution systems of various sizes taken the pacific Gas and Electric distribution system[5]. Both capacitors and regulators are included in the test systems, but the automatic controls for switching capacitors on/off, and the automatic tap adjustment function for regulators are not modeled in the test. All the loads are modeled as lumped constant power load. Table (1) lists the attributes of these test systems. It is seen that the two test systems have wide range of $\mathrm{r} / \mathrm{x}$ ratio and line impedance.

## Table(1) Attributes of Test systems

| Test system | No. of nodes | Voltage level (Kv) | r/x ratio |  | $\left\|\mathrm{Z}_{\mathrm{km}}\right\| \Omega$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Max | Min | Max | Min |
| 1 | 490 | 12 | 5.06 | 0.15 | 3.07 | 0.0012 |
| 2 | 722 | 12 | 5.06 | 0.26 | 2.43 | 0.0004 |

Table(2) shows that the load flow problem was solved by back/forward sweep conventional Newton's method in 4 iterations to an accuracy of $10^{-4}$ for each individual power mismatch $\left(\Delta \mathrm{P}_{\mathrm{k}}, \Delta \mathrm{Q}_{\mathrm{k}}\right)$. In the proposed method 3 iterations were required with the same accuracy. The values of optimum ( $\alpha$ ) obtained for each iteration in the proposed method were close to one. My experience has shown that optimum ( $\alpha$ ) is either close to 1 or very close to 0 . The cubic interpolation formula will produce an appropriate value of $(\alpha)$ even in the case where the optimum is near, but outside the interpolating limits. So optimum ( $\alpha$ ) may sometimes be slightly greater than one. If the interpolation is performed between zero and one, the correction ( $\alpha$ ) value would determined for all cases without any extra Jacobian calculation per iteration, thus saving computation time. From table (2), it is seen that the proposed method is as robust as the back/forward sweep method. All the cases tested have reached convergence regardless the wide range of $\mathrm{r} / \mathrm{x}$ ratio and line impedance. The principal value of the proposed method lies in the control of the convergence process for both weakly Meshed networks and data error cases, whereas using the conventional Newton's method alone during the iterations of a load flow problem may result in poor solution or divergence.

Table (2) Comparison of the proposed method with back/forward sweep method with the value of optimum ( $\alpha$ ).

| $\begin{array}{c}\text { Test system of } \\ \text { distribution sys. }\end{array}$ | $\begin{array}{c}\text { No. of iterations } \\ \text { Back/Forward } \\ \text { sweep method }\end{array}$ | $\begin{array}{c}\text { No. of iterations } \\ \text { Proposed method }\end{array}$ | $\begin{array}{c}\text { Optimum } \alpha \text { /iteration } \\ \text { Proposed method } \\ 1\end{array}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 2 | 3 | 4 |  |  |  |$]$

Table (3) Convergence pattern (power mismatches at each iteration) of the proposed method and the back/forward sweep method.

| Iteration | Test sys. 1 |  | Test sys. 2 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Proposed | B/F sweep | Proposed |
| B/F sweep |  |  |  |  |  |
|  |  |  |  |  |  |
| 1 | $\Delta \mathrm{P}_{\mathrm{k}}$ | 0.30000561 | 0.30000561 | 0.14006200 | 0.14006200 |
|  | $\Delta \mathrm{Q}_{\mathrm{k}}$ | 0.14322091 | 0.14322091 | 0.05244800 | 0.05244800 |
| 2 | $\Delta \mathrm{P}_{\mathrm{k}}$ | 0.00989422 | 0.00643219 |  |  |
|  | $\Delta \mathrm{Q}_{\mathrm{k}}$ | 0.00149278 | 0.01113158 | 0.01709456 | 0.00982138 |
|  |  |  |  |  |  |
| 3 | $\Delta \mathrm{P}_{\mathrm{k}}$ | 0.00009821 | 0.00057982 | 0.00012252 | 0.00415140 |
|  | $\Delta \mathrm{Q}_{\mathrm{k}}$ | 0.00002741 | 0.00027818 | 0.00011821 | 0.00148164 |
|  |  |  |  |  |  |
| 4 | $\Delta \mathrm{P}_{\mathrm{k}}$ |  | 0.00001753 | 0.00004853 | 0.00034887 |
|  | $\Delta \mathrm{Q}_{\mathrm{k}}$ |  | 0.00003554 | 0.00003041 | 0.00077424 |
|  |  |  |  |  |  |
| 5 | $\Delta \mathrm{P}_{\mathrm{k}}$ |  |  |  | 0.00015501 |
|  | $\Delta \mathrm{Q}_{\mathrm{k}}$ |  |  |  | 0.00005526 |

Note: All algorithms programs were executed using MATLAB 5.3.

## CONCLUSIONS:

This paper presents an improved Newton method for solving the load flow problem of radial distribution systems. The derivation of this method has revealed that under certain assumptions, the Jacobian matrix of a radial system can be formed as UDU ${ }^{\mathrm{T}}$, with identical topology to that of the nodal admittance matrix. The attractive characteristic of such a Jacobian matrix is to allow a back/forward iteration algorithm instead of the conventional LU factorization. Thus, the proposed method is more reliable in convergence with ill-conditioned radial distribution systems. Also, a more rapid convergence and a non-divergent characteristic for both well-conditioned and ill-conditioned systems by using the optimum correction factor $(\alpha)$ through the cubic interpolation technique. Tests of the proposed method on large distribution feeders have shown that it is as robust and efficient as the back/forward sweep method.

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## APPENDIX I:

For a linear, time-invariant RLC circuit with sinusoidal voltage, which a typical distribution system is modeled as, Ohm's law has the following familiar form[8]:

$$
\begin{equation*}
\mathrm{I}_{\mathrm{b}}=\mathrm{Y}_{\mathrm{b}} \mathrm{~V}_{\mathrm{b}} \tag{A.1}
\end{equation*}
$$

where $I_{b}$ : a vector of complex branch current,
$\mathrm{Y}_{\mathrm{b}}$ : a diagonal matrix with diagonal element to be branch admittance,
$\mathrm{V}_{\mathrm{b}}$ : a vector of complex branch voltage.
The directions of $\mathrm{I}_{\mathrm{b}}$ and $\mathrm{V}_{\mathrm{b}}$ must be consistent. For KCL, we have:

$$
\begin{equation*}
A \mathrm{I}_{\mathrm{b}}=\mathrm{I}_{\mathrm{n}} \tag{A.2}
\end{equation*}
$$

where $I_{n}$ : vector of nodal injection current,
A : node to branch incidence matrix, defined as:
1, if branch $m$ is directed away from node $k$
$A_{k m}=\quad-1$, if branch $m$ is directed towards node k
0 , if branch m is not incident to node k

Each row of (A.2) corresponds to KCL for a node. Since each branch is always directed away

## H.A. Kubba

from one node and towards one other node, the summation of all rows will end with zero. Hence, for a system with nodes, only ( $\mathrm{n}-1$ ) rows in (A.2) are independent. An arbitrary row can be removed from (A.2) so that the remaining ( $\mathrm{n}-1$ ) rows are independent. The node corresponding to the removed row is usually called the reference node. To express KVL in matrix form, a loop matrix B is defined as:

1, if branch m is in loop k , and their direction agree
$\mathrm{b}_{\mathrm{km}}=\quad-1$, if branch m is in loop k , and their direction oppose
0 , if branch m is not in loop k
Then KVL can be expressed as:

$$
\begin{equation*}
b V_{b}=0 \tag{A.3}
\end{equation*}
$$

Each row of (A.3) corresponds to KVL for a loop. It is not necessary to include all loops in (A.3) since independent loops are sufficient for $\mathrm{V}_{\mathrm{b}}$ to obey. The independent loop is defined as that not all the branches of the independent loop can be found in other independent loops.

# CURVATURE DUCTILITYOF REINFORCED CONCRETE BEAM SECTIONS STIFFENED WITH STEEL PLATES 

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#### Abstract

ABSTRCUT This paper presents theoretical parametric study of the curvature ductility capacity for reinforced concrete beam sections stiffened with steel plates. The study considers the behavior of concrete and reinforcing steel under different strain rates. A computer program has been written to compute the curvature ductility taking into account the spalling in concrete cover. Strain rate sensitive constitutive models of steel and concrete were used for predicting the moment-curvature relationship of reinforced concrete beams at different rate of straining. The study parameters are the yield strength of main reinforcement, yield strength of transverse reinforcement, compressive strength of concrete, spacing of stirrups and steel plate thickness. The results indicated that higher strain rates improve both the curvature ductility and the moment capacity of reinforced concrete beam sections. Moreover the section curvature ductility increases as the thickness of the stiffening plates decreases.


$$
\begin{aligned}
& \text { فدم هذا البحث در اسـة نظربه لقابلية مطيلبة الثقوس لمقاطع الاعتاب الخرسانبة المسلحه و المقو اة بـالصفائح الحدبدية. تم } \\
& \text { في هذه الدر اسه الأخذ بنظر الأعتبار تصرف كل من الخرسانة وفو لاذ النسليح تحت تأثنبر نسب قيم زمنية مختلفة للأنفعـــال. }
\end{aligned}
$$

$$
\begin{aligned}
& \text { اسنعمال مخططات متحسسه للمعدل الزمني للأنفعال لكل من الفو لاذ و الخرسانة وذللك لنوقع علاقة العزم مع الثفوس لمةـــاطع } \\
& \text { الاعتاب. المتغير ات النتي استخدمت في هذه الدر اسةة هي مقاومة الخضو ع لفو لاذ التسليح الرئبسي، مقاومة الخضو ع لفــو لاذ } \\
& \text { اللنسلبح الثانوي، مقاومة الانضغاط للكونكريت، مسـافات رو ابط الاعتاب و سمك صفائح الفو لاذ المقو اة. النتائج المستحــصلة } \\
& \text { من الدر اسه أثنارت الى أن زبادة المعدلات الزمنية للأنفعال تحسن من المقاو مة و قابلية العزم لمقاطع أعتـــاب الكونكربـــ } \\
& \text { المسلح. اضـافة الى ذلك ازدادت مطيلية الثقوس بنقصـان سمك صفائح الفو لاذ المقو اة. }
\end{aligned}
$$

## KEYWORDS

Curvature Ductility, Beams, Reinforced Concrete, Steel Plates, Strain Rate.

## INTRODUCTION

The philosophy of seismic design for moment resisting reinforced concrete frames is based on the formation of plastic hinges at the critical sections of the frame under the effect of substantial load
reversals in the inelastic range. The ability of the plastic hinge to undergo several cycles of inelastic deformation without significant loss in its strength capacity is usually assessed in terms of the available ductility of the particular reinforced concrete section.

The ductility capacity of reinforced concrete sections is usually expressed in terms of the curvature ductility ratio $\left(\mu_{\phi}=\phi_{u} / \phi_{y}\right)$ where $\phi_{y}$ is the curvature of the section at first yield of the tensile reinforcement and $\phi_{u}$ is the maximum curvature corresponding to a specific ultimate concrete compression strain.

The moment-curvature analysis of the section is usually performed under monotonically increasing load which represents the first quarter-cycle of the actual hysteretic behavior of the plastic hinge rotation under the earthquake loading. Therefore, $\mu_{\phi}$ of a section calculated under such assumption is a theoretical estimate of the actual inherent ductility of the section when subjected to an actual earthquake loading. However, the theoretical estimation of $\mu_{\phi}$ under monotonic loading is widely used as an appropriate indicator of the adequacy of earthquake resistant design for reinforced concrete members.

Steel plates have been used for many years due to their simplicity in applying and their effectiveness for strengthening and stiffening. The high tensile strength and stiffness lead to an increase in bending capacity and a reduction of the deformations. Hussain et. al (1995) ${ }^{[4]}$ tested eight beams of $(0.15 * 0.15 * 1.25 \mathrm{~m})$ with a steel ratio ( $\rho=0.0096$ ), the concrete cylinder strength was ( $f_{c}^{\prime}=31 \mathrm{MPa}$ ) and the average yield strength of the main steel and stirrups was ( 414 and 275 MPa ). The effect of plate thickness and plate end anchorage on ductility and mode of failure of beams were studied and concluded that increasing the plate thickness than 1 mm caused a premature failure due to tearing of concrete in the shear span at loads lower than that calculated according to the ACI code shear strength formula.

Soroushian and Sim (1986) ${ }^{[9]}$ used strain rate sensitive constitutive models for steel and concrete to predict the axial load-axial strain relationship of reinforced concrete rectangular columns at different rates of strain. The analysis parameters were the yield strength of reinforcement $\left(f_{y}=276,414,552 \mathrm{MPa}\right.$ ), the concrete strength ( $f_{c}^{\prime}=20.7,27.6 \mathrm{MPa}$ ), the steel ratio ( $\rho=0.026,0.032,0.04$ ) and the amounts of hoop reinforcement ( $\rho_{s}=0.01388,0.02082,0.04164$ ). The results indicated that for the range of analysis parameters considered and for the range of strain rates of $(0.00005 / \mathrm{sec}-0.5 / \mathrm{sec})$ the secant axial stiffness increases in the range of $(16 \%-36 \%)$. AlHaddad (1995) ${ }^{[1]}$ studied the curvature ductility for reinforced concrete beams under strain rates in a range of (static, 0.05 and $0.1 / \mathrm{sec}$ ) for values of ( $f_{y}=414,440,483,518 \mathrm{MPa}$ ) and reinforcement ratio ( $\rho=0.003,0.3$ ). He assumed that only the steel reinforcement is a strain rate sensitive. The results indicated that for a strain rate of $(0.05 / \mathrm{sec})$ the curvature ductility ratio was decreased by about $(12 \%)$ for an increase of ( 34.5 MPa ) in $f_{y}$ compared with that under static loading.

## MATERIAL MODELS OF THE PRESENT STUDY

## Constitutive Concrete Model

The concrete constitutive model adopted in the present study is that of Razvi \& Saatcioglu $(1999)^{[6]}$ which takes into account the cross sectional shape and reinforcement arrangements, Fig.(1). The effect of the strain rate had been accounted for in this model by using the two coefficients ( $k_{f}, k_{\varepsilon}$ ) as had been derived by Soroushian (1986) ${ }^{[9]}$ on the test results basis.
The ascending part of the proposed curve is represented by:

$$
\begin{equation*}
f_{\mathrm{c}}=\frac{f_{c c}^{\prime} \cdot \mathrm{k}_{f} \cdot\left(\frac{\varepsilon_{c}}{\varepsilon_{1} \cdot \mathrm{k}_{\varepsilon}}\right) \cdot r}{r-1+\left(\frac{\varepsilon_{c}}{\varepsilon_{1} \cdot \mathrm{k}_{\varepsilon}}\right)^{r}} \tag{1}
\end{equation*}
$$

Where:

$$
r=\frac{E_{c}}{E_{c}-E_{\mathrm{sec}}} \quad, \quad E_{\mathrm{sec}}=\frac{f_{c c^{\prime}} \cdot k_{f}}{\varepsilon_{1} \cdot k_{\varepsilon}} \quad, \quad E_{c}=4730 \sqrt{f_{c^{\prime}}} \quad, \quad \varepsilon_{1}=\varepsilon_{01}\left(1+5 k_{3} K\right)
$$

The descending part assumes a slope that changes with confinement reinforcement and as follows:-

$$
\begin{aligned}
& \varepsilon_{85}=260 k_{3} \cdot \rho_{c} \cdot \varepsilon_{1}\left[1+0.5 k_{2}\left(k_{4}-1\right)\right]+\varepsilon_{085} \\
& k_{1}=6.7\left(f_{l e}\right)^{-0.17} \quad, \quad k_{2}=0.15 \sqrt{\left(\frac{b_{c}}{S}\right)\left(\frac{b_{c}}{S L}\right)} \leq 1 \quad, \quad k_{3}=\frac{40}{f_{c^{\prime} o}} \leq 1 \\
& k_{4}=\frac{f_{L e}}{500}>1 \quad, \quad K=\frac{k_{1} \cdot f_{L e}}{f_{c^{\prime} o}} \\
& \varepsilon_{01}=0.0028-0.008 k_{3} \quad \varepsilon_{085}=\varepsilon_{01}+0.0018 k_{3}^{2} \\
& \rho_{c}=\frac{\sum_{i=1}^{n}\left(A_{s x}\right)_{i}+\sum_{j=1}^{m}\left(A_{s y}\right)_{j}}{S\left(b_{c x}+b_{c y}\right)} \\
& f_{L e}=k_{2} f_{L} \\
& k_{f}=1.48+0.16 \log _{10} \varepsilon^{\bullet}+0.0127\left(\log _{10} \varepsilon^{\bullet}\right)^{2} \\
& k_{\varepsilon}=1.08+0.112 \log _{10} \varepsilon^{\bullet}+0.0193\left(\log _{10} \varepsilon^{\bullet}\right)^{2}
\end{aligned}
$$



Fig.(1). Strain rate modified stress-strain relationship for concrete ${ }^{[6]}$

## Constitutive Steel Model

Several models were proposed to represent the stress-strain relationship of steel reinforcement by using many dynamic tests results ${ }^{[7]}$. The following constitutive model of steel has been empirically derived by Parvis Soroushian $(1987)^{[8]}$ from dynamic test results on structural steel, reinforcing bars and deformed wires for different wires and for different types of steel, Fig.(2).


Where:
$f_{y}^{\prime}=f_{y}\left[\left(-6.54 * 10^{-8} f_{y}+1.46\right)+\left(-1.334 * 10^{-7} f_{y}+0.0927\right) \log _{10} \varepsilon^{\prime}\right]$
$f_{u}{ }^{\prime}=f_{u}\left[\left(-1.118 * 10^{-7} f_{y}+1.15\right)+\left(-0.354 * 10^{-7} f_{y}+0.04969\right) \log _{10} \varepsilon^{\prime}\right]$
$\varepsilon_{h}{ }^{\prime}=\varepsilon_{h}\left[\left(-6.105 * 10^{-6} f_{y}+4.46\right)+\left(-1.22 * 10^{-6} f_{y}+0.693\right) \log _{10} \varepsilon^{\prime}\right]$
$\varepsilon_{u}{ }^{\prime}=\varepsilon_{u}\left[\left(-1.295 * 10^{-6} f_{y}+1.4\right)+\left(-2.596 * 10^{-7} f_{y}+0.0827\right) \log _{10} \varepsilon^{\prime}\right]$


Fig. (2). Comparison of Static and Dynamic Constitutive Model of Steel ${ }^{[8]}$
The comparison between the experimental $(f-\varepsilon)$ curve and Parvis Soroushian (1987) ${ }^{[8]}$ constitutive model for two different strain rates for steel specimens with yield strength of (235 MPa) as shown in Fig.(3).


Fig.(3). comparison of Parvis Soroushian (1987) ${ }^{[8]}$ constitutive model of steel with test results for $f_{y}=235 \mathrm{MPa}$

## MOMENT-CURVATURE RELATIONSHIP FOR CONCRETE SECTION

The response of reinforced concrete cross section to an applied bending moment and an axial force may be adequately described by the relation between moment and curvature referred to moment-curvature relationship. This relation depends on the material and geometrical properties of cross section as well as the level of the applied axial force.
This relationship is established using the following procedure:

1. The ultimate concrete compressive strain is first computed using Bing, Park and Tanka (2001) ${ }^{[2]}$ equation and as follows:

$$
\begin{equation*}
\varepsilon_{c u}=\varepsilon_{c o}\left[2+\left(122.5-0.92 f_{c o}\right) \sqrt{\frac{f_{l}}{f_{c o}}}\right] \tag{8}
\end{equation*}
$$

Where:
$f_{l}=$ lateral confining stress of transverse reinforcing steel
$f_{c o}=$ compressive strength of unconfined concrete
$\varepsilon_{c o}=$ strain at peak stress of unconfined concrete
The concrete spalling strain is limited by (0.004) as reported in Ref. ${ }^{[5]}$.
2. For a given concrete strain in the extreme compression fiber $\varepsilon_{c m}$ and neutral axis depth $k d$, the analysis is performed as follows:
a) The steel strains $\left(\varepsilon_{s l}, \varepsilon_{s 2} \ldots\right)$ can be determined from similar triangles of the strain diagram. For example, for bar $i$ at depth $d_{i}$ the steel strain is:

$$
\begin{equation*}
\varepsilon_{s i}=\varepsilon_{c m}\left(\frac{k d-d i}{k d}\right) \tag{9}
\end{equation*}
$$

The steel stresses $\left(f_{s 1}, f_{s 2} \ldots\right.$ ) corresponding to strains ( $\varepsilon_{s l}, \varepsilon_{s 2} \ldots$ ) may be found from the stress-strain curve for the steel using equations (3). Then the steel forces ( $S_{s l}, S_{s 2} \ldots$ ) may be found from the steel stresses and the areas of steel, Fig.(4). For example for bar $i$ the force equation is:

$$
\begin{equation*}
S_{i}=f_{s i} \cdot A_{s i} \tag{10}
\end{equation*}
$$



Fig.(4). theoretical moment curvature analysis (a) steel in tension and compression.
b) The concrete compressive force $C_{c}$ is made up of two parts, a confined part coming from the core concrete confined by the stirrups, and the unconfined part coming from the cover concrete. Each part is analyzed separately and both are added to make up the total concrete compressive force, Fig.(5).


Fig.(5). concrete section analysis.
3. The force equilibrium equation is:

$$
\begin{equation*}
C_{c}=\sum_{i=1}^{n} f_{s i} A_{s i} \tag{11}
\end{equation*}
$$

and the moment equilibrium equation:

$$
\begin{equation*}
M=C_{c}\left(\frac{h}{2}-X_{c}\right)+\sum_{i=1}^{n} f_{s i} A_{s i}\left(\frac{h}{2}-d_{i}\right) \tag{12}
\end{equation*}
$$

Where:
$X_{c}=$ the moment arm of concrete compressive force $\left(C_{c}\right)$.
The curvature is given by
$\phi=\frac{\varepsilon_{c m}}{k d}$
4. The method of establishing these relations is based on equilibrium of internal and external forces assuming a linear distribution of strain across the depth of section. Concrete spalling outside the ties has no contribution in internal force calculation at strains more than the maximum unconfined value of (0.004). The moment-curvature curve exhibits a discontinuity at first yield of tension steel and has been terminated when external fiber compressive concrete strain $\varepsilon_{c m}$ reaches the maximum compressive strain $\varepsilon_{c u}$, $\mathbf{F i g}$.(5).
Fig.(6) shows a comparison between experimental results and the present study results. It is obvious that there is a good agreement between the analytical model and the test results.


Fig.(6) Comparison between Experimental Results ${ }^{[3]}$ and the Present Study Results for Confined Beam Section

## Effects of Strain Rate on the Curvature Ductility

Any increase in the rate of loading usually increases both the compressive strength of concrete and the yield strength of steel. Hence it may be expected that the moment capacity of reinforced concrete beams increases with increasing in the loading rate.

The reinforced concrete beam shown in Fig.(7) is analyzed the results are presented in Figs.(8) to (12). In each Figure five curves of moment-curvature relationships are shown for four different strain rates of $0.0001 / \mathrm{sec}$ (a typical quasi-static value), $0.001 / \mathrm{sec}, 0.01 / \mathrm{sec}$ and $0.1 / \mathrm{sec}$ in addition to the static load condition for different parameters of ( $f_{y}, f_{y t}, f_{c}^{\prime}, S$ and steel plate thickness). The steel plates stiffening the top and the bottom face of the reinforced concrete section.


Fig.(7) Details of Beam

Table (1) summarizes the results of the curvature ductility for different parameters $\left(f_{y}, f_{y t}, f_{c}{ }^{\prime}\right.$ and $S$ ). The effects of the above parameters on $\mu_{\phi}$ for reinforced concrete beam sections are as follows:

1. $\mu_{\phi}$ is increased by about $10 \%$ for $f_{y}=414 \mathrm{MPa}$ and by about $30 \%$ for both $f_{y}=345$ and 276 MPa under the strain rate of $(0.1 / \mathrm{sec})$ as compared to the static loading, Fig.( 13-a).
2. For different yield strengths of the transverse reinforcement the curvature ductility factor under the strain rate of $(0.1 / \mathrm{sec})$ increased an average by about ( $14 \%$ ) as compared to the static loading, Fig.( 13-b).
3. For different concrete compressive strengths the average increase in curvature ductility under the strain rate of $(0.1 / \mathrm{sec})$ is about $(10 \%)$ as compared to the static loading, Fig. ( 13c).
4. For different values of spacing of stirrups the average increase in $\mu_{\phi}$ under strain rate of $0.1 / \mathrm{sec}$ is about $12 \%$ as compared to the static loading, Fig. ( 13-d).
5. for different $f_{y}, f_{c}^{\prime}, f_{y t}$ and S the average increase in moment capacity at strain rate of ( $0.1 / \mathrm{sec}$ ) as compared to the static rate is about $20 \%$, Figs.(8) to (11).

## Effects of Strengthening by Steel Plates:

For different strain rates the beam section of Fig.(7) has been strengthened by using steel plates of $1 \mathrm{~mm}, 3 \mathrm{~mm}$ and 5 mm thickness. The results are given in Table (2) the following can be concluded:

1. For different steel plate thickness the average increase in $\mu_{\rho}$ under strain rate of $0.1 / \mathrm{sec}$ is about $14 \%$ as compared to the static loading.
2. For a strain rate of $0.1 / \mathrm{sec}$ the strengthening of the beam by steel plates of $1 \mathrm{~mm}, 3 \mathrm{~mm}$ and 5 mm respectively decreases the curvature ductility by $8 \%, 9 \%$ and $10 \%$ respectively as compared to the unplated sections.
3. For the static strain rate the strengthening of the beam by steel plates of $1 \mathrm{~mm}, 3 \mathrm{~mm}$ and 5 mm respectively decreases the curvature ductility by $6 \%, 12 \%$ and $18 \%$ respectively as compared to the unplated sections.
4. For higher strain rates the increase in thickness of steel plates is become insignificant on the curvature ductility of the beam section, Fig.(13-e).
5. For different steel plate thickness the average increase in moment capacity at strain rate of $0.1 / \mathrm{sec}$ over the static rate is (19\%), Fig.(12).

Table (1) Curvature ductility $\mu_{\emptyset}$ for beams under different strain rates

| Strain-Rate <br> ( ह́) $1 / \mathrm{sec}$ | 0.1 | 0.01 | 0.001 | 0.0001 | $\begin{gathered} \text { Static } \\ 0.00001 \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $f_{y}($ MPa) | $f_{c}^{\prime}=28 \mathrm{MPa}, f_{y t}=414 \mathrm{MPa}, \mathrm{S}=100 \mathrm{~mm}$ |  |  |  |  |
| 276 | 45.28 | 43.50 | 40.08 | 37.16 | 34.20 |
| 345 | 30.23 | 30.39 | 29.05 | 25.62 | 22.58 |
| 414 | 18.08 | 17.53 | 17.02 | 16.95 | 16.28 |
| $\mathrm{f}_{\text {yt }}$ (MPa) | $f_{c}^{\prime}=28 \mathrm{MPa}, \mathrm{f}_{y}=414 \mathrm{MPa}, \mathrm{S}=100 \mathrm{~mm}$ |  |  |  |  |
| 276 | 15.58 | 15.05 | 14.17 | 13.86 | 13.26 |
| 345 | 17.01 | 16.67 | 16.17 | 15.98 | 14.89 |
| 414 | 18.08 | 17.53 | 17.02 | 16.95 | 16.28 |
| $f_{\text {c }}{ }^{\prime}$ (MPa) | $f_{y}=414 \mathrm{MPa}, f_{y t}=414 \mathrm{MPa}, \mathrm{S}=100 \mathrm{~mm}$ |  |  |  |  |
| 21 | 14.39 | 13.92 | 13.57 | 13.32 | 13.10 |
| 28 | 18.08 | 17.53 | 17.02 | 16.951 | 16.28 |
| 35 | 19.39 | 18.90 | 18.48 | 18.22 | 17.47 |
| $S(\mathrm{~mm})$ | $f_{c}{ }^{\prime}=28 \mathrm{MPa}, f_{y}=414 \mathrm{MPa}, f_{y t}=414 \mathrm{MPa}$ |  |  |  |  |
| 100 | 18.08 | 17.53 | 17.02 | 16.95 | 16.28 |
| 150 | 13.77 | 13.14 | 12.49 | 12.32 | 12.01 |
| 200 | 11.82 | 11.76 | 11.18 | 10.88 | 10.54 |
| 250 | 10.76 | 10.99 | 10.37 | 10.17 | 9.80 |

Table (2) Effect of Plate Thickness and Strain Rate on the Curvature Ductility $\mu_{\emptyset}$ for Beam Sections

| Strain-Rate <br> $(\mathbf{\varepsilon}) \mathbf{1 / s e c}$ | $\mathbf{0 . 1}$ | $\mathbf{0 . 0 1}$ | $\mathbf{0 . 0 0 1}$ | $\mathbf{0 . 0 0 0 1}$ | Static <br> $\mathbf{0 . 0 0 0 0 1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Plate <br> Thickness $(\mathbf{m m})$ | $\boldsymbol{f}_{\boldsymbol{c}}{ }^{\prime}=\mathbf{2 8} \mathbf{M P a}, \boldsymbol{f}_{\boldsymbol{y}}=\mathbf{4 1 4} \mathbf{M P a}, \boldsymbol{f}_{\boldsymbol{y t}}=\mathbf{4 1 4} \mathbf{M P a}, \boldsymbol{S}=100 \mathbf{m m}$ |  |  |  |  |
| $\mathbf{0}$ | 18.08 | 17.53 | 17.02 | 16.951 | 16.28 |
| $\mathbf{1}$ | 16.75 | 16.48 | 15.99 | 15.94 | 15.30 |
| $\mathbf{3}$ | 16.55 | 16.06 | 15.89 | 15.43 | 14.57 |
| $\mathbf{5}$ | 16.35 | 15.86 | 14.78 | 14.25 | 13.81 |



Fig (8) Effect of strain-rate on the moment curvature relationship for different yield strength of main reinforcement $f_{c}{ }^{\prime}=28 \mathrm{MPa}, f_{y t}=414 \mathrm{MPa}, S=100 \mathrm{~mm}$


Fig (9) Effect of strain-rate on the moment curvature relationship for different yield strength of transverse reinforcement $f_{c}{ }^{\prime}=28 \mathrm{MPa}, f_{y}=414 \mathrm{MPa}, S=100 \mathrm{~mm}$


Fig (10) Effect of strain-rate on the moment curvature relationship for different compressive strength of concrete $f_{v}=414 \mathrm{MPa}, f_{v t}=414 \mathrm{MPa}, S=100 \mathrm{~mm}$

| T. K. Al-Azzawi | Curvature Ductilityof Reinforced Concrete Beam |
| :--- | ---: |
| R. K. Al Azzawi | Sections Stiffened With Steel Plates |
| T. H. Ibrahim |  |



Fig (11) Effect of strain-rate on the moment curvature relationship for different spacing of transverse reinforcement $f_{c}{ }^{\prime}=28 \mathrm{MPa}, f_{y}=414 \mathrm{MPa}, f_{y t}=414 \mathrm{MPa}$


Fig (12) Effect of strain-rate on the moment curvature relationship for beams with and without steel plates $f_{c}^{\prime}=28 \mathrm{MPa}, f_{y}=414 \mathrm{MPa}, f_{y t}=414 \mathrm{MPa}, S=100 \mathrm{~mm}$


Fig(13). Effect of strain rate on curvature ductility for different:
(a) Effect of steel yield strength for main reinforcement $\left(f_{c}{ }^{\prime}=28 \mathrm{MPa}, f_{y t}=\mathbf{4 1 4} \mathbf{~ M P a}, S=100 \mathrm{~mm}\right)$
(b) Effect of steel yield strength for transverse reinforcement ( $f_{c}{ }^{\prime}=\mathbf{2 8} \mathrm{MPa}, f_{y}=\mathbf{4 1 4} \mathrm{MPa}, S=100 \mathrm{~mm}$ )
(c) Effect of concrete compressive strength ( $\left.f_{y}=414 \mathrm{MPa}, f_{y t}=414 \mathrm{MPa}, S=100 \mathrm{~mm}\right)$
(d) Effect of spacing of stirrups $\left(f_{c}{ }_{c}=\mathbf{2 8} \mathrm{MPa}, f_{y}=\mathbf{4 1 4} \mathrm{MPa}, f_{y t}=\mathbf{4 1 4} \mathrm{MPa}\right)$
(e) Effect of steel plate thickness ( $f_{c}{ }^{\prime}=28 \mathrm{MPa}, f_{y}=\mathbf{4 1 4} \mathrm{MPa}, f_{y t}=414 \mathrm{MPa}, S=100 \mathrm{~mm}$ )

| T. K. Al-Azzawi | Curvature Ductilityof Reinforced Concrete Beam |
| :--- | ---: |
| R. K. Al Azzawi | Sections Stiffened With Steel Plates |
| T. H. Ibrahim |  |

R. K. Al Azzawi

## CONCLUSIONS:

Based on the results obtained in the present study, the following conclusions can be drawn:

1. The curvature ductility factor increased by about ( $14 \%$ ) for a strain rate of $(0.1 / \mathrm{sec})$ as compared to the static loading for different yield strengths of the transverse reinforcement and different steel plate thickness
2. The curvature ductility factor increased on average by ( $20 \%$ ) under the strain rate of $(0.1 / \mathrm{sec})$ over the static strain rate for different yield strengths of the main reinforcement.
3. The moment capacity increased on average by ( $20 \%$ ) for the strain rate of $(0.1 / \mathrm{sec})$ as compared to the static load condition for different yield strengths of the main reinforcement, strengths of the transverse reinforcement, compressive strength of concrete, spacing of stirrups and steel plate thickness.
4. The curvature ductility under different strain rates for the sections strengthened by steel plates as compared to the unplated sections decreased for the beam sections by about ( $10 \%$ ).

## NOTATIONS:

$A_{s x}, A_{s y}=$ area of one leg of transverse reinforcement in x and y directions.
$b_{c x}, b_{c y}=$ core dimensions measured c/c of perimeter hoop in x and y directions.
$E_{c} \quad=$ modulus of elasticity for concrete.
$E_{s} \quad=$ modulus of elasticity for steel.
$E_{\text {sec }} \quad=$ secant modulus of elasticity for concrete.
$f_{\mathrm{c}}^{\prime} \quad=$ concrete cylinder strength (in MPa).
$f_{c c}{ }^{\prime} f_{c c^{\prime}}=$ confined \& unconfined concrete compressive strength in members (in MPa).
$f_{L} \quad=$ average confinement pressure (in MPa).
$f_{L e}{ }^{\prime}=$ equivalent uniform lateral pressure (in MPa).
$f_{u} \quad=$ static ultimate yield strength of steel (in MPa).
$f_{u}{ }^{\prime} \quad=$ dynamic ultimate yield strength of steel (in MPa).
$f_{y} \quad=$ steel yield strength (in MPa).
$f_{y}^{\prime} \quad=$ dynamic yield strength of steel (in MPa).
$f_{y t} \quad=y i e l d$ strength of transverse reinforcement (in MPa).
$m, n=$ number of tie legs in x and y directions.
$S \quad=$ spacing of transverse reinforcement.
$S_{L} \quad=$ spacing of longitudinal reinforcement laterally supported by corner of hoop or hook of cross tie.
$\dot{\varepsilon} \quad=$ strain rate $\geq 10^{-5}$
$\rho_{c} \quad=$ total transverse steel area in two orthogonal directions divided by corresponding concrete area.
$\varepsilon_{01}=$ strain corresponding to peak stress of unconfined concrete.
$\varepsilon_{085}=$ strain corresponding to $85 \%$ of peak stress of unconfined concrete on the descending branch.
$\varepsilon_{1} \quad=$ strain corresponding to peak stress of confined concrete.
$\varepsilon_{85}=$ strain corresponding to $85 \%$ of peak stress of confined concrete.
$\varepsilon_{c} \quad=$ concrete strain.
$\varepsilon_{h} \quad=$ static strain hardening initiation strains of steel.
$\varepsilon_{h}{ }^{\prime} \quad=$ dynamic strain hardening initiation strains of steel.
$\varepsilon_{u} \quad=$ static ultimate strains of steel.
$\varepsilon_{u}{ }^{\prime} \quad=$ dynamic ultimate strains of steel.

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# DEFLECTION OF STRAIGHT AND CAMBERED BEAMS MEASURED DURING FOURTEEN HOURS PER DAY 

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#### Abstract

Straight and camber beams in portal frames [Footings + Columns + Beams] were studied. Deflection for period of fourteen hours in a day was measured for ten days.

Peak value of deflection within a day is predicted for each one of the beams under a sustained load uniformly distributed.

It is suggested that the load test is to be performed during critical period, within a day, that gives peak deflection.




## KEY WORDS

: camber, deflection, load test, peak, straight.

## INTRODUCTION

Reinforced concrete has taken its place as one of the most important structural material due to its relatively high compressive strength, durability, adaptability to various forms and its relatively low cost. It, however, has the unfavorable characteristic of relatively low tensile strength.

Reinforced concrete buildings respond quite significantly to changes in loading and environment in addition to the natural laws which govern the behavior of the materials, leading to the inevitable deflection. To the engineer, these movements (deformations) should take an important considerations in ensuring that the structure is safe and will satisfactorily fulfil its purpose.

Arching is the oldest structural method for bridging too long spans. Arches are made of masonry, steel, timber and reinforced concrete.

Introducing some camber (shallow curvature) to flexural members (beams or slabs) may mobilize end restraint forces. Curved flexural members tend to straighten when a load is applied on them under the action of "angular deformation". This tends to increase the span of a curved member. To maintain the original span, a horizontal thrust reaction will be initiated by the action of the restraining supports. This axial restraint force acts in a similar manner as the axial pre-stressing force.

## LITERATURE REVIEW

Generally, all codes recommend the practice of providing an initial camber, to overcome excessive deflections due to vertical loads.

CEB-FIB Model Code ${ }^{[2]}$ states that in order to balance the deflections, fully or in part, and to prevent the unwanted effects, adequate cambers are introduced in the form-work during construction.
$\mathrm{ACI}{ }^{[1]}$ and Iraqi Building Code ${ }^{[3]}$ specify that the maximum permissible deflection may be exceeded if camber is provided so that the total deflection minus camber does not exceed the permissible limit.

An upward deflection is sometimes introduced to the member. This deflection is equal to the downward deflection caused by dead loads only, especially when the dead load represents the largest share of loads ${ }^{[4]}$.

## SCOPE OF RESEARCH

An attempt is made, in this research, to study the deflection of straight and camber beams in actual portal frames [Footings + Columns + Beams]. The deflection was measured during months July and September of the year 2003 every two hours in a day [readings start at 8:00 a.m. and finished at 10:00 p.m.] for ten days.

An attempt is made to search for the peak period, i.e. the period which the deflection takes its peak value (maximum value)within a day. It is believed that it is possible to make use of this peak period in actual buildings [as an example, reducing the load (live load) during this period depending on the type and performance of each building (commercial, industrial, residential, . . .)]. Also, it may be possible to make use of this peak period for load test, i.e. to perform load test on buildings during this peak period in order to give the decision of the load test taking into account the worst situation of environment daily changes.

An attempt is also made, to study the effect of camber beams (whether it is interior or not). To ensure the accuracy, all dial gages have been calibrated at the central Institution for Measuring and Quality Control.

## EXPERIMENTAL WORK

Three model portal frames were prepared [for general information of the portal frames, see Appendix (A)] as follows:

Single span frame (with straight beam) [Frame (A)], shown in Fig. (1).
Single span frame (with cambered beam) [Frame (B)], shown Fig. (2).
Triple span frame (with cambered beam) [Frame (C)], shown Fig. (3).
The upward camber is chosen to be $4.6 \%$ upward curvature (gives best results ${ }^{[5]}$ ). Dead load was applied on beams after frames were about more than $\mathbf{1 0 0}$ days age. The date of the dead load application is $\mathbf{1 2} / \mathbf{5} / \mathbf{2 0 0 3}$, and that of live load application is $\mathbf{2 0} / \mathbf{6} / \mathbf{2 0 0 3}$. Deflection readings for frames ( $\mathbf{A} \& \mathbf{C}$ ) were from $\mathbf{1 5} / 7 / 2003$ to 24/7/2003, and that for frames ( $\mathbf{A} \& \mathbf{B}$ ) were from $\mathbf{1 1 / 9 / 2 0 0 3}$ to $\mathbf{2 0 / 9 / 2 0 0 3}$. These periods were chosen to study the effect of Baghdad climate of hot weather (frames A \& C) and moderate weather (frames A \& B).

Structural analysis indicates that the total ultimate load is ( $\mathbf{5 . 3 8 3} \mathbf{~ k N} / \mathbf{m}$ ). According to load test requirements, $\mathbf{8 5 \%}$ of the total load should be considered as total test load, hence:

Total Test Load $=0.85(5.383)=4.576 \mathrm{kN} / \mathrm{m}$
Beam self weight $=0.072 \mathrm{kN} / \mathrm{m}$
Super imposed dead load $=\mathbf{2 . 4 6 1} \mathbf{~ k N} / \mathbf{m}$ (assumed, to use equal concrete block rows, each row contain equal number of concrete blocks)

Total dead load $=2.533 \mathrm{kN} / \mathrm{m}$
Hence test live load $=4.576-2.533=2.043 \mathrm{kN} / \mathrm{m}$
Dead and live loads were applied (experimentally) using concrete blocks and sags filled with gravel and hanged on steel pipes. The loads were applied at the same time for all frames.

Tables (1), (2), (3) and (4) give the measured deflection of the portal frames during fourteen hours of ten days of the research.

Fig. (1) shows the relationship between the average measured deflection and daily hours for frames ( $\mathbf{A} \& \mathbf{C}$ ), whereas Fig. (2) shows the same relationship for frames (A \& B). Fig. (3) shows the same relationship for frame (A) at both months (July and September).

To ensure that there is no settlement in the foundation, the soil is compacted, then a brick layer is placed under a thin concrete blinding layer on which experimental models were cast.

For theoretical verification of the deflection results obtained experimentally, the following formulas were applied ${ }^{[1,6]}$ :

$$
\begin{equation*}
\Delta_{2 i}=\frac{5 L^{2}}{48 E_{c} I_{e}}\left[M_{2}-\frac{1}{10}\left(M_{1}+M_{3}\right)\right] \tag{1}
\end{equation*}
$$

and

$$
\begin{align*}
& \Delta_{(c p+s h)}=\lambda \cdot\left(\Delta_{i}\right)_{s u s t}  \tag{2}\\
& \lambda=\frac{\xi}{1+50 \rho^{\prime}} \tag{3}
\end{align*}
$$

where
$\boldsymbol{E}_{c}$ is the modulus of elasticity.
$\boldsymbol{I}_{\boldsymbol{e}}$ is the effective moment of inertia.
$\boldsymbol{M}_{\boldsymbol{1}} \boldsymbol{\&} \boldsymbol{M}_{3}$ are the moments at the left and right ends respectively.
$\boldsymbol{M}_{2}$ is the moment at mid-span of the beam.
$\boldsymbol{\lambda} \boldsymbol{\xi} \boldsymbol{\xi}$ are the long term deflection multiplier and coefficient respectively.
$\left(\Delta_{i}\right)_{\text {sust }}$ is the immediate deflection due to sustained load.
$\boldsymbol{\Delta}_{(c p+s h)}$ is the long term deflection due to creep and shrinkage.
$\Delta_{2 i}$ is the immediate deflection.
Total (immediate plus long term) theoretical deflections are given at the bottom of Tables (1, 2, $3 \& 4$ ), which indicate that the experimental results are acceptable.

It can be seen from Tables (1), (2), (3) and (4) and Figs. (4), (5) and (6), the following remarks: straight beam will suffer from the reduction of its ability to withstand the external action (effect) done on it.
6- From Tables (1), (2), (3) and (4), it can be seen that the range of daily hours for peak values of deflection is as follows:

4:00 to 8:00 p.m.] for frame (A) in July and September.
[6:00 to 8:00 p.m.] for frame (B) in September.
[8:00 to 10:00 p.m.] for frame (C) in July.
7- It is possible to conclude that the cambered beam (Frames $\mathbf{B} \& \mathbf{C}$ ) is better than straight beam (Frame A).
8- It is possible to conclude that the camber beam will be better if it is interior beam (Frame C) compared to single span beam (Frame B).

## CONCLUSIONS

It is preferable to perform load test on straight members during the period [4:00 p.m. - 8:00 p.m.], and for cambered members during the period [6:00 p.m. - 10:00 p.m.] in order to give load test decision taking into account the worst case of daily deflection changes (peak value). It is preferable for a straight beam to be cambered one to improve the beam behavior.

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Table (1) Deflection around day for frame (A) (mm) [during July 2003].

| Day | Hour |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{8 : 0 0}$ | $\mathbf{1 0 : 0 0}$ | $\mathbf{1 2 : 0 0}$ | $\mathbf{2 : 0 0}$ | $\mathbf{4 : 0 0}$ | $\mathbf{6 : 0 0}$ | $\mathbf{8 : 0 0}$ | $\mathbf{1 0 : 0 0}$ |  |
| $\mathbf{1 5 / 7}$ | 3.291 | 3.311 | 3.313 | 3.331 | 3.375 | 3.376 | 3.380 | 3.378 |  |
| $\mathbf{1 6 / 7}$ | 3.286 | 3.295 | 3.313 | 3.331 | 3.376 | 3.376 | 3.376 | 3.358 |  |
| $\mathbf{1 7 / 7}$ | 3.287 | 3.304 | 3.322 | 3.347 | 3.394 | 3.392 | 3.395 | 3.395 |  |
| $\mathbf{1 8} / 7$ | 3.295 | 3.331 | 3.349 | 3.362 | 3.404 | 3.401 | 3.385 | 3.369 |  |
| $\mathbf{1 9 / 7}$ | 3.318 | 3.349 | 3.368 | 3.388 | 3.412 | 3.422 | 3.412 | 3.398 |  |
| $\mathbf{2 0 / 7}$ | 3.322 | 3.349 | 3.369 | 3.393 | 3.421 | 3.430 | 3.428 | 3.412 |  |
| $\mathbf{2 1 / 7}$ | 3.349 | 3.371 | 3.383 | 3.396 | 3.438 | 3.443 | 3.434 | 3.421 |  |
| $\mathbf{2 2 / 7}$ | 3.351 | 3.369 | 3.371 | 3.386 | 3.434 | 3.440 | 3.434 | 3.434 |  |
| $\mathbf{2 3 / 7}$ | 3.358 | 3.377 | 3.380 | 3.403 | 3.447 | 3.439 | 3.443 | 3.443 |  |
| $\mathbf{2 4 / 7}$ | 3.347 | 3.359 | 3.368 | 3.394 | 3.430 | 3.434 | 3.435 | 3.435 |  |
| Aver- <br> age | $\mathbf{3 . 3 2 0}$ | $\mathbf{3 . 3 4 2}$ | $\mathbf{3 . 3 5 4}$ | $\mathbf{3 . 3 7 3}$ | $\mathbf{3 . 4 1 3}$ | $\mathbf{3 . 4 1 5}$ | $\mathbf{3 . 4 1 2}$ | $\mathbf{3 . 4 0 4}$ |  |

Final average deflection $=3.379 \mathrm{~mm}$
Theoretical average deflection $=5.479 \mathbf{~ m m}$

Table (2) Deflection around day for frame (C) (mm) [during July 2003].

| Day | Hour |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{8 : 0 0}$ | $\mathbf{1 0 : 0 0}$ | $\mathbf{1 2 : 0 0}$ | $\mathbf{2 : 0 0}$ | $\mathbf{4 : 0 0}$ | $\mathbf{6 : 0 0}$ | $\mathbf{8 : 0 0}$ | $\mathbf{1 0 : 0 0}$ |  |
| $\mathbf{1 5} / \mathbf{7}$ | 2.111 | 2.099 | 2.091 | 2.095 | 2.101 | 2.132 | 2.137 | 2.137 |  |
| $\mathbf{1 6 / 7}$ | 2.108 | 2.100 | 2.095 | 2.090 | 2.110 | 2.130 | 2.146 | 2.145 |  |
| $\mathbf{1 7 / 7}$ | 2.110 | 2.095 | 2.090 | 2.100 | 2.115 | 2.150 | 2.158 | 2.157 |  |
| $\mathbf{1 8} / 7$ | 2.103 | 2.100 | 2.098 | 2.105 | 2.115 | 2.140 | 2.152 | 2.150 |  |
| $\mathbf{1 9 / 7}$ | 2.117 | 2.112 | 2.108 | 2.110 | 2.120 | 2.126 | 2.150 | 2.150 |  |
| $\mathbf{2 0 / 7}$ | 2.118 | 2.110 | 2.105 | 2.121 | 2.133 | 2.152 | 2.155 | 2.158 |  |
| $\mathbf{2 1 / 7}$ | 2.140 | 2.130 | 2.125 | 2.118 | 2.139 | 2.152 | 2.160 | 2.160 |  |
| $\mathbf{2 2 / 7}$ | 2.143 | 2.140 | 2.130 | 2.133 | 2.135 | 2.160 | 2.165 | 2.163 |  |
| $\mathbf{2 3 / 7}$ | 2.148 | 2.144 | 2.141 | 2.143 | 2.150 | 2.164 | 2.170 | 2.170 |  |
| $\mathbf{2 4 / 7}$ | 2.151 | 2.130 | 2.115 | 2.120 | 2.140 | 2.160 | 2.163 | 2.162 |  |
| Aver- <br> age | $\mathbf{2 . 1 2 5}$ | $\mathbf{2 . 1 1 6}$ | $\mathbf{2 . 1 1 0}$ | $\mathbf{2 . 1 1 4}$ | $\mathbf{2 . 1 2 6}$ | $\mathbf{2 . 1 4 7}$ |  | $\mathbf{2 . 1 5 6}$ |  |
| $\mathbf{2 . 1 5 5}$ |  |  |  |  |  |  |  |  |  |

$$
\text { Final average deflection }=2.131 \mathrm{~mm}
$$

Theoretical average deflection $=\mathbf{3 . 4 6 8} \mathbf{~ m m}$

Table (3) Deflection around day for frame (A) (mm) [during September 2003].

| Day | Hour |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{8 : 0 0}$ | $\mathbf{1 0 : 0 0}$ | $\mathbf{1 2 : 0 0}$ | $\mathbf{2 : 0 0}$ | $\mathbf{4 : 0 0}$ | $\mathbf{6 : 0 0}$ | $\mathbf{8 : 0 0}$ | $\mathbf{1 0 : 0 0}$ |  |
| $\mathbf{1 1 / 9}$ | 4.135 | 4.155 | 4.152 | 4.252 | 4.358 | 4.365 | 4.358 | 4.358 |  |
| $\mathbf{1 2 / 9}$ | 4.138 | 4.154 | 4.155 | 4.251 | 4.357 | 4.402 | 4.357 | 4.357 |  |
| $\mathbf{1 3 / 9}$ | 4.140 | 4.163 | 4.161 | 4.258 | 4.365 | 4.365 | 4.365 | 4.365 |  |
| $\mathbf{1 4 / 9}$ | 4.143 | 4.177 | 4.180 | 4.280 | 4.396 | 4.384 | 4.390 | 4.385 |  |
| $\mathbf{1 5 / 9}$ | 4.146 | 4.179 | 4.182 | 4.279 | 4.391 | 4.382 | 4.389 | 4.379 |  |
| $\mathbf{1 6 / 9}$ | 4.148 | 4.190 | 4.189 | 4.286 | 4.398 | 4.387 | 4.393 | 4.392 |  |
| $\mathbf{1 7 / 9}$ | 4.151 | 4.199 | 4.204 | 4.299 | 4.413 | 4.397 | 4.410 | 4.407 |  |
| $\mathbf{1 8 / 9}$ | 4.155 | 4.210 | 4.206 | 4.306 | 4.410 | 4.396 | 4.410 | 4.407 |  |
| $\mathbf{1 9 / 9}$ | 4.158 | 4.217 | 4.221 | 4.318 | 4.427 | 4.406 | 4.423 | 4.421 |  |
| $\mathbf{2 0 / 9}$ | 4.161 | 4.227 | 4.232 | 4.328 | 4.437 | 4.414 | 437 | 4.433 |  |
| Aver- <br> age | $\mathbf{4 . 1 4 8}$ | $\mathbf{4 . 1 8 7}$ | $\mathbf{4 . 1 8 8}$ | $\mathbf{4 . 2 8 6}$ | $\mathbf{4 . 3 9 5}$ | $\mathbf{4 . 3 9 0}$ | $\mathbf{4 . 3 9 3}$ | $\mathbf{4 . 3 9 0}$ |  |

Final average deflection $=4.297 \mathrm{~mm}$
Theoretical average deflection $=\mathbf{6 . 3 2 4} \mathbf{~ m m}$

Table (4) Deflection around day for frame (B) (mm) [during September 2003].

| Day | Hour |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 8:00 | 10:00 | 12:00 | 2:00 | 4:00 | 6:00 | 8:00 | 10:00 |
| 11/9 | 3.606 | 3.585 | 3.604 | 3.638 | 3.726 | 3.766 | 3.760 | 3.663 |
| 12/9 | 3.595 | 3.579 | 3.598 | 3.634 | 3.721 | 3.762 | 3.705 | 3.636 |
| 13/9 | 3.600 | 3.573 | 3.585 | 3.602 | 3.623 | 3.764 | 3.634 | 3.609 |
| 14/9 | 3.600 | 3.529 | 3.560 | 3.595 | 3.616 | 3.767 | 3.641 | 3.624 |
| 15/9 | 3.605 | 3.560 | 3.594 | 3.622 | 3.673 | 3.770 | 3.723 | 3.662 |
| 16/9 | 3.610 | 3.564 | 3.583 | 3.609 | 3.684 | 3.768 | 3.673 | 3.624 |
| 17/9 | 3.611 | 3.534 | 3.561 | 3.584 | 3.637 | 3.762 | 3.672 | 3.623 |
| 18/9 | 3.611 | 3.535 | 3.553 | 3.573 | 3.586 | 3.760 | 3.602 | 3.573 |
| 19/9 | 3.598 | 3.515 | 3.547 | 3.558 | 3.579 | 3.765 | 3.596 | 3.579 |
| 20/9 | 3.599 | 3.496 | 3.536 | 3.562 | 3.578 | 3.780 | 3.597 | 3.585 |
| Average | 3.604 | 3.547 | 3.572 | 3.598 | 3.642 | 3.766 | 3.660 | 3.618 |
| Final average deflection $=3.626 \mathrm{~mm}$ |  |  |  |  |  |  |  |  |
| Theoretical average deflection $\mathbf{= 5 . 6 0 2} \mathbf{~ m m}$ |  |  |  |  |  |  |  |  |



Fig. (4) Deflection - Hour relationship for frames (A \& C).


Fig. (5) Deflection - Hour relationship for frames (A \& B).


Fig. (5) Deflection - Hour relationship for frames (A \& B).


# THEORETICAL SIMULATION OF STRESS-STRAIN RELATIONS FOR SOME IRAQICLAYS USING THE ENDOCHRONIC MODEL 

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#### Abstract

A constitutive law can be defined as a mathematical functional relation between physical quantities such as stress and strain and may take other factors like time, temperature and additional material properties into account.

In this paper, the endochronic model is used to predict the stress-strain relations of two Iraqi clays. This model is a viscoplastic one but without introducing a yield surface. It encompasses material behaviour such that the current stress state is a function of strain history through a time scale called "intrinsic time" which is not the absolute time but a material property.

The simulation showed that the model overestimates the strains for all cases studied. This may be attributed to the material parameters which require a parametric study to determine their actual values for Iraqi clays.


## KEYWORDS

Clay, End chronic Model, Stress, Strain, Model Parameters
الخلاصة
يمكن تعريف فو انين العلاقات النكوينية بأنها دو ال رياضية نربط بين كميات فيزياوية مثل الإجهاد و الانفعال
و قد تأخذ عو امل عديدة أخرى متل الزمن و الحرارة و خصـائص أخرى للمادة بنظر الاعتبار .
أستعمل في هذا البحث نموذج الزمن الضمني للتتبؤ بعلاقات الإجهاد-الانفعال لتربنين طينيتين عــر اقيتين.
إن هذا النموذج هو من النوع الللان - اللز ج و لكنه لا يود خل سطح خضوع. و يعبر عــن ســلوك المـــادة
بحيث أن حالة الإجهاد الحالية تكون دالة لتاريخ الانفعال من خلا ملا مقياس زمني يدعى "الزمن الضمني" الذي
يختلف عن الزمن المطلق من حيث أنه خاصية من خو اص المادة. لقد بين التمثيل أن هذا النموذج يعطي قيما
عالية للانفعال لكل الحالات التي تمت دراستها. و يعزى هذا إلى معاملات المادة التي يتضمنها النمــوذج و
التي تحتاج إلى در اسة معاملات لتحديد فيمها الحقيقبة بالنسبة للترب الطينية العر اقية.

## INTRODUCTION

Endochronic theory was first introduced by Valanis in 1971. He coined this Greek name "Endochronic" that consists of two roots, endos (meaning inner) and chronos (meaning time). This theory encompasses material behaviour such that the current stress state is a function of the strain
history through a time scale called " intrinsic time" which is not the absolute time measured by a clock as in viscoplasticity but a material property. Hence, the endochronic theory is a "viscoplastic" one but without introducing a yield surface. Therefore, all the complexities and difficulties that develop in introducing a suitable yield criteria are avoided, (Valanis,1971).

Bazant in 1974 and later with his coworkers extended Valanis theory to predict the behaviour of different engineering materials such as concrete, and soils.

## GENERALIZED CONSTITUTIVE RELATIONS:

To generalize the uniaxial concept of the endochronic theory into three dimensions, first, the definition of the intrinsic time increment, dz , which is used in stead of real time increment, dt, is introduced. The intrinsic time for time-dependent behaviour is function of strain increments, $\mathrm{d} \epsilon_{i j}$ and time, dt . The dependence of dz upon $\mathrm{d} \epsilon_{i j}$ is assumed to be gradual to exclude ideal plastic reponse. The function of dz will be continuous, smooth, and monotonically increasing. Thus, function (dz) ${ }^{\mathrm{S}}$ with an appropriate exponent " s ", can be expanded in a tensorial power series in $\mathrm{d} \epsilon_{i j}$ and dt, i.e., (Bazant and Bhat,1976):

$$
\begin{align*}
& (d z)^{s}=p+p_{i j} d \epsilon+p_{4} d t+p_{i j k l} d \epsilon_{i j} d \epsilon_{k l}+p_{i j 4} d \epsilon_{i j} d t+p_{4} d t+  \tag{1}\\
& p_{i j k l m n} d \epsilon_{i j} d \epsilon_{k l} d \epsilon_{m n}+\ldots . . .
\end{align*}
$$

where:
$\mathrm{P}=$ coefficient matrices, the subscripts refer to the components in the Cartesian coordinates $\mathrm{X}_{\mathrm{i}}$, $\mathrm{i}=1,2,3$, and number (4) refers to the time axis.

Since, dz must vanish as $\mathrm{d} \epsilon_{i j} \rightarrow 0$ and $d t \rightarrow 0$, thus $\mathrm{P}=0$. Setting $\mathrm{s}=1$, and neglecting all quadratic terms, then $\mathrm{dz}=\mathrm{P}_{4}$. dt which is of no interest, thus $\mathrm{P}_{4}=0$. Setting $\mathrm{s}=2$, and satisfying the conditions of isotropy, the quadratic form of Equation (1) can be written in terms of the first two invariants of $\mathrm{d} \epsilon_{i j}$, as follows, (Bazant and Bhat,1976):
$(d z)^{2}=P_{o} J_{2}+\left(P_{1} I_{1}+P_{2} d t\right)^{2}+P_{3}(d t)^{2}$
where:
$\mathrm{P}_{\mathrm{o}}, \mathrm{P}_{1}, \mathrm{P}_{2}, \mathrm{P}_{3}=$ non-negative coefficients.
$\mathrm{J}_{2}=$ second deviatoric strain increment invariant, and
$\mathrm{I}_{1}=$ first strain increment invariant.
Then, dz must vainish for both instantaneous time, $\mathrm{dt}=0$, and pure volumetric deformation, $\mathrm{J}_{2}=0$, hence $\mathrm{P}_{1}=0$. Thus, the remaining terms in Equation (2) can be rewritten in the following form:

$$
\begin{equation*}
(d z)^{2}=\left(\frac{d \xi}{Z_{1}}\right)^{2}+\left(\frac{d t}{\tau_{1}}\right)^{2} \tag{3}
\end{equation*}
$$

where:
$d \xi=f_{1}(\sigma, \epsilon) \cdot d \zeta$
$d \zeta=\sqrt{J_{2}}=\sqrt{\frac{1}{2} d e_{i j} \cdot d e_{i j}}$
$\mathrm{de}_{\mathrm{ij}}=$ deviatoric strain increment tensor
$=d \epsilon_{i j}-\frac{1}{3} \delta_{i j} \cdot d \in$
$\delta_{i j}=$ Kronecker delta.
$d \in=$ Volumetric strain increment $=d \epsilon_{k k}$
$z_{1} \tau_{1}=$ Constants.
$d \xi$ is scalar called "damage measure" that depends on strain increments and stresses to predict hardening and softening. $d \zeta$ is called "deformation measure" that depends on strain increments only. From Equations (3) and (4), $d \zeta$ and dz represent geometrically the length of path traced by material states in a six-dimensional strain space for $d \zeta$, or in a strain-time space for dz., (Ansal et al., 1979).

Secondly, generalizing of equations to three dimensions using dz instead of dt, and splitting the strain components into deviatoric and volumetric components to satisfy isotropy conditions, the following differential constitutive equations are deduced:

$$
\begin{align*}
& d e_{i j}=\frac{d S_{i j}}{2 G}+\frac{S_{i j}}{2 G} \cdot d z  \tag{5.a}\\
& d \in=\frac{d \sigma_{m}}{3 k}+\frac{\sigma_{m} \cdot d t}{3 k \tau_{1}}+d \lambda+d \epsilon^{o} \tag{5.b}
\end{align*}
$$

where:

$$
\begin{aligned}
& d e_{i j}=d \in_{i j}-\frac{1}{3} \delta_{i j} \cdot d \in \\
& d \in=d \in_{11}+d \epsilon_{22}+d \in_{33} \\
& d \lambda=\text { inelastic dilatancy, } \\
& \mathrm{S}_{\mathrm{ij}}=\text { deviatoric stress tensor, } \\
& \quad=\sigma_{i j}-\delta_{i j} \cdot \sigma_{m} \\
& \sigma_{m}=\text { mean stress }=\frac{1}{3} \sigma_{k k}
\end{aligned}
$$

$\mathrm{G}, \mathrm{K}=$ shear and bulk elastic moduli, and
$d \epsilon^{o}=$ stress-independent inelastic strains (e.g. thermal strains).
Both of the first terms of Equations (5.a) and (5.b) represent the elastic strain increments, while the remaining terms represent the inelastic strain increments. For instance, the term $\left(\sigma_{m} \cdot d t / 3 K \tau_{1}\right)$ represents the time-dependent inelastic volumetric strain, i. e. creep, while $d \lambda$ represents the time-independent volumetric strain.

To develop a quasi-linear elastic incremental constitutive law for simplicity, the plastic stress increment tensor $d \sigma_{i j}^{p}$ can be obtained from Equations (5) by multiplying Equation (5.a) by 2G, and Equation (5.b) by 3 K , hence:

$$
\begin{align*}
d \sigma_{i j}^{p} & =2 G \cdot d e_{i j}^{p}+\delta_{i j}\left(3 K \cdot d \in^{p}\right) \\
& =S_{i j} d Z+\delta_{j j}\left(\sigma_{m} d t \tau+3 K d \lambda+3 K d \epsilon^{g}\right) \tag{6}
\end{align*}
$$

The stress increments $d \sigma_{i j}$ are related to the elastic strain increments $d \epsilon_{i j}^{e}$ by the following equations:

$$
\begin{equation*}
d \sigma_{i j}=2 G \cdot d e_{i j}^{e}+\delta_{i j}\left(3 K \cdot d \epsilon^{e}\right) \tag{7}
\end{equation*}
$$

Hence, the summation of Equations (7) and (8) yields:
$d \sigma_{i j}+d \sigma_{i j}^{p}=D_{i j k l} \cdot d \epsilon_{k l}$
where:
$D_{i j k l}=$ elastic coefficient matrix

## THE NUMERICAL PROCEDURE:

The basic constitutive law, Equation (5), is of a differential form, and the variables that govern inelastic deformations are (dz) and ( $d \lambda$ ). Bazant and Bhat (1976) used the step-by-step integration or step-iterative algorithm in which for each loading step, a number of iterations are performed till satisfaction of equilibrium of stresses and strains occurs. This is assured when the change in values of ( dz ) and ( $d \lambda$ ) for the same loading step becomes very small.

In this algorithm, the values of $(\mathrm{dz})$ and $(d \lambda)$ computed from the previous loading step provide an initial estimate for the next loading step.

## Endochronic Hardening Functions and Parameters:

The function $\mathrm{f}_{1}$ in Equation (4) that accounts for hardening or softening, should decrease as the inelastic strains accumulate, because $d \xi$ is adopted as a measure of the accumulated inelastic strain, hence:
$d \xi=\frac{d \eta}{f(\eta)} \quad ; \quad d \eta=F(\sigma, \epsilon) \cdot d \zeta$
where:
$f(\eta)=$ Strain-hardening function.
$F(\sigma, \in)=$ Strain-softening function.

Thus, the function $f(\eta)$ has a significant effect on the non-linearity of the stress-strain relations, while the function $F(\sigma, \in)$ allows for a gradual decrease of these relations on approach to peak stress. Both functions depend mainly on material type.

## Hardening Functions and Dilatancy for Normally Consolidated Clays:

The function F in Equation (9) is determined semi-empirically from experimental data. The function F is governed by the effective confining stress $\boldsymbol{I}_{1}^{\boldsymbol{\sigma}}$, the volume change, $\boldsymbol{I}_{1}^{\boldsymbol{\varepsilon}}$, and the second deviatoric strain invariant, $\boldsymbol{J}_{2}^{\boldsymbol{\varepsilon}}$. Bazant et al. (1979) introduced the following formulation for function F :

$$
\begin{equation*}
F(\sigma, \epsilon)=a+\frac{\left|1-a_{1} 1_{1}^{E}\right| /\left(1+a_{3} J_{2}^{\ominus}\right)}{0.01+a_{2}\left(I_{1}^{\sigma} / P a\right)} \tag{10}
\end{equation*}
$$

where: a 's $=$ material constants.

$$
\mathrm{Pa}=\text { atmospheric pressure }=101.3 \mathrm{kN} / \mathrm{m}^{2}
$$

The division of $\boldsymbol{I}_{1}^{\boldsymbol{\sigma}}$ in Equation (10) by Pa is to make the relation dimensionless. Constant "a" must be positive to ensure irreversible strain increment for the critical case of no hardening or softening, (Bazant et al., 1979).

The function $f(\eta)$ represents the limiting critical case of no hardening or softening. Thus, for large values of $\eta$, this function, $f(\eta)$, must converge to one. The function $f(\eta)$ takes the following form:

$$
\begin{equation*}
f(\eta)=1+\frac{\beta_{1}}{1+\beta_{2} \eta} \tag{11}
\end{equation*}
$$

where: $\beta_{1}$ and $\beta_{2}=$ constants.
The dilatancy or densification function $\mathrm{d} \lambda$ of clays depends on shear and volumetric stresses and strains. Hence, the function $\mathrm{d} \lambda$ depends on $\boldsymbol{J}_{2}^{\boldsymbol{\varepsilon}}, \boldsymbol{I}_{1}^{\boldsymbol{\sigma}}$ and $\boldsymbol{I}_{1}^{\boldsymbol{\varepsilon}}$. Moreover, $\mathrm{d} \lambda$ depends on $\lambda$ itself because the volumetric strain increment should decrease monotonically till zero as a limit in the case of failure. Hence $\mathrm{d} \lambda$ is equal to (Bazant et al., 1979):

$$
\begin{equation*}
d \lambda=\frac{C_{o}\left|1+C_{1} I_{1}\right| d \zeta}{\left(1+C_{2} I_{1}^{\sigma} / P a\right)\left(1+C_{3} J_{2}^{\epsilon}\right)\left(1+C_{4} \lambda\right)} \tag{12}
\end{equation*}
$$

where: $c_{0}, c_{1}, c_{2}, c_{3}, c_{4}=$ material constants.
$\mathrm{d} \lambda$ is determined empirically from tests and it depends on the clay type, stress path and stress history.

The tensile strengths of soils are very small and hence neglected.
The elastic moduli G and K of the soil element change during loading, and thus the accumulated densification-dilatancy measure $\lambda$ and the effective normal stress also change. Thus, the effect of void ratio is:

$$
\begin{equation*}
\frac{d e}{e_{o}}=\frac{\varepsilon_{v}\left(1+e_{o}\right)}{e_{o}}=\frac{3\left(1+e_{o}\right) \lambda}{e_{o}}=\frac{3 \lambda}{n} \tag{13}
\end{equation*}
$$

where: $\mathrm{e}_{\mathrm{o}}=$ initial void ratio
$\varepsilon_{\mathrm{v}}=$ volumetric strain $=\varepsilon_{\mathrm{kk}}$
$\mathrm{n}=$ porosity.
while the effect of normal stress is the ratio $\left(\boldsymbol{I}_{1}^{\boldsymbol{\sigma}}-\boldsymbol{I}_{1}^{\boldsymbol{\sigma}_{o}}\right) / \boldsymbol{I}_{1}^{\boldsymbol{\sigma}_{o}}$, where $\boldsymbol{I}_{1}^{\boldsymbol{\sigma}_{o}}$ is the initial first stress invariant. Hence, the elastic moduli will be equal to:

$$
\begin{equation*}
G=G_{o}\left(1+b_{1} \frac{I_{1}^{\sigma}-I_{1}^{\sigma_{o}}}{I_{1}^{\sigma_{o}}}+b_{2} \frac{3 \lambda}{n}\right) \tag{14}
\end{equation*}
$$

where: $b_{1}$ and $b_{2}=$ constants,

$$
\begin{equation*}
\text { and } K=\frac{2}{3} G(1+v) /(1-2 v) \tag{15}
\end{equation*}
$$

## MODEL PARAMETERS OF CLAYS

All material parameters in the previous equations are based on best fit of experimental results.
Constant "a" in Equation (10) affects the value of the peak stress. Constant $a_{3}$ which is called "distortion coefficient" is determined by the following correlation proposed by Ansal et al. (1979). Based on general pattern of results:

$$
\begin{equation*}
a_{3}=153.8\left(e_{o} \mathrm{~Pa} / \mathrm{Po}\right)+34.62 \tag{16}
\end{equation*}
$$

where:
$\mathrm{Po}=$ consolidation pressure .
Similarly, the plasticity coefficient $\mathrm{Z}_{1}$ in Equation (3) that accounts for rigidity and deformibility of clays, is determined from the following correlation:

$$
\begin{equation*}
Z_{1}=0.00294\left(\boldsymbol{e}_{o} \boldsymbol{P}_{o} / \boldsymbol{P}_{a}\right)^{2}-0.0177\left(\boldsymbol{e}_{o} \boldsymbol{P}_{o} / \boldsymbol{P}_{a}\right)+0.0396 \tag{17}
\end{equation*}
$$

Ansal et al. (1979) determined an approximate correlation for densification coefficient $\mathrm{C}_{0}$ in Equation (12), softening coefficient $\beta_{2}$ in Equation (11), and the elastic modulus E, as shown in Figure (1). This correlation depends on the consolidation pressure $\mathrm{P}_{\mathrm{o}}$, and the liquidity index of the clay $\mathrm{I}_{\mathrm{L}}$, where (Mitchel, 1993):

$$
\begin{equation*}
I_{L}=\frac{w_{\text {nat }}-w_{p}}{I_{P}} \tag{18}
\end{equation*}
$$

where:
$\mathrm{w}_{\mathrm{ant}}=$ natural water content.
$\mathrm{w}_{\mathrm{p}}=$ plastic limit
$\mathrm{I}_{\mathrm{p}}=$ plasticity index $=\mathrm{w}_{\mathrm{L}}-\mathrm{w}_{\mathrm{P}}$
$\mathrm{w}_{\mathrm{L}}=$ liquid limit.
Choice of appropriate ratio of the liquidity index to the consolidation stress is tempered by judgement in the absence of test results.

All other constants are determined experimentally. The values of the parameters as proposed by Bazant et al. (1979) are shown in Table (1):

Table (1) - Material parameters of endonchronic model for normally consolidated clays.

|  | Value |
| :---: | :---: |
| $\mathrm{a}_{\mathrm{o}}$ | 4 |
| $\mathrm{a}_{1}$ | 500 |
| $\mathrm{a}_{2}$ | 0.75 |
| $\beta_{1}$ | 5 n (n = porosity) |
| $\mathrm{C}_{1}$ | 2500 |
| $\mathrm{C}_{2}$ | 0.25 |
| $\mathrm{C}_{3}$ | 1000 |
| $\mathrm{C}_{4}$ | 9000 |
| $\mathrm{~b}_{1}$ | 0.1 |
| $\mathrm{~b}_{2}$ | 0.1 |

## Computer Program

The computer program Endoch, coded in Fortran laguage, was written by the authors. The algorithm used in the endochronoc model incorporates an iterative procedure. The program computes stresses, strains, all functions like $F, f(\eta)$, and variables like $\lambda$, $\eta$, at mid-step loading. Iterations are then performed till the tolerance of the values of dz and $\mathrm{d} \lambda$ becomes less than $0.05 \%$. The values of strain increments, $\mathrm{d} \varepsilon$, intrinsic time, dz , and inelastic dilatancy, $\mathrm{d} \lambda$, or the previous step are taken as an estimate for the current step.

## APPLICATIONS:

This model have been applied for simulating stress-strain relationships of two Iraqi soils:
i) First application Al- Mufty (1990) carried out a series of tests on al-Fao soft clay. Block samples were obtained from an area close to the river Shatt-Al-Arab.
The top layer of Fao soil was found to be stiff to very stiff brownish gray silty clay with a desiccated crust. This layer is followed by a soft to very soft gray silty clay.
According to the unified classification system, the soil from both layers may be classified as CLCH, inorganic clays of medium to high plasticity. According to, AASHTO M145-73, the soil is classified as A-7-6 (16).

(a)

b) Softening coerticient, $p_{2}$.

(c)
c) Elastic modulus, E.

The average properties of the soil at sampling depths 1.25 m and 3 m respectively are listed in Table (2).

Table (2). - Average properties of the soft clay from Al-Fao, (from Al-Mufty, 1990).

| Property | 1.25 m depth | 3 m depth |
| :--- | :---: | :---: |
| Total unit weight $\gamma_{\mathrm{t}}, \mathrm{kN} / \mathrm{m}^{3}$ | 17.9 | 17.7 |
| Water content $\mathrm{w} \%$ | 30 | 45 |
| Liquid limit $\mathrm{w}_{\mathrm{L}} \%$ | 54 | 50 |
| plasticity index Ip \% | 27 | 24 |
| Liquidity index $\mathrm{I}_{\mathrm{L}}$ | 0.11 | 0.79 |
| Specific gravity G | 2.7 | 2.72 |
| Sand size fraction \% | 9 | 12 |
| Silt size fraction \% | 58 | 60 |
| Clay size fraction \% | 33 | 28 |
| Activity A | 0.82 | 0.86 |

Among the tests carried out by Al-Mufty (1990) unconsolidated undrained triaxial compression tests on samples compacted by the standard compaction test to the maximum dry density and optimum moisture content. These results are compared with those predicted by the endochronic model in Figures (2) to Figure (6).

Fig (2) and (3) represent the samples that are taken from the top layer, and the figures from (4) to (6) represent the samples that are taken from the layer below the top layer.


Fig.(2). - A comparison between the stress-strain relationships predicted by the endochronic model with laboratory tests of Al - Mufty (1990), $\sigma_{3}=300 \mathrm{kPa}$.


Fig.(3). - A comparison between the stress-strain relationships predicted by the endochronic model with laboratory tests of Al - Mufty (1990), $\sigma_{3}=300 \mathrm{kPa}$.


Fig.(4). - A comparison between the stress-strain relationships predicted by the endochronic model with laboratory tests of $\mathrm{Al}-\mathrm{Mufty}(1990), \sigma_{3}=100 \mathrm{kPa}$.



Fig. (5). - A comparison between the stress-strain relationships predicted by the endochronic model with laboratory tests of Al - Mufty (1990), $\sigma_{3}=200 \mathrm{kPa}$.

Fig (6). with laboratory tests of Al - Mufty (1990), $\sigma_{3}=300 \mathrm{kPa}$.
It can be observed in these figures that the model overestimates the strains for all the cases studied under high stress increments.
In addition, there is no definite yield point can be obtained. Thus it is approximately suitable for normally consolidated clays where ductile behaviour of the stress-strain is expected.

## ii) Second application

Al- Saady (1989) carried out laboratory tests on an A-6 soil during construction of a road embankment. A representative area located at Al - Zafarania (south of Baghdad), was chosen for the research. The site covers an area of soil composed of silty clay with varying thickness. This stratum behaves as normally or slightly overconsolidated soil, have an upper desiccated crust 0.5 0.75 m thick.

The distribution of the particle sizes indicated:
Clay fraction $=45 \%$, silt fraction $=37 \%$, sand fraction $=18 \%$.
It is classed as "CL" in a Casagramde classification chart.
Among the tests carried out by Al- Saady (1989) consolidated undrained triaxial test which was designated as series D as shown in Table (3).
In addition, unconsolidated undrained triaxial test which was designatd as series G as shown in Table (4).

Consolidated undrained triaxial test results are compared with those predicted by the endochronic model in Figures (7) to (12) which show a comparison between the stress-strain relationships predicted by the endochronic model with laboratory tests of Al-Saady, (series, D).
Consolidated drained triaxial test results are compared with those predicted by the endochronic model in Figures (13) to (18). Figures (19) to (24) show a comparison between the volumetric strain-axial strain relationships predicted by the endochronic model with laboratory tests of Al-Saady, (series, G).

Table(3). - The results of series (D), (from Al-Saady, 1989).

| Test No. | $\sigma_{c}^{\prime} \mathrm{kN} / \mathrm{m}^{2}$ | $\mathrm{e}_{\mathrm{o}}$ | $\mathrm{w}_{\mathrm{c}} \%$ | $\left(\sigma_{1}-\sigma_{3}\right)_{f} \mathrm{kN} / \mathrm{m}^{2}$ | $\left(\sigma_{1} / \sigma_{3}\right)_{f} \mathrm{kN} / \mathrm{m}^{2}$ | $\Delta u_{f} \mathrm{kN} / \mathrm{m}^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 79 | 0.76 | 26.0 | 123.24 | 3.50 | 30.81 |
| 2 | 100 | 0.70 | 24.3 | 123.00 | 3.55 | 52.22 |
| 3 | 150 | 0.74 | 25.6 | 189.21 | 3.30 | 72.45 |
| 4 | 200 | 0.69 | 24.6 | 219.60 | 3.25 | 104.45 |
| 5 | 300 | 0.75 | 25.4 | 279.00 | 3.25 | 176.68 |
| 6 | 376 | 0.73 | 26.0 | 348.01 | 3.30 | 224.07 |



Fig.(7). - A comparison between the stress-strain relationship predicted by the endochronic model with laboratory tests of Al-Saady, Test 1, Series D.

Fig. (8) - A comparison between the stress-strain relationship predicted by the endochronic model with laboratory tests of Al - Saady, Test 2, Series D.


Fig. (9) - A comparison between the stress-strain relationship predicted by the endochronic model with laboratory tests of Al - Saady, Test 3, Series D.


Fig. (10) - A comparison between the stress-strain relationship predicted by the endochronic model with laboratory tests of Al-Saady, Test 4, Series D.


Fig. (11) A comparison between the stress-strain relationship predicted by the endochronic model with laboratory tests of A1 - Saady, Test 5, Series D.


Fig. (12). A comparison between the stress-strain relationship predicted by the endochronic model With laboratory tests of Al-Saady, Test 6, Series D.

Table (4). - The results of series (G), (from Al-Saady, 1989).

| Test No. | $\sigma_{c}^{\prime} \mathrm{kN} / \mathrm{m}^{2}$ | $\mathrm{e}_{\mathrm{o}}$ | $\mathrm{w}_{\mathrm{c}} \%$ | $\left(\sigma_{1}-\sigma_{3}\right)_{f} \mathrm{kN} / \mathrm{m}^{2}$ | $\left(\Delta V / V_{o}\right)_{f} \mathrm{kN} / \mathrm{m}^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 79 | 0.66 | 23.5 | 198.87 | 2.300 |
| 2 | 100 | 0.69 | 24.7 | 281.18 | 2.283 |
| 3 | 150 | 0.75 | 26.0 | 348.03 | 3.026 |
| 4 | 200 | 0.75 | 27.0 | 405.03 | 3.016 |
| 5 | 300 | 0.69 | 25.2 | 752.55 | 3.590 |
| 6 | 376 | 0.72 | 25.0 | 913.52 | 3.710 |



Fig. (13). - A comparison between the stress-strain relationship predicted by the endochronic model with laboratory tests of Al - Saady, Test1, series G.


Fig. (14). - A comparison between the stress-strain relationship predicted by the endochronic model with laboratory tests of Al - Saady, Test2, series G.


Fig.(15) - A comparison between the stress-strain relationship predicted by the endochronic model with laboratory tests of Al - Saady, Test3, series G.


Fig.(16) - A comparison between the stress-strain relationship predicted by the endochronic model with laboratory tests of Al - Saady, Test4, series G.


Fig.(17) - A comparison between the stress-strain relationship predicted by the endochronic model with laboratory tests of Al - Saady,, Test5, series G.


Fig.(18) - A comparison between the volumetric strain - axial strain relationship predicted by the endochronic model with laboratory tests of Al-Saady, Test1, series G.


Fig.(19) - A comparison between the volumetric strain - axial strain relationship predicted by the endochronic model with laboratory tests of Al-Saady, Test2, series G.


Fig.(20) - A comparison between the volumetric strain - axial strain relationship predicted by the endochronic model with laboratory tests of Al - Saady, Test3, series G.


Fig.(21). - comparisons between the volumetric strain - axial strain relationship predicted by the endochronic model with laboratory tests of Al - Saady, Test 4, series G.


Fig.(22) - A comparison between the volumetric strain - axial strain relationship predicted by the endochronic model with laboratory tests of Al - Saady, Test 5, series G.
The same behaviour is noticed in this clay. The predicted volumetric strains are closer to measured strains under small stress increments. At large stresses, the predicted strains became larger.

## CONCLUSIONS:

The endochronic model overestimates the strains for all the cases simulated under high stress increments.

There is no definite yield point can be obtained when simulating the laboratory tests. This means that this model can be adopted for normally consolidated clays where ductile behaviour of the stress-strain is expected.

The error in simulation may be attributed to the model parameters, which need to be evaluated by carrying out parametric study for Iraqi clays.

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| $\begin{aligned} & \text { NOTATION: } \\ & \qquad \mathrm{d} \epsilon_{i j} \end{aligned}$ | Strain increments |
| :---: | :---: |
| dt | Time increments |
| P | Coefficient matrices |
| $\mathrm{J}_{2}$ | second deviatoric strain increment invariant |
| $\mathrm{I}_{1}$ | first strain increment invariant |
| $\mathrm{de}_{\mathrm{ij}}$ | deviatoric strain increment tensor |
| $\delta_{i j}$ | Kronecker delta |
| $d \in$ | Volumetric strain increment |
| $z_{1,} \tau_{1}$ | Constants |
| $d \xi$ | damage measure |
| $d \zeta$ | deformation measure |
| $d \lambda$ | inelastic dilatancy |
| $\mathrm{S}_{\mathrm{ij}}$ | deviatoric stress tensor |
| $\sigma_{m}$ | mean stress |
| G | shear elastic moduli |
| K | bulk elastic moduli |
| $d \epsilon^{o}$ | stress-independent inelastic strains |
| $d \sigma_{i j}$ | The stress increments |
| $D_{i j k l}$ | elastic coefficient matrix |
| $d \in_{i j}^{e}$ | elastic strain increments |
| $f(\eta)$ | Strain-hardening function. |
| $F(\sigma, \in)$ | Strain-softening function. |
| $I_{1}{ }^{\boldsymbol{\sigma}}$ | effective confining stress |
| $I_{1}^{\boldsymbol{\varepsilon}}$ | the volume change |
| $J_{2}^{\boldsymbol{\varepsilon}}$ | the second deviatoric strain invariant |
| a's | material constants |
| Pa | atmospheric pressure |
| $\beta_{1}$ | constants |
| c's | material constants |
| $\beta_{2}$ | softening coefficient |
| $\mathrm{e}_{0}$ | initial void ratio |
| $\varepsilon_{\mathrm{v}}$ | volumetric strain |
| n | porosity |
| b's | constants |
| Po | consolidation pressure |
| $\mathrm{C}_{\text {o }}$ | densification coefficient |
| E | elastic modulus |
| $\mathrm{I}_{\mathrm{L}}$ | the liquidity index of the clay |
| $\mathrm{W}_{\text {ant }}$ | natural water content. |
| $\mathrm{w}_{\mathrm{p}}$ | plastic limit |
| $\mathrm{I}_{\mathrm{p}}$ | plasticity index |
| $\mathrm{w}_{\mathrm{L}}$ | liquid limit. |

# EFFECT OF COMPACTION ON THE BEHAVIOUR OF KIRKUK GYPSEOUS SOIL 

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#### Abstract

The purpose of the present work is to investigate the effect of compaction on the behaviour of gypseous soil. A testing program carried out to study the geotechnical properties and the behaviour of gypseous soil (gypsum content $\chi=37 \% \& 56 \%$ ) taken from Kirkuk city.

The tests include classification tests, chemical tests, X-ray diffraction analysis, compaction characteristics, compressibility \& collapsibility, California Bearing Ratio (CBR) \& shear strength tests.The effect of dry unit weight, water content, compactive efforts, relative compaction \& soaking on the engineering properties of the soil tested are included in the program. All tests were carried out using Standard and Modified Proctor.

Based on the results, several conclusions have been obtained. The soil compacted at the dry side of optimum tends to collapse upon soaking while the soil compacted at the wet side of optimum tends to swell. The percent of swelling for soil with $\chi=37 \%$ is more than that with $\chi=56 \%$.

Through the observation of shear strength test results, for the two compactive efforts and the two types of gypseous soil,the cohesion(c) increases with decreasing gypsum contents.The angle of internal friction ( $\varphi$ ) decreases with increasing moulding water content and increases with increasing gypsum contents. The soaked CBR values increase with increasing compactive efforts and gypsum content.


الغرض من هذا البحث هو النحري عن تأثير الرص على تصرف التربة الجبسية. وقد تضمنت الفحوص المختبرية
برنامج لار اسة الخصائص الجيو تكنيكية و السلوك الهندسي للتربة تحت الار اسة بمحتوى جبسي\% 37 و 56\% مـــأخوذة مــن مدينة كركوك. هذا وقد اثتملت الفحوص تصنيف التربة والفحوص الكيميائية وتحليل انحر اف الاشعة الــسينية وخـصـائص الرص وفحوص الانضغاطية والانهيارية و نسبة التحمل الكاليفورني CBR وفحوص مقاومة القص .وتضمن البرنامج ايضاً دراسة وحدة الوزن الجاف والمحتوى المائي و جهـ الرص والرص النسبي والغمـر عـــى الخـصـائص الهندســية للتــرب الدفحوصة,ور قد جرت كل الفحوص باستخدام بروكتور القياسي والمحسن.
و على ضوء النتائج فقد تم الحصول على استتتاجات عديدة .لوحظ أن التزب المرصوصة بمحتوى مائي الى الجانـــبـ

للانتفاخ .كما و ان النسبة المئوية للانتفاخ لللترب بمحتوى جبسي \% 37 كانت اكثر من تلك ذات المحتوى الجبسي\% 56 .

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من خلال ملاحظة نتائج فحوص مقاومة القص ,نستتتج أنه لكل من جهيّ الرص وكلا النوعين من التربة الجبسية , 
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    الجبس. لوحظ ان قيم نسبة التحمل الكاليفورني المغورة تزداد مع ازدياد جه> الرص ونسبة الجبس. 
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## KEY WORDS

standard compaction, modified compaction, optimum, water content, maximum dry unit weight, gypsum content, cohesion, angle of friction, collapse potential, and CBR.

## INTRODUCTION

Soil compaction is the process where by soil particles are constrained to pack more closely together through a reduction in the air voids , generally by mechanical means, Ingles and Metcalf(1972).

Gypseous soil is that soil which contains enough gypsum $\left(\mathrm{CaSO}_{4} \cdot 2 \mathrm{H}_{2} \mathrm{O}\right)$ to interfere with engineering construction .It is the worst among the problematic soils as it contains soluble salt and its chemical reactions.Gypseous soil in Iraq constitutes (11 to 15) \% of the area of Iraq. Many major projects suffered from several problems related to construction on or by gypseous soils such as cracks, tilting, collapse and leaching the soil, Mahdi(2004).

Proper construction of gypseous soil embankment essentially requires a careful and slow process of compaction control since it involves a prior selection of proper fill borrow areas which have the potential contractual degree of compaction. The compaction control of gypseous soils also requires the slow heating in temperature ranging between $(60-80)^{\circ} \mathrm{C}$ for 48 hrs , instead of 24 hrs for non gypseous soils, Al-Khafaji(1997).

## MATERIALS USED:

To achieve the purpose of this study, natural gypseous soil of two different percentages of gypsum ( $37 \%, 56 \%$ ) was taken from Kirkuk city.The chemical properties of these samples are shown in Table (1).

Table (1). Chemical Properties of Soils

| Chemical composition, \% | $\mathrm{K} 1(\chi=37 \%)$ | $\mathrm{K} 1(\chi=56 \%)$ |
| :---: | :---: | :---: |
| $\mathrm{Al}_{2} \mathrm{O}_{3}$ | 5.9 | 4.96 |
| CaO | 21.98 | 25.2 |
| $\mathrm{SO}_{3}$ | 13.8 | 22.6 |
| Gypsum content | 37 | 56 |
| $\mathrm{Cl}^{-}$ | 0.088 | 0.096 |
| pH | 7.8 | 7.8 |

The components of the minerals for each type of saline soil are given in Table (2). It can be noted that gypsum, quartz, calcite, and Palygroskite are the predominated minerals in the soils.

Table (2). Mineralogical composition of soils

| Soil Type | Non Clayey Mineral | Clayey Mineral |
| :--- | :--- | :--- |
| $\chi=37 \%$ | Gypsum, Calcite, Quartz. | Palygroskite |
| $\chi=56 \%$ | Gypsum, Calcite, Quartz, Dolomite, Feldspar. | Palygroskite |

Classification tests were performed first. Physical tests include specific gravity Gs, grain size distribution and Atterberg limits. Standard and modified compaction tests were carried out to determine the moisture-density relationships.Series of engineering tests were conducted on compacted samples. The tests performed include standard oedometer test, double oedometer test, triaxial and CBR tests.
The physical and compaction characteristics are given in Table (3).

Table (3). Summary of physical and classification tests results.

| Soil Property | Soil Designation |  |
| :---: | :---: | :---: |
|  | K1 | K2 |
| Gypsum Content,\% | 37 | 56 |
| Specific gravity | 2.51 | 2.46 |
| Liquid limit,\% | 29 | 29 |
| Plasticity Index,\% | 8 | 7 |
| \%Sand | 82.31 | 77.18 |
| \%Fines | 17.66 | 22.82 |
| Moisture-density relations <br> (D698) <br> Optimum water content (\%) <br> Maximum dry unit weight(kN/m3) | 17.73 | 17.6 |
| Moisture-density relations <br> (D1557) <br> Optimum water content (\%) <br> Maximum dry unit weight(kN/m3) | 18.75 | 13.85 |
| Soil Classification According to <br> ASTM D 2487 | SM | SM |

## PREPARATION OF COMPACTED SAMPLES:

The following procedure was adopted in preparing the compacted soil samples for the oedometer and collapse tests. The soil was compacted using standard and modified Proctor procedure, and then the compacted samples were extruded from compaction mould by pushing the test ring to the required thickness. The faces were leveled after trimming

A manufactured hammer was adopted to carry out the preparing of compacted soil samples for triaxial shear tests. A hammer of 1.9 cm diameter, 500 gm mass and 30 cm drop as shown in Plate (1). Table (4) shows the required number of blows that gives the same compactive effort of the standard and modified compactive effort. The drop height, weight of hammer and number of blows were determined on the basis of the standard and modified compactive efforts.

Plate (1). Manufactured hammer.


Table (4). Corresponding compactive efforts in the manufactured hammer.

| Type of compaction | No. of blows / layer in the compaction mould | Compactive effort, CE in compaction mould (kN.m/m ${ }^{3}$ ) | No. of blows / layer in manufactured mould | Compactive effort, CE in manufactured mould ( $\mathrm{kN} . \mathrm{m} / \mathrm{m}^{3}$ ) |
| :---: | :---: | :---: | :---: | :---: |
| Standard compaction | 25 blows <br> (3 layers) | 593.7 | 3 layers (2 of them compacted @ 12 blows and the other @ 11 blows) | 597.525 |
| Modified compaction | 25 blows <br> (5 layers) | 2710 | 5 layers (4 of them compacted @ 32 blows and the other @ 31 blows) | 2714.48 |

* Compaction Mould of 4 " diameter.


## COMPRESSIBILITY TESTS:

A series of Oedometer tests were carried out using standard back loading Oedometer. The sample size used 50 mm in diameter by 19 mm in height.

The series of Oedometer tests include two tests as follows:

## Standard consolidation tests:

These tests were carried out on compacted samples to determine the compressibility characteristics. These tests were performed on samples prepared at different water content and dry unit weights of the standard and modified compaction tests.

## Double Oedometer Tests:

This test was conducted according to Jennings \& Knight (1957). In this test, two samples were tested. The first one was loaded at its initial water content throughout the test without addition any water (dry test). Precautions were taken to minimize the evaporation of water from specimen by covering the cell with a nylon bag. The other sample was primarily saturated them loaded progressively as in the standard consolidation test. The difference between the two curves quantifies the amount of deformation that would occur at any stress level if the soil to be saturated during it is loading history.

## SHEAR TESTS

The purpose of those tests was to investigate the shear strength characteristics of the compacted gypseous soil. Further more the effects of soaking on the strength characteristics were studied.

## Triaxial Compression Tests:

To study the effect of water content and dry unit weight on shear strength of the soil tested, $\underline{\text { Unconsolidated }} \underline{U}$ ndrained tests, $\underline{\mathbf{U}} \underline{\mathbf{U}}$ were conducted on specimens ( 38 mm in diameter and 76 mm in height) compacted at different water contents and dry unit weights of the standard \& modified compaction tests by mean of manufactured hammer .

## California Bearing Ratio (CBR) test

Two series of tests were conducted on each soil sample (K1, K2). For the first series, the preparation of specimens and testing procedure were generally in accordance with AASHTO T14381. Three specimens were prepared at optimum water content of the standard compaction test. And compacted in three layers using 2.5 kg hammer dropped from a height of 30.5 cm . Ten, thirty and sixty-five blows per layer were used for compacting the three specimens.

Identified specimens were prepared and testing after soaking in water until the swelling is ended to simulate the effect of saturation on the bearing characteristics.

In the second series, the whole program was repeated on specimens prepared at optimum water content of the modified compaction test and compacted in five layers using 4.5 kg hammer dropped from height of 45 cm .

In these entire tests, surcharge weights of 4.5 kg , in form of annular steel rings, were placed on the top surface of the prepared specimens before testing. The surcharge simulates the effect of the thickness of road construction overlaying the layer being tested.

## RESULTS AND DISCUSSION:

## Grain size distribution:

Table (5) shows the grain size distribution data. This table revealed that both soils with gypsum content $\chi=37 \%, \chi=56 \%$ consist of coarse, medium and fine sand. The data for both soils reflects a significant difference between the dry and wet sieving by water, with respect to soil with
gypsum content equal $37 \%$ the dry sieving showed only $13.84 \%$ fines while the wet sieving or natural specimen results in $70.02 \%$ fines.

The variation in the grain size distribution by both techniques (dry andwet by water) is attributed to the cementing agent (gypsum), which softens or dissolves in water, Ismael and Mollah (1998).

However, depending on either dry or wet sieving by kerosene, the soils can be classified according to ASTM D 2487 as (SM), i.e., silty sand.

Table (5). Results of Sieve Analysis.

| Sample Type |  | Sieving method | $\begin{gathered} \text { Gravel } \\ (>4.75) \mathrm{mm} \end{gathered}$ | $\begin{gathered} \text { Coarse } \\ (2-4.75) \\ \mathrm{mm} \end{gathered}$ | Medium sand (0.427- 2) mm | Fine sand (0.0750.425) mm | Silty clay $\begin{gathered} (<0.075) \\ \mathrm{mm} \end{gathered}$ | Specific <br> gravity <br> Gs |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \chi \\ =37 \% \end{gathered}$ | Natural | Dry | 0.04 | 11.15 | 42.61 | 32.36 | 13.84 | - |
|  | Natural | Wet (water) | 0 | 0.64 | 8.7 | 20.63 | 70.02 | 2.49 |
|  | Natural | Wet (kerosene) | 0.03 | 10.93 | 38.59 | 32.79 | 17.66 | 2.51 |
| $\begin{gathered} \chi \\ =56 \% \end{gathered}$ | Natural | Dry | 0 | 2.52 | 42.28 | 30.52 | 24.69 | - |
|  | Natural | Wet (water) | 0 | 0.25 | 12.38 | 20.46 | 66.91 | 2.47 |
|  | Natural | Wet (kerosene) | 0 | 2.48 | 42.53 | 32.17 | 22.82 | 2.46 |

## COMPACTION TESTS:

Relationships between dry unit weight and water content for the tested soil are shown in Fig. (1) for compactive efforts associated with the modified and standard Proctor.It is noticed that the standard maximum dry unit weight of the soil with gypsum content $\chi=37 \%$ is somewhat higher than the standard maximum dry unit weight of the soil with gypsum content $\chi=56 \%$, while the opposite is true for modified compaction test as shown in Fig. (1).

This behaviour may be explained by the role of gypsum in the soil as stated by Al-Mufty (1997). In other words, the standard compaction curve where specific gravity and cementing of gypsum (both of them decreases as the gypsum content increase which tends to decrease the unit weight) are the predominate factors, while in the modified compaction tests, filling the voids which tends to increase the unit weight with increasing gypsum content is the controlled factor rather than the other two factors (specific gravity and cementing of gypsum).

It can be concluded from the water-unit weight relationships, that the test results are depending on the soluble salt content (gypsum content) water content, soil components, the solubility degree of gypsum in water and compactive effort.


Fig. (1). Compaction curves for $\chi=37 \%$ and $\chi=56 \%$.

## OEDOMETER TESTS:

## Compression Tests:

The results are presented as void ratio versus logarithm of vertical pressure and are shown in Figs (2) and (3) for all tested specimens.

It can be seen that the shape of e-log pressure curves for compacted samples with gypsum content $\chi=56 \%$ is steeper than the curves of samples with gypsum content $\chi=37 \%$. This is due to the effect of gypsum content.

Table (6) and Figs (2) and (3) show the tests results for the two groups. It is noticed from Table (6) that compression index increased for soaked specimens. This is due to soften and dissolve of gypsum.

## Double Oedometer:

The effect of compaction on the collapse behaviour of the tested soil was investigated by conducting the double oedometer test. To give a clear picture of tests results, collapse potential, CP , \% for both gypsum contents and both compactive efforts as a function of moulding water content for all vertical pressures are plotted as shown in Figs (4) to (5).

Table (6). Results of compression tests.

| $\\| \frac{\stackrel{0}{2}}{\stackrel{\rightharpoonup}{i}}$ |  | As compacted specimens |  |  |  |  | Soaked specimens |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\begin{gathered} \gamma \mathrm{d} \\ \mathrm{kN} / \mathrm{m}^{3} \end{gathered}$ | $\begin{aligned} & \text { w.c } \\ & \% \end{aligned}$ | e。 | Cc | Cr | $\begin{gathered} \gamma \mathrm{d} \\ \mathrm{kN} / \mathrm{m}^{3} \end{gathered}$ | $\begin{gathered} \text { w.c } \\ \% \end{gathered}$ | e。 | Cc | Cr |
| $\begin{array}{\|l\|l} \stackrel{\circ 9}{8} \\ \stackrel{\pi}{1} \\ \hline \end{array}$ |  | 17.73 | 13.5 | 0.416 | 0.128 | 0.024 | 17.73 | 13.5 | 0.416 | 0.1 | 0.020 |
|  |  | 17.46 | 11 | 0.437 | 0.161 | 0.021 | 17.46 | 11 | 0.437 | 0.173 | 0.023 |
|  |  | 17.46 | 16.1 | 0.437 | 0.131 | 0.026 | 17.46 | 16.1 | 0.437 | 0.134 | 0.023 |
|  |  | 16.5 | 8 | 0.52 | 0.171 | 0.0193 | 16.5 | 8 | 0.52 | 0.146 | 0.022 |
|  |  | 18.75 | 0.75 | 0.339 | 0.156 | 0.024 | 18.75 | 10.75 | 0.339 | 0.071 | 0.029 |
|  |  | 17.46 | 6.25 | 0.437 | 0.134 | 0.023 | 17.46 | 6.25 | 0.437 | 0.128 | 0.028 |
|  |  | 17.46 | 15.75 | 0.437 | 0.203 | 0.01 | 17.46 | 15.75 | 0.437 | 0.125 | 0.011 |
|  |  | 18.125 | 8 | 0.385 | 0.116 | 0.019 | 18.125 | 8 | 0.385 | 0.111 | 0.027 |
| $\begin{array}{\|l} 00 \\ i \\ i n \\ 0 \end{array}$ |  | 17.6 | 13.85 | 0.396 | 0.11 | 0.017 | 17.6 | 13.85 | 0.396 | 0.095 | 0.022 |
|  |  | 17.46 | 11.6 | 0.4078 | 0.1 | 0.019 | 17.46 | 11.6 | 0.408 | 0.164 | 0.023 |
|  |  | 17.46 | 16 | 0.7078 | 0.133 | 0.017 | 17.46 | 16 | 0.408 | 0.166 | 0.019 |
|  |  | 16.25 | 8 | 0.513 | 0.181 | 0.016 | 16.25 | 8 | 0.513 | 0.17 | 0.025 |
|  |  | 18.8 | 9 | 0.307 | 0.097 | 0.027 | 18.8 | 9 | 0.307 | 0.091 | 0.023 |
|  |  | 17.46 | 4.75 | 0.4078 | 0.117 | 0.025 | 17.46 | 4.75 | 0.408 | 0.11 | 0.028 |
|  |  | 17.46 | 15.5 | 0.4078 | 0.137 | 0.022 | 17.46 | 15.5 | 0.408 | 0.199 | 0.037 |
|  |  | 18.75 | 8 | 0.311 | N.D | N.D | 18.75 | 8 | 0.311 | N.D | N.D |



Fig.(2).Compression curves for soil samples of standard compaction at: (a) w.c=8\%, (b) dry side, (c) optimum water content, (d) wet side.


Fig. (3).Compression curves for soil samples of modified compaction at: w.c=8\%,(b) dry side, (c) optimum water content, (d) wet side

From these figures, in general, the trend of the tested samples were found to collapse from dry side of optimum for both gypsum contents and both compactive efforts until it reached the optimum water content the trend was changed to swell where the swelling is higher for samples of gypsum content $37 \%$. This behaviour can be explained as follows: as the water enters the soil void leads to soften the cementing bonds that took place in term of collapse potential. Collapse potential increased with a decrease in gypsum content. This may be attributed to the effect of sand-silt mixture, as the amount of silt size particles become angular in shape due to crushing of sand by compaction. As a result of that, the collapse decreased. This behaviour was noticed by Assallay, Rogers and Smalley (2004). They found that higher collapse values were obtained when the angular silt fraction was replaced with smooth, spherical glass balls thus confirming that the geometrical properties of the silt particles have a significant effect on the hydro collapse behaviour of loess deposits.

As the water content increased, the role of Palygroskite will begin in term of swelling which increased then decreased. The swelling can occur when anhydrous calcium sulphate imbibes water ,Abduljawad (1994).This process of gypsification refers to the addition of water crystallization to the mineraland is associated with a volume increase of up to $62 \%$,Blatt et al.(1980). The swelling was noticed to increase as the gypsum content decreased. This phenomenon could be attributed to the effect of gypsum in limiting the amount of swelling at higher water content as reported by Bridge and Tunny (1973). They explained this effect to the replacement of ions in the clay mineral by the calcium on the clay exchange sites.


Fig. (4). Influence of moulding water content on collapse potential from double oedometer of compacted soil specimens: (a) $\chi=37 \%$ (b) $\chi=56 \%$ of standard compaction.


Fig. (5). Influence of moulding water content on collapse potential from double oedometer of compacted soil specimens: (a) $\chi=37 \%$, (b) $\chi=56 \%$ of modified compaction.

## SHEAR STRENGTH CHARACTERISTICS:

## Triaxial Compression Tests:

Different dry unit weights and moulding water contents of the standard and modified compaction tests were adopted to obtain a complete picture of effect compactive effort on shear behaviour of the tested gypseous soils.

Fig.(6) shows the shear strength parameters cohesion c and angle of internal friction $\varphi$ as a function of compactive effort for both gypsum contents. From the results, the following can be observed:
a- The cohesion c increased as the compactive effort increased for both gypsum content.
b- The angle of internal friction $\varphi$ also increased with an increase in compactive effort for both gypsum content with a decrease in moulding water content.


Fig. (6). (a) Angle of internal friction, (b) cohesion versus compactive energy.

To show a clear picture of effect moulding water content on shear strength parameters c and $\varphi$, figs (7) and (8) are plotted.


Fig. (7). Relationship between cohesion and moulding water content of soil tested.
Fig. (7) shows that the cohesion c increased with increasing compactive effort and decreased with increasing gypsum content. The increase in cohesion for all compactive efforts and gypsum content with increasing moulding water content till it reaches a maximum value at optimum water content then tends to decrease in similar manner of compaction curve.

As the cohesion which is due to internal forces holding soil particles together in a solid mass so, as the gypsum content increased, the generated crystal formation pressure in the pore spaces increased leading to rupture of primary and newly bond, as a result of which cohesion is reduced.


Fig. (8). Relationship between angle of internal friction and moulding water content of soil tested.

Examining Fig.(8) revealed that the angle of internal friction decreased with increase moulding water content because water acts as a lubricant reducing friction and minimizing the sliding effect, which leads to reduce the angle of friction. It is also clear that angle of internal
friction increased with increasing gypsum content for both compactive efforts. This may be attributed to the fact that $\varphi$ increased with increasing coefficient of uniformity Cu of the soil, where $C u=17$ for soil with gypsum content $=37 \%$ while $C u=25$ for soil gypsum content $=56 \%$. Furthermore, the friction between gypsum particles is greater than mineral components of the soil.

Figs (9.a) and (9.b) show the shear strength as a function of moulding water content. From the results, the following can be observed:
a- The shear strength tends to increase with increasing confining pressure for both compactive efforts and both gypsum contents. This increased is somewhat little at wet side of optimum. As seen in compaction curves for both soils ( $\chi=37 \%$ and $\chi=56 \%$ ), the selected points at wet side of optimum could be considered nearly saturated soils ( $\mathrm{S}=92.35 \%$ and $\mathrm{S}=90.3 \%$ for standard and modified compaction tests of $\chi=37 \%$ and $\mathrm{S}=96.44 \%$ and $\mathrm{S}=93.42 \%$ for standard and modified compaction tests of $\chi=56 \%$ ). This behaviour can be explained in terms of pore pressure in the saturated soil, the pore water takes up which is a portion of applied load.
b- In standard compactive effort for both gypsum content, shear strength decreases as the moulding water content increased, while in modified compactive effort the shear strength increased as the moulding water content increased until it reached the optimum water content then decreased as the water content increased.


Fig. (9). Influence of moulding water content on shear strength compacted soil samples of $\chi=37 \%$ and $\chi=56 \%$ : (a) standard, (b) modified.

## California Bearing Ratio (CBR) Tests:

The tests were performed on samples prepared at optimum water content and compacted to various unit weights. A second series of tests were performed on specimen soaked in water for 4 days to give an indication of strength loss due to saturation and to give information concerning

Soaked CBR values at 2.5 and 5 mm penetration are summarized in Table (7).

Table (8). Results of CBR Tests.

| Soil type | No. of blows | 2.5 kg hammer |  | 4.5 kg hammer |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | CBR <br> @ 2.5 mm <br> penetration | CBR <br> @ 5.0 mm <br> penetration | CBR <br> @ 2.5 mm <br> penetration | CBR @ 5.0mm penetration |
|  | 10 | 1.133 | 2.987 | 4.0 | 4.13 |
|  | 30 | 3.437 | 2.8557 | 7.93 | 8.767 |
|  | 65 | 5.589 | 4.959 | 10.196 | 12.024 |
|  | 10 | 2.077 | 1.754 | 2.832 | 3 |
|  | 30 | 9.479 | 9.143 | 7.55 | 10.52 |
|  | 65 | 13.784 | 14.024 | 35.876 | 42.08 |

It can be seen that CBR values are greater at 2.5 and 5 mm penetration for gypsum content $\chi$ $=56 \%$ than the corresponding values for gypsum content $\chi=37 \%$. This may be attributed to the gypsum content as this result coincides with the effect of gypsum in reducing the plasticity of the tested soil, since the plasticity index can be considered as a shear index as well Rodrigues, Castillo and Sowers (1988). A summary of all CBR soaking test results for both gypsum contents at 2.5 and 5 mm penetration are presented in Fig. (10).

The soaked values of CBR are plotted against the number of blows per layer in Fig (11). In all cases shown in this figure, CBR values found to increase with increase in number of blows, weight of hammer used and gypsum content. Fifty six blows per layer are generally required to mould CBR specimen to hundred percent of the maximum dry unit weight determined by ASTM D 678-70 and D 1557-70, at this number of blows, a soaked CBR values of $5 \%$ and $11 \%$ are obtained for soil with gypsum content $\chi=37 \%$ whereas, for soil with gypsum content $\chi=56 \%$, soaked CBR gives high values in the range (12.5-34\%).

It is worth to mention that at this stage: by relating the soaked CBR values obtained at $100 \%$ of the maximum dry unit weight and optimum water content of the standard and modified compactive efforts with the shear parameters cohesion c and angle of internal friction $\varphi$ that gained from triaxial tests of samples compacted at maximum dry unit weight and optimum water content of the standard and modified compactive efforts for both gypsum content as shown in Fig. (12).

From this figure, the cohesion is observed to decrease with increasing soaked CBR values while the angle of internal friction is seemed to increase with increasing soaked CBR values with increasing compactive efforts.



Fig. (10). CBR values at 2.5 and 5 mm penetration for gypsum content: (a) $\chi=37 \%$, (b) $\chi=56 \%$.


Fig. (11). Number of blows per layer versus CBR: (a) $\chi=37 \%$, (b) $\chi=56 \%$.


Fig. (12). Variation of shear strength parameters with soaked CBR values: (a) Angle of internal friction, (b) Cohesion.

## CONCLUSIONS

A program of laboratory tests was carried out on two types of gypseous soil taken from Kirkuk city. Tests were performed on compacted soil samples using Standard and Modified Proctor. Based on the results, the following conclusions are made:
-With the increase in compactive effort, the maximum dry unit weight increases and the optimum water content decreases for both types of gypseous soil. The percent increase in dry unit weight is $5.75 \%$ and $6.82 \%$ and the percent decrease in optimum water content is $20.4 \%$ and $35.02 \%$ for soils with gypsum content $\chi=37 \%$ and $\chi=56 \%$ respectively.
-Compacted soil specimens at dry side of optimum tend to collapse after soaking with water while soil specimens compacted at wet side of optimum tend to swell for both compactive efforts. The percent of swell of soil with $\chi=37 \%$ is more than that with $\chi=56 \%$.
-Shear strength parameters (cohesion and friction) increase with increase in gypsum content. The cohesion (c) increases with the increase in moulding water content till it reaches a maximum value at optimum water content then tends to decrease in a manner similar in shape of compaction curve.
This behaviour is independent of compactive effort and gypsum content.
The angle of internal friction $(\varphi)$ decreases with the increase in moulding water content and with the decrease in gypsum content for both compactive efforts.

- Values of California Bearing Ratio (CBR) at 2.5 mm and 5 mm penetration are higher for soil with gypsum content $\chi=56 \%$ as compared with the corresponding values for gypsum content $\chi=37 \%$.
- The soaked CBR values increase with the increase in compactive efforts (number of blows, weight of hammer used) and gypsum content.
-The increase in soaked CBR values obtained at maximum dry unit weight and optimum water content were found to be compatible with the increase in angle of friction and decrease in cohesion for both types of compactive efforts.


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## ABBREVIATIONS AND NOTATIONS

## AASHTO: American Association of State Highway and Transportation Officials

ASTM: American Sociaty of Testing Material
CBR: California Bearing Ratio, \%
Cu : Coefficient of uniformity
CP: Collapse potential, \%
c: $\quad$ Cohesion (kPa)
Gs: Specific gravity
K1: Soil with gypsum content $37 \%$
K2: Soil with gypsum content $56 \%$
S: Degree of saturation
SM: Silty Sand
$\underline{\mathrm{U}}-\underline{\mathrm{U}}: \quad$ Unconsolidated Undrained
$\chi$ : Gypsum content
f : Angle of internal friction

# PREDICTION OF THE EFFICIENCY OF SIEVE TRAY USING AIRWATER SYSTEM 

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#### Abstract

This investigation deals with the effect of weir height, liquid and gas flow rate on tray efficiency. The tests were carried out on a single pass cross flow tray of air-water system of 0.3 m diameter for clear liquid height over sieve tray with weir height 3,4 and 5 cm .

Point efficiency values were found to be in the same range for different weir height, but it improves slightly with weir height. And the average values of point efficiency were $83 \%$ for 3 cm weir height, $85 \%$ for 4 cm weir height and $89 \%$ for 5 cm weir height. While, point efficiency of $90 \%$ was obtained for 5 cm weir height and liquid flow rate ranging between 5.8 to $7.32 \mathrm{~m}^{3} / \mathrm{s}$.

In the range of clear liquid height over hole diameter $\left(\mathrm{h}_{\mathrm{L}} / \mathrm{d}_{\mathrm{H}}\right)$ between 2 to 10 , increasing the Reynolds number ranging between $2.0 * 10^{5}$ to $1.6 * 10^{6}$ for gas phase increases point efficiency.

Prediction of Murphree (Tray) efficiency using Lopez and Castells (1999) equation shows that the ratio of $\mathrm{E}_{\mathrm{MV}} / \mathrm{Ep}$ is equal to 1 , due to low value of calculated Peclet number (degree of liquid mixing), which ranged between 0.07 to 1.5 .


الخلاصة
درس هذا البحث تاثير تغير كل من إرتفاع السد و جريان السائل و الغاز على إرتفاع السائل فوق الصينية المنخلية و كفائتها لنظام هواء هماءاء. يزد داد ارتفاع السائل فوق صينية اختبار واحدة ذات قطر 0.3 متر و عدد فتحـات 213 فتحـة و ارتفـاع سد3 و4 و و5 سم بزيادة جريان السائل بين 0.12 الى 0.58 متر مكعب لساعة ويقل مع زيادة جريان الغاز من 35 الى 100 متر مكعب \ساعة.
 83\% لار تفاع سد3 سم و 85\% لار تفاع سد 4 سمو 89\% لارتفاع سد 5 سم . في حين اعلى قيمـة للكفـاءة النقطيـة كانت 90\% \% لار تفاع سد 5 سم و جريان ماء بين 8.5 و 7.32 م³/ ثا .

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كذلك زيادة عدد رينوللاز للطور الغازي يزيد من الكفاءة اللقطية للصواني المنخلية في حالة كون نسبة إرتفاع السائلّ إلى قطر ثقب الصينية تتز او ح بين 2 إلى 10.
 ميرفري إلى الكفاءة النقطية كانت تساوي واحد بسبب إنخفاض قيم عدد بكلت للسائل و التي تراوحت بين 0.07 و 1.5. KEYWORDS
Sieve tray, Tray efficiency, Point efficiency, Murphree plate efficiency

## INTRODUCTION

The tray efficiency governs the number of actual trays needed to achieve the desired product purity specifications. With highly efficient trays one can install a lower number of these highly efficient trays to achieve the separation desired.

Several tray efficiency definitions in use. Three different efficiencies are useful, in particular (Wijn, 2003).

- The overall efficiency (Eo), the socalled: Fenske efficiency.
- The average tray efficiency, first defined by Murphree $\left(E_{M V}\right)$.
- The local (or point) efficiency ( $E p$ ).

For nonreactive systems, several methods are available for estimating the Murphree tray efficiency from point efficiency estimates made either from laboratory-scale measurements, such as using an Oldershaw column, or from published correlations (Dribika and Biddulph, 1986; Bennett and Grimm, 1991; AIChE, 1958). Klemola 1998 lists references for more than a dozen tray efficiency correlations. For each of these methods, the conversion of point efficiency to tray efficiency relies on the choice of the mixing model to be used.

The liquid mixing on the tray has been modeled using several approaches. Lewis (1936) analyzed the ideal case of plug flow across the tray, which may be approached for large diameter columns. Gautreaux and O'Connell (1955) treated the flow as a series of perfectly mixed pools across the tray. The primary difficulty in the utility of their method is incorrectly estimating the number of mixed pools on the tray. The AIChE (1958) study used a more rigorous mixing model based on eddy diffusivity for diffusive backmixing based on the dimensionless Peclet number AIChE, (1958). Foss et al. (1958) developed a method for relating the Peclet number to the number of perfectly mixed pools across the tray. More recent work has included mixing models of increasing complexity Prado and Fair, (1990); Garcia and Fair, (2000).

For nonreactive systems with cross-flow trays, the concentration varies across the tray as a result of nonideal mixing. In the limit of perfect liquid mixing on the tray, the concentration is constant across the tray and the point efficiency and tray efficiency are the same. For nonideal mixing, concentration gradients develop across the tray that lead to differences in the tray and point efficiencies. In the extreme limit of plug flow across the tray, the concentration gradient is maximized and the difference is also at a maximum.

Bennett et al. (2000) used the recent correlation reported by Bennett et al. (1997), they address point efficiency, entrainment, mixing within the froth, weeping, and cross-flow and parallel-flow tray types. Their correlation for point efficiency is:
$E=1-\exp \left[\frac{-0.0029}{1+m \frac{\rho_{M V}}{\rho_{M L}} \sqrt{\frac{D_{V}\left(1-\varphi_{e}\right)}{D_{L}\left(\frac{A_{H}}{A_{B}}\right)}}}(\operatorname{Re})^{0.4236}\left(\frac{h_{L}}{d_{H}}\right)^{0.6074}\left(\frac{A_{H}}{A_{B}}\right)^{0.3195}\right]$

There are no generalized correlations that apply to all types of tray deck designs. So, this approach will use the broadly based correlations developed for sieve trays to develop some optimization rules and then to discuss the implications of using other types of trays on these rules. The optimization goals are:

1. Maximizing theoretical stages per section or column height,
2. Minimizing pressure drop per theoretical stage, and
3. Maximizing the operational range, turn-down, or turn-up.

## MURPHREE AND POINT EFFICIENCIES

The Murphree vapor efficiency for a tray is defined as the ratio of the actual change in vapor mole fraction for a component divided by the change in mole fraction that would be experienced if the vapor leaving the tray were in equilibrium with liquid leaving the tray.

$$
\begin{equation*}
E_{M V}=\left(\frac{\bar{y}_{n+1}-\bar{y}_{n}}{y_{n+1}-y_{n}^{*}}\right)_{\text {Tray }} \tag{2}
\end{equation*}
$$

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When $E_{M V}$ is Murphree vapor efficiency, $\bar{y}_{n+1}$ is average mole fraction in the vapor entering the tray, $\bar{y}_{n}$ is average mole fraction in the vapor leaving the tray, and $y_{n}^{*}$ is the mole fraction that would be in equilibrium with liquid leaving the tray.

The point efficiency $E p$ is defined similarly, but applies to a particular point on the tray, with a particular liquid-phase composition.

$$
\begin{equation*}
E p=\left(\frac{y_{n+1}-y_{n}}{y_{n+1}-y_{n}^{*}}\right)_{p o \text { int }} \tag{3}
\end{equation*}
$$

The point efficiency follows from application of the two-film-mass-transfer model for point of vapor as it travels up-ward through the liquid phase and engages in mass-transfer exchange with the liquid. The liquid composition is assumed to be constant in the vertical direction.

The key point in introducing the above equations is to realize that difference between point efficiency and Murphree vapor efficiency arises as a result of the variation in $y^{*}$ that occurs across the tray as liquid phase composition changes. These changes result from mass balance consideration (as components are absorbed or desorbed) for no reactive system, and from both mass balance and chemical reactive consideration for reactive system. Thus, it is necessary to perform some type of integration across the tray, that is to invoke a mixing model, to account for these changes. In addition, for fast reactions where local mass-transfer coefficients are enhanced depending on the local concentration of reactants, the resulting gradient in mass-transfer enhancement factor must also be accounted for (Fisher and Rochelle, 2002).

## EFFECT OF MIXING AND SIGNIFICANCE OF LIQUID PECLET NUMBER (PE) ON $E_{M V} / E P$ RELATIONSHIP

The assumption of Lewis (1936) concerning lack of liquid mixing (backmixing) on the gas-liquid contacting tray (although mathematically expedient at the time) is in reality not true; just as total liquid mixing equally not true in traditional industrial-size columns (diameter equal to or grater than one meter). In fact, a degree of liquid backmixing always exists in the liquid as it traverses the tray of such columns. The degree of liquid mixing is characterized by the Peclet number ( Pe ).

$$
\begin{equation*}
P e=\frac{Q_{L} Z_{o}^{2}}{A_{a} h_{L} D e} \tag{4}
\end{equation*}
$$

A small Peclet number indicates a high degree of mixing and vice versa. According to (Lo'pez and Castells, 1999), if $P e$ is less than 0.2 the liquid is considered well-mixed such that $E_{M V}$ can be considered equal to $E p$. On the other hand a $P e$ value of about 39 indicates condition approaching liquid plug flow on the tray (Dribika and Biddulph, 1986). Hence a $P e$ value of 50 and higher indicates definite liquid plug flow condition. In such a case the tray efficiency will be larger than point efficiency; the difference between them increasing as $P e$ increases.

Of the above models, the AlChE study (1958) seems to be still the most popular (Lo'pez and Castells, 1999) and is as follows:

$$
\begin{equation*}
\frac{E_{M V}}{E_{P}}=\frac{1-e^{-(\eta+P e)}}{(\eta+P e)\left(1+\frac{\eta+P e}{\eta}\right)}+\frac{e^{\eta}-1}{\eta\left(1+\frac{\eta}{\eta+P e}\right)} \tag{5}
\end{equation*}
$$

Where

$$
\begin{equation*}
\eta=\frac{P e}{2}\left[\sqrt{\left(1+\frac{4 \lambda_{o} E}{P e}\right)}-1\right] \tag{6}
\end{equation*}
$$

## Eddy diffusivity ( $\boldsymbol{D e}$ )

As pointed out in the previous section, one of the parameters affecting the liquid Peclet number value (and consequently the degree of liquid mixing as it traverses the tray) is the eddy diffusivity ( De ). Usually specific eddy diffusivity is measured experimentally (Chan and Fair, 1984),

To develop a simple relationship and to approximately account for eddy diffusion and the liquid continuous region, droplet mass exchange was assumed to occur over the entire two-phase layer height $h_{2 \Phi}$, . Hence, Bennett and Grimm (1991) correlation was:

$$
\begin{equation*}
D e=0.02366\left(g h_{2 \Phi}^{3}\right)^{1 / 2} \tag{7}
\end{equation*}
$$

Where for the correlation (equation (7)):

$$
\begin{align*}
& h_{2 \Phi}=h_{F e}+\left[\frac{0.794 K_{s}^{2}}{\left(A_{h} / A_{a}\right) \Phi_{e}}\right]  \tag{8}\\
& h_{F e}=C^{\prime}\left[\frac{Q_{L}}{\Phi_{e}}\right]^{2 / 3}+h_{w}  \tag{9}\\
& \Phi_{e}=\exp \left(-12.55 K_{s}^{0.91}\right) \tag{10}
\end{align*}
$$

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$$
\begin{equation*}
C^{\prime}=0.501+0.439 \exp \left(-137.8 h_{w}\right) \tag{11}
\end{equation*}
$$

The correlation (equation (7)) was modified later by Bennett et al. (1997) taking also into consideration diffusion resulting from turbulence in the liquid continuous region. This modified correlation was given by Lo'pez and Castells (1999) as follows:

$$
\begin{equation*}
D e=(4)(0.024)\left(g h_{2 \Phi}^{3}\right)^{1 / 2} \tag{12}
\end{equation*}
$$

Where for this correlation

$$
\begin{equation*}
h_{2 \Phi}=h_{F e}\left[1+\left(1+6.9\left(\frac{h_{L}}{d_{H}}\right)^{-1.85}\right) \frac{F r_{G}}{2}\right] \quad \text { (13) } \quad F r_{G}=\frac{V_{e j}^{2}}{g h_{F e}} \tag{13}
\end{equation*}
$$

$$
\begin{equation*}
V e_{j}=3 K_{s} \sqrt{\frac{\sqrt{3}}{\left(A_{h} / A_{a}\right) \Phi_{e}}} \tag{14}
\end{equation*}
$$

## Experimental Work

## Equipment

The experimental laboratory apparatus used is shown in Fig. 1 and consisted of the following:
i. Glass column. (QVF)
ii. Liquid storage tank.
iii. Blower.
iv. Centrifugal pump.
v. Connecting piping.
vi. Measuring instruments

## Geometrical parameters

The following specifications were used which were concluded from Coulson (1985), Treybal (1981) and Ludwig (1979).The plate used is shown in Fig. (2)

Material of construction of sieve plate aluminum alloy A-1050 ( $99.5 \%$ by wt. Al)

Column diameter
Hole diameter
Plate thickness
Weir height
Weir length

30 cm
5 mm
5 mm
$3 \mathrm{~cm}, 4 \mathrm{~cm}, 5 \mathrm{~cm}$
22 cm

| Length of liquid path | 22 cm |
| :--- | :--- |
| Total no. of holes | 213 |
| \% Free area | 7.7 |
| Active or bubbling area | $0.05372 \mathrm{~m}^{2}$ |
| Vapor density (air) standard | $1.1982 \mathrm{~kg} / \mathrm{m}^{3}$ |
| Liquid density (water) standard | $997.94 \mathrm{~kg} / \mathrm{m}^{3}$ |
| Hole pitch | 13.5 mm triangular |
| Hole area /Active area | $13.16 \%$ |
| Active area /Column area | $76.1 \%$ |
| Outlet calming zone width | 18 mm |



Fig. (1), Schematic diagram of the experimental rig

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No. of holes $=213$
Diameter of hole $=0.5 \mathrm{~cm}$
Fig. (2)., Schematic diagram of the sieve tray

## Experimental procedures

The experimental program related to the laboratory rig consisted of the following particular steps employed for the operational system:

1. Initially, a sufficient quantity of the liquid to be used was prepared and introduced to the larger of the one liquid tank. This liquid quantity amounted to about $50 * 10^{-3} \mathrm{~m}^{3}$.
2. The air blower was operated and the air flow was adjusted by a manual gate valve (placed on the 3 " ND pipe) utilizing the installed calibrated orifice meter for this purpose. This value of air flow corresponded to the minimum required to avoid dumping of the liquid from the perforated test tray at its minimum adopted inlet flow rate of $0.25 \mathrm{~m}^{3} / \mathrm{h}$.
3. The main supply/recirculating liquid pump was then operated and the liquid flow was adjusted at $0.1 \mathrm{~m}^{3} / \mathrm{h}$ by the globe valve upstream of the area flow meter which was utilized for this purpose. This value of liquid flow rate was practically the minimum stable rate of
flow achievable in the rig due to the variation in the reservoir tank liquid level over the duration of an experimental run.
4. The glass column was then observed to ensure that some liquid overflowed the outlet weir. If that was not the case, the air flow rate was gradually increased to achieve this overflow and subsequently fixed and recorded at this overflow occurrence. This procedure was necessary to keep away from the weep point.
5. The next step was to increase the air flow was used to values corresponding approximately to $35,50,60,70,86$ and $100 \mathrm{~m}^{3} / \mathrm{h}$ while maintaining the liquid flow are at $0.1 \mathrm{~m}^{3} / \mathrm{h}$. Hence, it was possible to decrease the value of the weeping fraction and/or increase the value of liquid flow over the outlet weir.
6. The procedure pointed out in points 2 and 5 above was repeated over for increasing in the liquid flow rate to the test tray; namely $0.1,0.14,0.18,0.22,0.26,0.3,0.34,0.38,0.46$ and $0.58 \mathrm{~m}^{3} / \mathrm{h}$ and measuring the clear liquid height and froth height for each change.

## DISCUSSIONS

Effect of weir load $\left(Q_{L} / L_{w}\right)$, clear liquid height $\left(h_{L}\right)$ and weir height $\left(h_{w}\right)$ on point efficiency (Ep)
Figure (3) shows the effect of changing liquid flow rate (weir load) on the point efficiency. The point efficiency appears increase with clear liquid height as shown in Figure (4), when the liquid flow rate increasing the liquid height increases over the tray deck which will increase the interfacial area and contact time and hence point efficiency.

Maximum values of point efficiency for 5 cm weir height $90 \%$ for liquid flow rate ranging between 5.8 to $7.32 \mathrm{~m}^{3} / \mathrm{s} \mathrm{m}$ and clear liquid height between 3.5 to 4 cm .

Point efficiency values appear in the same range for different weir height. The average values of point efficiencies versus weir height are summarized in Table (1) and appear improve slightly with weir height. This improvement of point efficiency is due to increasing of liquid height above the tray deck.

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Fig. (3)., The point efficiency versus weir Fig.(4)The point efficiency versus clear liquid height liquid load

The results of point efficiency versus liquid height are compared with Porter (1992) results, who worked on air-water system with 6.35 mm hole diameter, weir height $10,20,50 \mathrm{~mm}$ and liquid weir load from 0.00125 to $0.025 \mathrm{~m}^{3} / \mathrm{m} . \mathrm{s}$ and Prado (1987), who worked on the same system but with weir height $25.4,50.8,76.2 \mathrm{~mm}$ and liquid weir load from 0.0015 to $0.0028 \mathrm{~m}^{3} / \mathrm{m} . \mathrm{s}$ as shown in Figure (5) Comparison between the results obtained from Porter (1992), Prado (1987) and the present work shows good agreement.

Table (1)., Average values of point efficiency versus weir height

| Weir height, cm | Average point efficiency, \% |
| :---: | :---: |
| 3 | 83 |
| 4 | 85 |
| 5 | 89 |



Fig. (5). Comparison of various air-water systems and present work

## Effect of F-factor on tray point efficiency ( $\boldsymbol{E p}$ )

Bennett et al. (1997) correlation (equation (1)) was used to calculate the point efficiency which is shown that point efficiency increases with gas velocity (Reynolds number Re) as shown in Figure (6).

Large values of gas velocity through the perforation (large $R e$ ) yield higher interfacial area. As expected the ratio of $h_{L} / d_{H}$ plays a significant role and the efficiency increases with $h_{L} / d_{H}$ which is ranging between 2 to about 10, as shown in Figure (7).


Fig. (6)., The point efficiency versus Reynolds number Fig. (7), the point efficiency versus $h_{L} / d_{H}$
The above results (effect of weir load and gas velocity on point efficiency) are in good agreement with Bennett et al. (2000).

Bennett et : 2000) reported that the denominator of the term within the major bracket is the correction required en liquid phase resistance is important. No significant effect of changing the diffusivities of $\mathrm{CO}_{2}$ and $\mathrm{NH}_{3}$. This gives good evidence that the liquid phase resistance is not important.

## Predicted Murphree tray efficiency ( $E_{M V}$ )

The prediction of Murphree tray efficiency is done by using recently equation of Lopez and Castells (1999). This equation predicts the ratio of Murphree tray efficiency over point efficiency as function of Peclet's number $(P e) . P e$ for experimental data are calculated and ranged between 0.07 to 1.5.

Referring to equation (4); namely:

$$
\begin{equation*}
P e=\frac{Q_{L} Z_{o}^{2}}{A_{a} h_{L} D e} \tag{4}
\end{equation*}
$$

It is apparent that $h_{L}$ and $D e$ must be evaluated in order to establish the value of $P e$. Clear liquid height was used in equation 2.13 was determined experimentally for three weirs height $(3,4$, and 5 cm$)$,

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while the De correlation given by Bennett et al. (1997), being most recent in the literature was used in this study. Accordingly $D e$ values shown in appendix were obtained.

According to Lopez and Castells (1999) equation $E_{M V}$ is equal to $E p$ obtained from the experimental data as shown in Figure (8).


Fig. (8)., Murphree tray efficiency per point Efficiency versus Peclet number

## CONCLUSIONS

The following conclusions can be drawn from the results obtained:

1. Maximum calculated value of point efficiency for 5 cm weir height is $90 \%$ for liquid flow rate ranging between 5.8 to $7.32 \mathrm{~m}^{3} / \mathrm{s}$ and clear liquid height between 3.5 to 4 cm .
2. Point efficiency values are in the same range for different weir height, but it improves slightly with weir height and the average values of point efficiency are $83 \%$ for 3 cm weir height, $85 \%$ for 4 cm weir height and $89 \%$ for 5 cm weir height.
3. At large values of Reynolds number for gas phase, the point efficiency increases with $h_{L} / d_{H}$ in the range 2 to 10 to about $90 \%$.
4. Evaluation of liquid Peclet number by equation of Lopez and Castells (1999), shows that $P e$ ranged between 0.07 to 1.5 .
5. Prediction of Murphree efficiency by using Lopez and Castells (1999) equation shows that the ratio of $E_{M V} / E p$ is equal to 1 for all experimental data due to low value of liquid Peclet number.

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## NOMENCLATURE

| Symbol | Description | Units |
| :--- | :--- | :--- |


| $A_{a}$ | Active area | $\mathrm{m}^{2}$ |
| :---: | :--- | :---: |
| $A_{h}$ | Hole area | $\mathrm{m}^{2}$ |
| $C^{\prime}$ | Constant defined by equation 11 |  |
|  |  | m |
| $d_{H}$ | Hole diameter | $\mathrm{m}^{2} / \mathrm{s}$ |
| $D e$ | Eddy diffusivity for liquid mixing | $\mathrm{m}^{2} / \mathrm{s}$ |
| $D_{L}$ | Liquid molecular diffusivity | $\mathrm{m}^{2} / \mathrm{s}$ |
| $D_{V}$ | Vapor molecular diffusivity | - |
| $E_{M V}$ | Murphree gas-phase tray efficiency | - |
| $E$ or $E_{p}$ | Point efficiency | - |
| $E_{o}$ | Overall column efficiency | $\mathrm{m} / \mathrm{s}$ |
| $F$ | F factor = $V_{g h} \sqrt{\rho_{g}}$ | - |
| $F r_{G}$ | Gas Froude number defined in equation 14 | $\mathrm{~m} / \mathrm{s}^{2}$ |
| $g$ | Gravity acceleration | m |
| $h_{2 \Phi}$ | Two-phase layer height on the tray (sum of liquid continuous region |  |
|  | + gas continuous region) | m |
| $h_{F e}$ | Effective froth height | m |
| $h_{L}$ | Clear liquid height in the two phase layer on the tray | m |
| $h_{w}$ | Outlet weir height | $\mathrm{m} / \mathrm{s}$ |
| $K_{S}$ | Density corrected superficial gas velocity over active area $\left(=V_{g a}\left[\rho_{g} /\left(\begin{array}{l}\text { m }\end{array}\right.\right.\right.$ |  |


|  | $\left.\left.\rho_{L^{-}} \rho_{g}\right)^{1 / 2}\right]$ ) | m |
| :--- | :--- | ---: |
| $L_{w}$ | Weir length |  |
| $m$ | Slope of equilibrium line | - |
| $P e$ | Liquid Peclet number | $\mathrm{m}^{3} / \mathrm{s}$ |
| $Q_{g}$ | Volumetric gas flow rate | $\mathrm{m}^{3} / \mathrm{s}$ |
| $Q_{L}$ | Volumetric liquid flow rate | - |
| $R e$ | Reynolds number | $\mathrm{m} / \mathrm{s}$ |
| $V_{e j}$ | Gas velocity defined by equation 15 |  |
| $y_{y}^{*}$ | Gas concentration (mole fraction) |  |
| $y_{n}$ | Mole fraction that would be in the equilibrium with liquid leaving |  |
| $\bar{y}_{n}$ | Average mole fraction in the vapor leaving the tray | m |

## Greek Letters

$\eta \quad$ Defined by equation 6
$\Phi_{e} \quad$ Effective relative froth density as defined in equation 10

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## Subscripts

$0 \quad$ Evaluate at $\mathrm{z}=0$
1 Evaluate at $\mathrm{z}=1$
$g$ Gas
$h$ Hole
hor Horizontal
$L \quad$ Liquid
$w$ Weir

## Superscripts

## _ Mean value

* Equilibrium value if used with x or y


# EVOLUTIONARY ALGORITHMS FOR TRANSFERRING <br> PROPERTIES BETWEEN IMAGES PART I: GRAYSCALE IMAGE COLORIZATION 

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#### Abstract

In this paper, an evolutionary algorithm (EA) for "colorizing" grayscale images is introduced by evolving color patch transfer process between a source colored image and a target grayscale image. As the general problem of inverting a gray palette to a color palette is a severely under-constrained, ambiguous problem and has no exact, objective solution, human labor and costly semantic knowledge are required. The presented EA attempts to minimize the amount of human work by automatically choosing colored patches from the source image and applying their colors to the grayscale patches of the target image. Furthermore, the best patch matching over all EA parent individuals are recombined in a single multi-sexual recombination scheme to form a single offspring individual. Mutation, on the other hand, forms all other EA individuals. The simple technique of the proposed EA can be successfully and efficiently applied to a variety of images.


> الخوارزميات التطورية لنقل الصور الرمات بين الصـية الصور الجزء الأول:

الخلاصه

يهتم هذا البحث بأيجاد خوارزميات تطورية لحل مشكلة نقل الصفات بين الصور . في هذا الجز ع نقدم خوارزميـة
 المقترحة على نقل رقع من الألوان من الصورة المصدر الـى الصورة الهدف في آن واحد. يرجع سبب أختيارنـا

 بوساطة الأختيار الأتوماتيكي للرقع الملونة من الصورة المصدر ونقل الوان هذه الرقع الى الرقع الرماديـة للصـورة
 نتولى عملية الطفرة الور اثية نوليد بقية الأفراد للجيل الجديد. طبقت الخوارزمية المقترحة بنجاح وبكفاءة على أنواع مختلفة من الصور.

## KEYWORDS

Image colorization, genetic algorithm, multi-sexual crossover, color patch

## INTRODUCTION

Colorization is a useful technique in increasing the visual appeal of black-and-white photos, classic movies or scientific visualizations. Further, colorization has applications in color editing and compression. The problem of coloring a grayscale image involves assigning three-dimensional (RGB) pixel values from a source, color image to a target, grayscale image whose pixels are varied along only one dimension (luminance). As several hues and/or saturation levels may carry the same luminance value, colorization problem has no inherently correct solution. Moreover, it has several other challenges including ambiguity, fuzzy boundary identification, and user expert. [1] [2]. In other words, colorization is in general a severely under-constrained and ambiguous problem for which it makes no sense to try to find an "optimum" solution, and for which even the obtainment of "reasonable" solution requires some combination of strong prior knowledge about the scene depicted and decisive human intervention. Even in the case of pseudo coloring, where the mapping of luminance values to color values is automatic, the choice of the color map is commonly determined by human decision.

Several techniques are published for digital colorization. Readers please refer to recent papers. Some (but mostly used) colorization work are color transfer of Reinhard et al [3], image analogies of Hertzmann et al [4], the classical full search of Welsh et al [5], and the Antypole strategy of Di Blasi and Reforgiato [1]. The main concept of these colorization techniques is to exploits textural information. For example, the work of Welsh et al, which is inspired by the color transfer [3] and by image analogies [4], examines the luminance values in the neighborhood of each pixel in the target image and add to its luminance the chromatic information of a pixel from a source image with best neighborhoods matching. This technique works well on images were differently colored regions give rise to distinct textures. Otherwise, the user must specify rectangular swatches indicating corresponding regions in the two images. Di Blasi and Reforgiato [1] propose an improvement to Welsh et al work, where Antipole clustering strategy is adopted as an efficient data structure for fast color retrieving. Their approach provides a way to speed up the searching process but at the expense of increasing implementation complexity.

In this paper, the technique of evolutionary algorithms (EAs), probabilistic search algorithms based on the model of natural evolution will be applied, for colorization problem. The procedure of evolution works by minimizing the matching error (in term of luminance and texture information) between pairs of source and target square patches. Then transfer color mood from the best evolved source patches to the target patches. In what follow, the characteristic components of this EA will be presented.

## THE PROPOSED EVOLUTIONARY ALGORITHM

An Evolutionary Algorithm (EA) is inspired by biological evolution, and is widely believed to be an effective global optimization algorithm. There are a variety of evolutionary algorithms emerged:"evolutionary programming-EP" [6], "evolution strategies-ESs" [7] and "genetic algorithmsGAs" [8]. Moreover, since EAs are motivated by natural principles, when faced with problem, natural remedies are often emulated.

An EA consists of a population of individuals, which are evaluated using fitness function. The individuals (mostly fittest individuals) are reproduced and perturbed via three main EA's operators: selection, recombination, and mutation. The processes used to select which parents will produce
offspring varies significantly from one EA to another, and includes strategies such as uniform random selection, rank-proportional selection, and fitness-proportional selection. In addition to these selection processes, the mechanisms used for offspring reproduction also varies. They range from asexual reproduction with no mutation (in which offspring are exact replicas of parents), asexual reproduction with mutation, to sexual reproduction with recombination. Moreover, sexual reproduction can be in either local form with 2-parent recombination or global form with multi-parent recombination. Historically, the EP and ES communities have emphasizes asexual reproduction while the GA community has emphasized sexual reproduction.

In the proposed EA, square patches of pre-selected size- $w_{p} \times w_{p}$ - of the target, grayscale image are colorized from suitable $w_{p} \times w_{p}$ source patches. The evolution of the patch colorization scheme is manipulated by formulating individual representation, penalty function, and individual evolution via perturbation operators.

## Search space representation

In order to apply an EA to a particular problem, it is appropriate to select an internal representation of the space to be searched and define an external evaluation function, which assign utility to candidate solutions. Both components are critical to the successful application of the EA to the problem of interest. Here, to represent a solution (an individual's genotype), a two-dimensional array of $m \times n$ genes is used such that:
$m=h_{t} / w_{p}$, and
$n=w_{t} / w_{p}$
Where
$h_{t}$ : Height of the target grayscale image,
$w_{t}$ : Width of the target grayscale image, and
$w_{p}$ : Patch width (e.g., we use $w_{p}=3,5,7,9$, or 11).
Gene $(i, j)$ of an individual identifies an un-overlapped $w_{p} \times w_{p}$ target patch $(i, j)$ and can contain $x$ and $y$ coordinates of the center of a $w_{p} \times w_{p}$ source patch. To start the EA, a population of $p_{\text {size }}$ individuals is randomly created, and each individual can represent the genotype of a potential solution to the colorization problem.

The total number of possible solutions represents the search space size (which here, grows exponentially as increasing the number of un-overlapped source patches).

## Penalty function

Next, it is important to define a suitable penalty function which rewards the right kinds of individuals. For the colorization problem reported here, it would be desirable to minimize luminance matching error between pairs of target patches and source patches. In other words, each gene $(i, j)$ in an EA individual has associated with it a luminance matching error $(i, j)$ computed as:
$\operatorname{error}(i, j)=\operatorname{match}\left(p_{t}(i, j), p_{s}(i, j)\right)$
Where:
$p_{t}(i, j)$ : Target patch being identified by the gene $(i, j) ;$
$p_{S}(i, j)$ : Source patch referred to by the gene $(i, j)$;
and the match between two patches $p_{t}$ and $p_{S}$ of a given gene $(i, j)$ is defined to be:
$0.5 \mu_{s}(i, j)-\mu_{t}(i, j)|+0.5| \sigma_{s}(i, j)-\sigma_{t}(i, j) \mid$
Where $\mu$ and $\sigma$ are the luminance average and standard deviation both taken with respect to a $w_{p} \times w_{p}$ source or target patch as referred to by subscript $s$ or $t$ respectively. Then, an EA individual has a penalty function $E$ computed as the sum of all its gene luminance matching errors:
$E=\sum_{i=1}^{m} \sum_{j=1}^{n} \operatorname{error}(i, j)$
In order to match luminance information, both source and target images must be converted from RGB color space to a de-correlated space (de-correlated YIQ color space is used here).

## Evolutionary operators

In our EA, we breakdown the traditional views found in the EA communities and make a hybrid collection of evolutionary processes that would be useful for the colorization problem. The main issues made in the proposed EA are: extinctive selection, single multi-sexual discrete recombination, and preservative mutation operator.

The first character of the proposed EA is the strict denial of selection process; letting all offspring to be created from all parents using recombination and mutation. First a multi-sexual discrete recombination process is applied among all parents to produce only one mated offspring. Genes among all parents are competed and the best ones (with smallest matching errors) are inherited to that offspring.

Next, mutation is used to fulfill the new population with $p_{\text {size }}-1$ new offspring. $90 \%$ offspring are created by mutating the genes of the mated offspring while others $10 \%$ offspring are created randomly from the total search space.

## Genotype decoding: phenotype re-coloring

After stopping the EA to a pre-selected maximum number of generations, a population of individuals that may have some promising solutions is obtained. The best individual (with smallest $E$ ) has to be decoded to its colored result. In EA literatures, the output of the genotype decoding is normally known as phenotype. Here, phenotype coloring includes the following sequence of steps:

1. Go through the best EA individual genes and the target image in scan-line order in steps of one gene (for the individual) and one $w_{p} \times w_{p}$ patch (for the target image).
2. Select from the source image a $w_{p} \times w_{p}$ patch in which its center has coordinates $x$ and $y$ referred to by the current gene.
3. For each pixel in the target patch, search the selected source patch in scan-line order for the closest pixel (in term of luminance value). Add the chromatic components ( $I$ and $Q$ ) of that pixel to the luminance value of the current target pixel.
4. Repeat the sequence 1,2 , and 3 for all target patches.
5. Transform the target image from YIQ to $R G B$ color space to display the result on the screen.

## EXPERIMENTAL RESULTS

This section reports some results obtained by running the proposed EA with $p_{\text {size }}=40$ to a maximum number of generations equals to 30 for coloring a range of image domains with different sizes. Generally, the experimented images are classified as homogeneous ones. These images include
a single object in the foreground and this object is clearly discernible from a mostly homogeneous background. First, (if needed) luminance histogram matching of Hertzmann et al [4] is applied to match the first- and second- order statistics of the luminance distribution of the source image according these of the target image. More concretely, if $l(p)$ is the luminance of a pixel in the source image, then we remap it as
$l(p)^{\prime}=\frac{\sigma_{t}}{\sigma_{s}}\left(l(p)-\mu_{s}\right)+\mu_{t}$
EA results are compared with the Welsh et al classical full search method [5] (both are implemented using un-optimized visual Basic code.) The neighborhood statistics required in both algorithms are pre-computed over the source and target images. In the full search method, we need to pre-compute neighborhood average and standard deviation of each pixel, while in the EA; the statistics are needed for each un-overlapped patch. Different patch size was used. Obviously, decreasing patch size results in more acceptable results but at the expense of increasing maximum required number of generations. Each EA result is formulated by depicting the phenotype of the best individual obtained after only 30 generations together with the result of the full search algorithm (see figures 1 and 2). Quantitative EA results are also pointed out by including average of penalty function $(E / m * n)$ of the best individual in the initial and the last generations. Processing time required for a single Pentium IV PC computer is also included for both colorization algorithms (see table 1). Actually, EA algorithm requires less computation time than presented in the table. By comparing EA results with those of Welsh et al, we can easily demonstrate that the proposed easy to implement EA can produce visually accepted results in a number of image domains although there are some failure (yet tolerable) patch colorization cases. Running time will vary depending on the patch size, size of source and target images (total search space size), $p_{\text {size }}$ and the maximum number of generations. In most of experimented results, the computation time of EA colorization algorithm to obtain visually accepted results was better than the classical full search algorithm of Welsh et al.

## CONCLUSIONS

This paper introduces a simple colorization technique based on combing the concept of evolutionary algorithms with a patch-based luminance matching strategy. A new multi-sexual recombination strategy is given to recombine, in a single EA step, the best patches found between source color and target gray images. Without user expert, the algorithm can give pleasing visual results for homogenous images. Both EA and patch-based luminance matching could be the subject of future research. For example, try to test this colorization algorithm on more complicated images, i.e. heterogeneous images where the scene has multiple objects on the foreground, or has a cluttered background, or is illuminated in an uneven way.

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Table (1). Mean of penalty and processing time comparison between EA and full search.

$\left.$| Target <br> image | gen. <br> no.0 |  | gen. <br> no.30 | EA |
| :---: | :---: | :---: | :---: | :---: | | Full |
| :---: |
| search | \right\rvert\,

# EFFECTS OF NON-LINEAR MAGNETIC CHARGE ON INDUCTION FURNACE OPERATION DURING THE HEATING CYCLE 

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خلاصة
أن هذا البحث هو عبارة عن دراسة لسلوك المجال الكهرومغناطيسي للفرن الحثي عندما يكون قلبه مادة مغناطيسية اخذين بنظر الاعتبار العلاقة اللاخطية لكثافة الفيض المغناطيسي B المتولد في القلب الحديدي للفرن كداله للثندة المغناطيسية H المسلطة على ملفاته. بما أن كلا من الخواص ألمغناطيسيه للقلب الحديدي ومقاومته النو عية تتأثزان بشدة بارنفاع الحرارة فأن الدراسة تضمنت تأثنير الحرارة على كلا العاملين آنيا لنوضيح السلوك الكهرومغناطيسي للفرن خلال عملية التنخين. أن نوزيع كل من كثافة التيار و كثافة الفيض و شدة المجال المغناطبسي داخل القلب الحديدي و على سطحه الخارجي قد تم تحديدها. وكذلك فأن توزيع الفيض المغناطيسي قد تم رسمه للارجات حرارة مختلفة. أن هذه الار اسة قد أظهرت أهمية تضمين اللاخطية المغناطيسية وتأثرّز ها بالحر ارة في در اسة الأفر ان الحثية لذا، فأنها سنكون كأساس للعمل المستقبلي الذي سيتضمن التعشيق بين التحليالت الحرارية و الكهرو مغناطيسية لهذه الأفران.
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#### Abstract

This research studying the electromagnetic behavior of the induction furnace when its core is a magnetic material taking into consideration the effect of the non-linear dependence of the magnetic flux induced in it due to the applied magnetizing force.

Since the magnetic characteristics are severely affected by temperature rise in a non-linear way, so as the specific electric resistance of the charge material, this work deals with studying the effect of temperature on the non-linear characteristics of a magnetic core simultaneously with that on the specific electric resistance to show the electromagnetic behavior of the furnace during heating operation. The distribution of the current density, flux density and the magnetizing force at different temperatures inside the furnace and on the charge surfaces are determined for different temperatures. Also the flux distribution is plotted at these cases. This study will be the base for future work on the electromagnetic-thermal coupled analysis for the induction furnace.


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A. H. Ahmad

\section*{INTRODUCTION}

This work represents the second step of analyzing the electromagnetic behavior of the induction furnace when its core is a ferromagnetic material. The results of the first step analysis have already been published and presented on a linear induction furnace \({ }^{[1]}\) using a FEM package (ANSYS 5.4). In this work the analysis is extended to take into consideration the effect of three types of non-linear relations on the furnace parameters these are:
a) The effect of the non-linearity of the permeability \(\mu\) with the magnetic field intensity \(H\), or \(B=\mu(H) \cdot H\).
b) The non-linear effect of the temperature \(T\) on the permeability \(\mu(T, H)\).
c) The non-linear variation of the specific electric resistance of the charge material with temperature \(\rho(T)\).
The new analysis was done using numerical technique based on a general-purpose finite element package "ANSYS 7". Two previous applications \({ }^{[2]}\) are considered in order to verify the results of this work. The first example is an induction furnace with magnetic core and operating at low frequency of 60 Hz , while the second furnace using the same material as a core operating at medium frequency of 4 KHz . The results obtained by ANSYS 7 show a good agreement with the published work. The magnetic material used is a carbon steel SAE 1045 (C45). The data of steel C45 are extracted from references [2], [3] \& [4].

It is very interesting in this work to show clearly what is going on inside the magnetic charge of the induction furnace during its operation by studying the effect of temperature increase on the distribution of flux lines, \(B, H \& J\) (from room temperature up to Curie temperature). Such knowledge will lead to expect the effect of non-linearity and temperature increase on Skin depth \(\delta=1 / \sqrt{\omega \mu \sigma}\). Also, it is an important step to prepare for the electromagnetic-thermal coupled analysis, which will complete the simulation of the induction heating process to be as real as possible.

\section*{The Magnetic Non-linearity Problem:}

When the magnetic non-linearity is considered, the conventional transient analysis method will elapse a long time to solve such problem. In FEM, harmonic analysis assumes that all quantities are sinusoidally varying, but if a sinusoidal exciting field \(H\) is used, non-linearity distorts the waveforms of the flux density \(B\), while considering sinusoidal \(B\) will lead to a non-sinusoidal \(H\). Therefore, non-linearity cannot be included in the analysis directly and iron saturation requires special treatment. Hence, Several methods \({ }^{[5-9]}\) for determining appropriate permeability have been used to make account of time variation. These methods include the use of time-averaged value of the permeability over a complete cycle. The problem can then be simplified by considering only the fundamental frequency component of \(B\) and \(H\). The problem, in this case, is cast in time harmonic form with \((d / d t)\) being replaced by \((j \varpi)\). The package " ANSYS 7 " deals with this problem to investigate the accurate results \({ }^{[10]}\).

Accurate data for carbon steel SAE 1045 (C45) about the dependence of its relative magnetic permeability on temperature are not readily available but it could be approximated as \({ }^{[4]}\)
\[
\begin{array}{lll}
\mu_{r}(T, H)=1+\left(\mu_{r}(H)_{T=0}-1\right) \cdot\left[1-\left(T \cdot 750^{-1}\right)^{2}\right] & \text { when } \quad T<750^{\circ} \mathrm{C} \\
\mu_{r}(T, H)=1 & \text { when } \quad T \geq 750^{\circ} \mathrm{C}
\end{array}
\]

The family of curves of \(B(T, H)\) is shown in Fig. (1) for steel C45, This figure


Fig. (1) The Magnetic Characteristics (B-H curves) for Steel C45 at different temperatures

Shows that Curie-temperature for this kind of steel is \(750^{\circ} \mathrm{C}\), so the characteristics at that degree is linear and \(\mu_{r}=1\).

It is already known that the specific electric resistance of conducting materials is a function of temperature; hence, this factor should be included in this analysis in order to make the simulation as real as possible. Fig. (2) represents \(\rho(T)\), the specific electric resistance or the resistively of the carbon steel C45 as a function of temperature \({ }^{[3]}\).
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Fig. (2). the electrical resistively of steel C 45 as a function of temperature

\section*{SIMULATION RESULTS}

\section*{a - Effect of non-linear magnetic charge}

As mentioned before two examples have been applied to verify the present results. The first example for a low frequency furnace of 60 Hz Its data shown in table (1) .

Table (1)
\begin{tabular}{|l|l|}
\hline Coil inner diameter \((\mathrm{m})\) & 0.08256 \\
\hline Coil length \((\mathrm{m})\) & 0.254 \\
\hline Number of turns & 29.5 \\
\hline Frequency \((\mathrm{Hz})\) & 60 \\
\hline Charge material & Steel SAE1045 (C45) \\
\hline Charge diameter \((\mathrm{m})\) & 0.06032 \\
\hline Charge length \((\mathrm{m})\) & 0.254 \\
\hline Charge conductivity \((\mathrm{mho} / \mathrm{m})\) & 5 E 6 \\
\hline Relative Permeability & 18 \\
\hline
\end{tabular}

In this example two solutions are obtained, (applying constant current density source), the first solution is done assuming linear magnetic material with \(\mu_{r}=18\), and in the second solution the (B-H) non-linear relation at \(\left(T=0^{\circ} C\right)\) as shown in Fig. (1) is considered. The finite element model of the furnace under consideration is shown in Fig. (3). The distribution of the normalized value of the current density magnitude \(J_{n}=|J| /\left|J_{\text {suff }}\right|\) on charge mid-plane is drawn as a function of normalized charge radius for the linear and non-linear case is shown in Fig. (4). The results show that the current density distribution
for the ANSYS and that of reference[2] are exactly the same, while, there is a difference in a nonlinear case, because they consider the non-linearity in different ways. The power loss in each case is calculated and the "Non-Linear Factor" NLF is about 1.524. Where, NLF is the ratio of the power loss inside the core in the non-linear case to that of the linear one. This computed value of NLF is about \(5.4 \%\) more than Boden's experimental value of this factor that has been found to be \(1.47^{[11]}\).


Fig. (3). Quarter of the longitudinal section in the finite element model of the furnace.
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Fig. (4) Distribution of normalized current density magnitude for linear and non-linear cases for a 60 Hz furnace

The second example is for the medium frequency range furnace with the data shown in table (2). The same graph is drawn as that for example (1), given in Fig. (5). The results show reasonable agreement with that of reference[2]. The NLF in this case is calculated to be 1.266 , which is \(20.4 \%\) less than Boden's value. The obtained results verifies the method used by ANSYS 7 to treat the non-linearity of the magnetic circuit.

Table (2)
\begin{tabular}{|l|l|}
\hline Coil inner diameter \((\mathrm{m})\) & 0.0412 \\
\hline Coil length \((\mathrm{m})\) & 0.5842 \\
\hline Number of turns & 61 \\
\hline Frequency \((\mathrm{Hz})\) & 4000 \\
\hline Charge material & Steel SAE1045 (C45) \\
\hline Charge diameter \((\mathrm{m})\) & 0.0254 \\
\hline Charge length \((\mathrm{m})\) & 0.5842 \\
\hline Charge conductivity \((\mathrm{mho} / \mathrm{m})\) & 4.878 E 6 \\
\hline Relative permeability & 88 \\
\hline
\end{tabular}


Fig. (5) Distribution of normalized current density magnitude for linear and non-linear case for a 4000 Hz furnace

\section*{b- Effect of temperature increase}

In order to study the electromagnetic parameters during the temperature increase inside the furnace, five different temperatures are assumed for the furnace under test, these are \(\left(0.0^{\circ} \mathrm{C}, 250^{\circ} \mathrm{C}, 450^{\circ} \mathrm{C}, 650^{\circ} \mathrm{C}, \& 750^{\circ} \mathrm{C}\right)\). The ( 60 Hz ) furnace of example (1), is analyzed at these temperatures. This analysis done on the low frequency furnace only, because, in such a kind of furnaces the heat distribution inside the core seems to be approximately uniform, so, the results will give the most logical descriptions can be obtained for the given temperature. While, this assumption is quiet wrong in the medium frequency furnaces due to the sever skin effect in such frequencies, which leads to nonuniform distribution of the temperature inside the core. The magnitudes of \(H, B\), and \(J\) for three different positions in the charge, (the mid-plane, the external side surface and the top surface) for each temperature are calculated and plotted as shown in Fig. (6.a.b.c), (7.a.b.c), \& (8.a.b.c.) respectively.
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(6-a)

(6-b)

(6-c)
Fig. (6-a, b, c) Distribution of \(|H|,|B|\), and \(|J|\) as a function of the core radius in the mid-plane of the core for different temperatures
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(7-a)

(7-b)

(7-c)
Fig. (7-a,b,c) Distribution of \(|H|,|B|\),and \(|J|\) at the external side surface for different temperatures

(8-a)
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(8-b)

(8-c)
Fig. (8-a, b, c) Distribution of $|H|,|B|$, and $|J|$ as a function of the core radius in the mid-plane of the core for different temperatures

## DISCUSSION

This paper declares the effect of the non-linearity in the (B-H) curve of the magnetic charge of the furnace on the flux distribution and on other parameters like $J, B, \& H$. The results obtained seems to be quite reasonable, and agrees with that
published to deal with non-linearity at room temperature only. Two kinds of furnaces are used for verification of the work, low frequency, and medium frequency one. The analysis extended to deal with other temperatures taking into consideration the effect of temperature increase on the permeability and the electrical resistivity of the steel charge

The results obtained in the first part of this research show that the power delivered to the charge is more than that calculated by the linear analysis, because NLF is always more than one. Also, it is clear that the skin depth is less than that in the linear case, while the eddy current magnitude increases especially behind the side external surface of the charge.

When the effect of temperature increase studied, the results show that the flux density reduced as the temperature increased due to the associative reduction in the permeability and the magnetizing force increased. This is quite reasonable because the magnetizing force is severely opposed by the flux generated due to the induced eddy currents, but, when the permeability reduced, the induced eddy currents reduced too leading to reduce the reduction of the magnetizing force. But the magnetizing force is constant since the input current to the coil from the power supply is constant, so the resultant $H$ will increase with the reduction of the permeability, which is the case here. Also, as a result of eddy current reduction, the distribution of the magnetic intensity $H$ will be approximately uniform everywhere inside the core when Curie temperature reached. This will lead to the conclusion that, the power losses due to eddy currents will be reduced with the increase of charge temperature

The flux distribution for each temperature is shown in Fig. (9) inside and outside the furnace. It is clear that the density of flux lines increased near the side surface of the charge at $\left(\mathrm{T}=0.0^{\circ} \mathrm{C}\right)$, and it tends to be approximately uniform at Curie temperature.

## Conclusion and Future Work

The results show that the permeability of the charge material is the dominant parameter due to its sever effect on the distribution of $J, B, \& H$, and the depth of penetration of the power inside the charge, is a function of temperature also during the heating cycle (for constant frequency).

It is very obvious that the distribution of $B, H, \& J$ is approximately uniform inside the core at Curie temperature. This study prepares to complete the simulation of the induction furnace using the FEM in that it helps to expect the furnace behavior during the heating process. In order to reach the most real study of the furnace, an electromagnetic-thermal coupled analysis should be done considering $\mu(T, H) \& \rho(T)$ simultaneously and continuously for each element inside the FE model during the increases in temperature of the furnace. Such a study will be the aim of the authors in future.

From the power supply point of view, it is clear that the furnace is a non-linear load. Hence an electromagnetic-thermal coupled analysis will lead to calculate the variation in load impedance during operation and this will help very much to expect the design parameters of the power supply needed for certain load.
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$\mathrm{T}=\mathbf{0 . 0}{ }^{\circ} \mathrm{C}$
$\mathrm{T}=\mathbf{2 5 0}{ }^{\circ} \mathrm{C}$


## $\mathrm{T}=450^{\circ} \mathrm{C}$



Fig. (9)
The distribution of flux during operation at different temperatures
$\mathrm{T}=750^{\circ} \mathrm{C}$
$B \quad$ : Magnetic flux density
$H$ : Magnetic field intensity
I : Current
$J$ : Current density
$T$ : Temperature.
$\mu \quad:$ The permeability
$\mu_{r} \quad:$ The relative permeability.
$\delta \quad:$ The Skin depth
$\rho \quad:$ The resistivity
$\sigma \quad$ : The conductivity
$\varpi \quad$ : The angular Frequency

Tesla.
Amp.m ${ }^{-1}$.
Amp.
Amp.m ${ }^{-2}$.
${ }^{o} C$
Henry. ${ }^{-1}$.
m
$\Omega . \mathrm{m}$.
( $\Omega . \mathrm{m})^{-1}$.
Rad. Sec ${ }^{-1}$

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# DESIGN AND IMPLEMENTATION OF A TRANSPARENT SECURE LAN 

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#### Abstract

Many attacks may be carried out against communications in Local Area Networks (LANs). However, these attacks can be prevented, or detected, by providing confidentiality, authentication, and data integrity security services to the exchanged data.

This paper introduces a security system that protects a LAN from security attacks. On each host in the protected LAN, the security system transparently intercepts each outbound IP (Internet Protocol) packet, and inserts a crypto header between the packet IP header and payload. This header is used to detect any modification to the content of the packet in transit, and to detect replayed packets. Then, the system encrypts the IP packet payload and some fields of the inserted crypto header. On the other hand, the system transparently intercepts each inbound IP packet, decrypts its encrypted portions, and then uses its crypto header to authenticate the packet. If the packet is properly authenticated, the system indicates it to upper protocols.

To be transparent to applications, the security system part that processes inbound and outbound IP packets was implemented as a NDIS (Network Driver Interface Specification) intermediate driver that resides between the LLC (Logical Link Control) and MAC (Medium Access Control) data link sublayers.


## الخلاصة

هنالكك العديد من الهجمات التي يمكن تتفيذها ضد اتصالات الثبكات المحلية (LANs). ألا أنه بالأككان منع أو اكتثشاف هذه
الهجمات عن طريق توفير السرية للمعلومات المتبادلة، و التأكد من سلامتها و صدق مصدر ها.

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يقترح هذا البحث نظاما أمنيا يمكن استعماله لحماية شبكة محلية من الهجمات التي قد تستهف أمنها. في كل حاسبة مرتبطة
بالثبكة المحمية، يقوم النظام الأمني المقترح بمقاطعة مسار كل رزمة خارجة من نوع IP packet بصورة شفافة، ثم يقوم
بادخال معلومات أمنية (crypto header) بين الـ IP header و الــ IP payload ورّ تستعطل هذه المعلومات لكثف أي تغيير
لدحنويات الرزمة أثنثاء تتقلها، و لكثف الرزم التي أعيد بثها. بعد ذلك، يقوم النظام بتشفير الــ IP Payload، و بعض الأجزاء
من المعلومات الأمنية المضافة. من جهة أخرى، يقوم النظام بمقاطعة مسار كل رزمة داخلة الى الحاسبة بصورة شفافة، ثم يقوم
بفتح تشفير الأجز اء المشفرة منها. بعد ذلك، يفصص النظام المعلومات الأمنية الموجودة في الرزمة المُستلمة للتأكد من صدق و
                        سلامة معلوماتها. فأذا كانت الرزمة سليمة، يقوم النظام بتسليمها الى البروتوكو لات العليا.
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لكي يكون النظام المقترح شفافاً للتطبيقات العليا، فأن ذلك الجزء من النظام الذي يعامل الرزم الخارجة و الداخلة تم تففيذه
    كسو اقة (NDIS intermediate driver)، و التي نقع بين طبقتي الـ LLC : data link layer و MAC.
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## KEYWORDS

LAN, security, encryption, authentication, transparent, NDIS intermediate driver

| ABBREVIATIONS |  |
| :--- | :--- |
| API: | Application Programming Interface |
| CIMD: | Cryptographic Intermediate Miniport Driver |
| DDK: | Driver Development Kit |
| DIX: | Digital equipment Intel Xerox |
| DoS: | Denial of Service |
| ESP: | Encapsulating Security Payload |
| GUI: | Graphical User Interface |
| ICMP: | Internet Control Message Protocol |
| IETF: | Internet Engineering Task Force |
| IM: | Intermediate Miniport |
| IP: | Internet Protocol |
| IPX/SPX: | Internet Packet Exchange/ Sequenced Packet Exchange |
| IV: | Initialization Vector |
| LAN: | Local Area Network |
| LLC: | Logical Link Control |
| LSP: | Layered Service Provider |
| MAC: | Medium Access Control |
| MAC: | Message Authentication Code |
| MD: | Message Digest |
| MTU: | Maximum Transmission Unit |
| NDIS: | Network Driver Interface Specification |
| NIC: | Network Interface Card |
| OSI: | Open Systems Interconnection |
| PMTU: | Path Maximum Transmission Unit |
| SDL: | Security Descriptors List |
| SHA: | Secure Hash Algorithm |
| SSM: | Security System Manager |
| TCP/IP: | Transport Control Protocol/ Internet Protocol |
| TDI: | Transport Driver Interface |
| WLAN: | Wireless LAN |

## INTRODUCTION

Networks have become indispensable for conducting business in government, commercial, and academic organizations. Networked systems allow people to access needed information rapidly, improve communications while reducing their cost, collaborate with partners, provide better customer services, and conduct electronic commerce. While computer networks revolutionize the way people do business, the risks they introduce can be fatal to a business. Attacks on networks can lead to lost money, time, products, reputation, sensitive information, and even lives [ALL01].

The problem of network security is a very complex issue. By definition, network security means a protection of the network assets from different kinds of threats in the network by implementation of different security services using various security mechanisms [TRC99].

The above definition introduces the following three aspects of network security [STA99]:

- Security Attack: Any action that compromises the security of information, such as eavesdropping, masquerading, replay attacks, Denial of Service (DoS) attacks, and active change to the exchanged information.
- Security Service: A service that enhances the security of data processing systems and information transfers. It is intended to counter security attacks. A security service makes use of one or more security mechanisms. The most important security services are confidentiality, integrity, and authentication.
- Security Mechanism: A mechanism that is designed to detect, prevent, or recover from a security attack. Encryption is the security mechanism that can be used to provide confidentiality, whereas hash functions or Message Authentication Codes (MACs) can be used in different ways to provide authentication and data integrity.

Some important insights in the literature concerning the subject of network security are summarized as follows:

- IPSec (IP Security) is a subset of IPv6 and a set of extension to IPv4. It has been developed by the Internet Engineering Task Force (IETF) to provide secure packet transmission over networks.
- A. Ganz, S. H. Park, and Z. Ganz [GAN00] had developed a security broker for Wireless LANs (WLANs). This system implements a number of security services such as authentication and realtime encryption/decryption for the communications in WLANs. The real time encryption/decryption service is implemented as a Layered Service Provider (LSP), and uses Microsoft's CryptoAPI. The use of a LSP allows a Trojan horse, or a worm to directly call the kernel-mode TCP/IP (Transport Control Protocol/ Internet Protocol) driver via the Transport Driver Interface (TDI), and completely bypass the provided security processing.
- The CIPRESS [RAD01] (Cryptographic Intellectual Property Rights Enforcement SyStem) from Mitsubishi Corporation and Fraunhofer-IGD was an attempt for providing transparent network access control, auditing, and encryption on the Microsoft Windows NT platform. CIPRESS provides these services by enforcing an automatic security policy that was implemented using LSP technique. However, CIPRESS supports only complete files, and does not support streaming data.
- B. S. Shaker [SHA02], Al-Nahrain University developed in 2002 an on-line end-to-end cryptography software system for LANs. An NDIS intermediate driver was used to process sent IP packets, and encrypt each IP packet payload using MARS algorithm if its upper protocol is TCP, whereas decryption of received packets was performed at the IP filter hook driver. While encrypting exchanged TCP data provides confidentiality, and some degree of data integrity (depending on encrypted TCP checksum), this system does not protect networks against masquerading because it does not authenticate the source of received packets. Moreover, replay attacks can be launched freely and successfully against the hosts that use this system. On the other hand, the use of IP filter hook driver for decryption instead of the used NDIS intermediate driver unnecessarily introduces additional processing overhead.

The purpose of this paper is to introduce the design of a security system that can be used to provide confidentiality, authentication, and integrity to the data exchanged within a LAN, so that attacks against the exchanged data are prevented (or detected). The security system provides the security services transparently, i.e. there is no need to change software on a user computer that benefits from the provided security services. Users can continue to use their usual network applications (without any change) while the security system provides security services to the exchanged data.

## SYSTEM SPECIFICATIONS AND DESIGN APPROACH

The following points shed the light on the specifications of the proposed security system:

- The security system provides confidentiality to the exchanged data.
- The security system provides authentication and integrity to the exchanged data.
- The security system provides access control.
- If received data is not properly authenticated or if it is replayed data, the security system collects audit information from it, and produces an alert to the network security administrator indicating the reception of such invalid data along with the collected audit information. In turn, the network security administrator could monitor the audit information, and take an appropriate action to prevent a possible attack that might cause the reception of the unauthenticated or replayed data.
- The security system is able to prevent DoS attacks launched by hosts unknown to the system.
- The security system is transparent to applications.
- The security system does not affect the work of routers that may exist in the protected network.
- The security system is able to protect itself from attacks.
- Due to the rapid increase of networks, many people who are not so experienced in network security have become network administrators. For this reason, the security system provides a friendly and easy to use interface for them.

To achieve the features and specifications stated above, the following choices were adopted:

- Microsoft Windows 2000 was chosen as the platform under which the proposed security system works, for of its reliability, high performance, and security.
- TCP/IP protocol was chosen as the transport protocol for the protected LAN.
- The LAN protected by the proposed security system was chosen to be Fast Ethernet. The security system assumes that Ethernet frames encapsulate IP packets according to the Ethernet II (DIX Ethernet) encoding, because by default, Microsoft Windows 2000 TCP/IP stack transmits Ethernet frames using this encoding [MAC00].
- The NDIS Intermediate Miniport (IM) driver was chosen to apply the required transparent security processing to inbound and outbound network traffic. NDIS IM driver was chosen for the following reasons:
1- It is well documented.
2- It is a kernel mode driver, and all incoming or outgoing packets should pass through this driver. This feature prevents network packets from bypassing the security policy enforced by the security system.
3- The NDIS IM driver lies below the network layer (between the LLC and MAC data link sublayers [DDK00]). This feature gives NDIS IM drivers a lot of control over network packets, without affecting other network protocol stack components. As an example, the position of NDIS IM drivers make them appropriate to be used to authenticate the source IP address of received IP packets.

The transparent security processing performed by the security system NDIS IM driver mostly follows the way in which the IPSec protocol processes network packets, but it avoids some problems that exist in the IPSec design. These problems are:
1- IPSec is too complex to be secure. The design obviously tries to support many different situations with different options. The number of major modes of operation can be drastically reduced without significant loss of functionality. IPSec is well beyond the level of complexity that can be
analyzed or properly implemented with current methodologies. Thus, no IPSec system will achieve the goal of providing a high level of security [SCH99].
2- The ESP (Encapsulating Security Payload) protocol allows the payload to be encrypted without being authenticated. In virtually all cases, encryption without authentication is not useful. ESP should be modified to always provide authentication; only encryption should be optional [SCH99].
3- When both encryption and authentication are provided, IPsec performs the encryption first, and then authenticates the ciphertext. This is the wrong because going by the "Horton principle", the protocol should authenticate what was meant, not what was said. The meaning of the ciphertext still depends on the decryption key used. Authentication should thus be applied to the plaintext, and not to the ciphertext [SCH99].
4- The specifications of IPSec allow predictable -but random- Initialization Vectors (IVs) to be used in IPsec ESP encryption, and explicitly allow the common practice of using the last ciphertext block of encrypted data from an encryption process as the IV for the next encryption process. Predictable initialization vectors compromise IPsec confidentiality. By using an adaptive chosen plaintext attack, an attacker can break low entropy plaintext blocks using brute force, and confirm guesses of the contents of arbitrary plaintext blocks. However, the preconditions of this attack are restrictive, and the vulnerability is thus difficult, but probably not impossible, to exploit in practice [NUO02].
5- Since IPSec is used to secure IP packets only, packets of transport protocols other than TCP/IP (IPX/SPX -Internet Packet Exchange/ Sequenced Packet Exchange- for instance) are not affected by the processing of IPSec. Hence, the packets of these protocols can still be used to launch attacks against a network, if they are installed on the hosts of that network, even if IPSec is deployed.

The developed security system avoids the complexity and many modes of operation inherent in the IPSec protocol, it always provides authentication and encryption for IP packets, it authenticates the plaintext instead of the ciphertext, it uses a random IV for each IP packet, and it prevents communications using transport protocols other than the TCP/IP protocol (the security system can be improved to secure the packets of these transport protocols instead of blocking them). However, the security system implemented now does not provide automatic key exchange, and this can be considered as a future work.

## SECURITY SYSTEM ARCHITECTURE AND COMPONENTS

The security system consists mainly of the following three components:
1- The Security Descriptors List (SDL), which stores security descriptors corresponding to hosts in the protected network.
2- The Security System Manager (SSM), which is a Win32 application that allows the network security administrator to control the operation of the CIMD, and alerts him (or her) if a suspicious packet is received.
3- The Cryptographic IM Driver (CIMD) that applies the transparent security processing to inbound and outbound IP packets.

Fig.( 1 illustrates the security system architecture and the interaction among its components. The following subsections introduce these components in more details.

## The Security Descriptors List (SDL)

The SDL stores security descriptors corresponding to hosts in the protected network. In other words, the SDL is essentially a list of the IP addresses of other hosts in the protected network, and their security parameters. If the network security administrator wants to enable communication with a certain host, he (or she) must specify a security descriptor corresponding to that host. This security descriptor is used by the security system to process packets exchanged with that host. The security policy enforced by the security system blocks all inbound and outbound packets exchanged with a host, if the SDL does not contain a security descriptor corresponding to that host.

The security system stores the SDL in the Windows 2000 Registry encrypted with a master key, so that it is inaccessible to unauthorized users. Moreover, choosing the Registry to store the SDL prevents non-administrator users from modifying the contents of the SDL.


Fig.( 1). Security System Architecture

Each security descriptor consists of the following security parameters:

- IP Address: This is the IP address of the host represented by the security descriptor.
- Secure Packets: This parameter states whether packets exchanged with the host represented by the security descriptor must be secured or not. This parameter is a Boolean flag. If its value is False, all other parameters except the IP Address parameter are ignored.
- Hash Algorithm: This parameter specifies the hash algorithm used in the authentication of packets exchanged with the host represented by the security descriptor. The security system implements two hash algorithms: SHA-1 (Secure Hash Algorithm-1) and MD5 (Message Digest 5).
- Encryption Algorithm: This parameter specifies the encryption algorithm used to encrypt or decrypt packets exchanged with the host represented by the security descriptor. The security system implements two encryption algorithms: Rijndael and Twofish.
- Key Length: This parameter specifies the length of the encryption key used to encrypt or decrypt packets exchanged with the host represented by the security descriptor. The length could be either 128 bits or 256 bits.
- Encryption Key: This parameter stores the encryption key used to encrypt or decrypt packets exchanged with the host.
- Sequence Number Counter: A monotonically increasing 32-bit value, written in the crypto headers of packets that will be sent to the host represented by the security descriptor. This number is used to detect replayed packets. It is also used as the number of packets, which have been secured with the security descriptor currently used key and algorithms, and which have been sent to the host represented by the security descriptor. This parameter is reset to zero if the security descriptor key or algorithms are changed.
- Packets Received: This parameter holds the number of packets that have been received from the host represented by the security descriptor, and processed with the security descriptor currently used key and algorithms. This parameter is reset to zero if the security descriptor key or algorithms are changed.
- Anti-Replay Window: A window that is used to detect replayed packets previously received from the host represented by the security descriptor. This parameter is reinitialized if the security descriptor key or algorithms are changed.
- Bytes Sent: This parameter holds the number of bytes that have been encrypted with the currently used key and encryption algorithm, and sent to the host represented by the security descriptor.
- Bytes Received: This parameter stores the number of bytes received from the host represented by the security descriptor and that have been decrypted with the currently used key and algorithm.


## THE SECURITY SYSTEM MANAGER (SSM)

The SSM presents a Graphical User Interface (GUI) to the network security administrator, so that he (or she) can interact with the security system, and control its operation. The SSM provides the following functions:

- At initialization time, the SSM loads the encrypted SDL from the Registry, decrypts it, and passes its security descriptors to the CIMD. The CIMD stores the passed security descriptors in a linked list in its own memory context for fast access. The CIMD uses the security parameters of each security descriptor to process inbound and outbound packets exchanged with the host represented by that security descriptor, and it updates some of these parameters during processing.
- The network security administrator can use the SSM to add, remove, or change the parameters of a security descriptor corresponding to a host in the protected network. The SSM updates the SDL accordingly, and uses the DeviceIoControl API (Application Programming Interface) (The DeviceIoControl API sends a control code directly to a specified device driver, causing the corresponding device to perform the corresponding operation [SDK01]) to communicate with the CIMD, and inform it of the changes.
- The SSM periodically communicates with the CIMD using the DeviceIoControl API to get status data reported by the CIMD, and display it to the security administrator. The status data encompasses the mutable security parameters (that are updated by the CIMD) of all the security
descriptors. These parameters are: Sequence Number Counter, Packets Received, Anti-Replay Window, Bytes Sent, and Bytes Received.
- The SSM periodically communicates with the CIMD using the DeviceIoControl API to get the audit data associated with unauthenticated or replayed packets that were received by the CIMD, if any. The audit data associated with each suspicious received packet is stored in an entry in a linked list maintained by the CIMD. The audit data of each suspicious packet includes: the packet source IP address, the packet source MAC address, whether the suspicious packet is unauthenticated or replayed, the upper protocol data encapsulated by the IP packet, the packet total length, and the time when the suspicious packet was received. If there is audit data, the SSM alerts the network security administrator, and indicates the audit data to him (or her).


## The Cryptographic NDIS IM Driver (CIMD)

The CIMD consists of two parts (like any other NDIS IM driver): the miniport part and the protocol part. The miniport part exposes miniport entry points (MiniportXxx functions), which NDIS calls to communicate the requests of one or more overlying protocol drivers. The miniport part in turn forwards these requests to the underlying miniport NIC (Network Interface Card) driver after performing the required security processing, if any.

The protocol part exposes protocol entry points (ProtocolXxx functions), which NDIS calls to communicate requests from underlying miniports. The protocol part in turn forwards these requests to overlying protocols after performing the required security processing, if any.

The CIMD inserts into each outbound IP packet that should be secured a 40-byte crypto header between its IP header and payload. This header consists of three fields:
1- The IV field ( 16 bytes) that holds the random initialization vector used in the encryption.
2- The Hash field ( 20 bytes) that holds a hash code calculated over the immutable fields of the IP header, the IP payload, and the Sequence Number field of the inserted crypto header. This hash code provides support for data integrity and authentication of the IP packet. The data integrity service detects any modification to the content of the packet in transit. The authentication service enables the receiving host to authenticate the sending host, and thus prevents address spoofing attacks.
3- The Sequence Number field (4 bytes), which is used to detect replayed packets. Each time that a packet is sent to a host, the sender increments the Sequence Number Counter of the security descriptor corresponding to that host, and places the resulting value in the Sequence Number field of the packet crypto header.

Then, the CIMD encrypts the payload of the IP packet along with the Hash and Sequence Number fields of the inserted crypto header using the encryption key of security descriptor representing the packet destination host. The encryption provides the required confidentiality to the exchanged data, and it protects the hash code held in the crypto header. Fig. ( 2 shows a typical outbound IP packet that becomes as shown in Fig. ( 3 after being processed by the CIMD.


Fig.( 2). A Typical Outbound IP Packet


Fig.( 3). The Outbound IP Packet after Being Processed by the CIMD

On reception, the CIMD decrypts the encrypted portions of each received IP packet, and then it inspects its crypto header. If the packet is properly authenticated and it is not a replayed packet, the CIMD strips off the crypto header, and then it delivers the packet to upper drivers. Otherwise, if the received packet is not properly authenticated or if it is a replayed packet, the CIMD collects audit information from this packet to be indicated to the network security administrator.

When the CIMD processes an outbound packet, it inserts the crypto header between the packet IP header and IP payload, so that routers in the protected LAN (if any) need not be changed, and they can route the packet properly. Leaving routers unaffected requires also that the CIMD does not encrypt the IP headers of outbound IP packets. However, the CIMD changes the value of the Total Length field of the IP header of each outbound secured packet to reflect the new packet length resulting after the insertion of the crypto header. The Checksum field of the IP header is also changed to a new value calculated over the new IP header.

The security system processes packets in layer 2 (data link layer) of the OSI (Open Systems Interconnection) protocol stack (between the LLC and MAC sublayers). Nevertheless, it does not provide link encryption, and it is considered to be an end-to-end cryptographic system.

## LARGE PACKETS RESTRICTIONS

Since the CIMD increases the length of outbound IP packets by the size of the inserted crypto header ( 40 bytes), the processing of large IP packets may impose the following two problems:

## The First Problem

If the CIMD inserts the crypto header into a large IP packet, whose size is larger than 1460 bytes, the size of the packet will become more than 1500 bytes after the insertion of the crypto header. This will cause the sending NIC to drop the packet, because maximum size of IP packets over Ethernet II is 1500 bytes [HOR84].

Hence, to resolve this problem, the security system explicitly sets the MTU (Maximum Transmission Unit) of each network interface to 1460 bytes instead of the default value (i.e. 1500 bytes). This must be done so that the TCP/IP protocol will not send to the CIMD IP packets larger than 1460 bytes. In Windows 2000, the MTU of an interface can be changed by modifying the following Registry value [MAC00]:
HKEY_LOCAL_MACHINE\SYSTEM\CurrentControlSet\Services\Tcpip\Parameters\Interfaces\int erface $\backslash$ MTU.

## The Second Problem

This problem results from the solution of the first problem. It occurs when a router that uses the security system routes a secured packet of size larger than 1460 bytes, and which was received from another host. Since the MTUs of the router network interfaces are set to 1460 bytes by the security system installed on it, the router will fragment the received secured packet. Apparently,
fragmentation of a secured packet conflicts with the work of the security system. This is because the packet fragments other than the first one will not have crypto headers, and so will be considered unauthentic by the security system on the target host. The first fragment will not be authentic also, because its crypto header originally authenticates the total packet, not only the first fragment. The security system resolves this problem by disabling the Path MTU (PMTU) Discovery [MOG90] that is used by default by Windows 2000 for packets destined to a non-local host [MAC00].

Since the IP layer on the sending host is unaware of the existence of the CIMD that increases the length of outbound packets, PMTU discovery cannot resolve the problem of large packets sent to a non-local host stated above. This is because even if the IP layer adheres to the Next-Hop MTU value in the ICMP (Internet Control Message Protocol) Destination Unreachable messages reported by some router in the packet path, the CIMD still increases the length of outbound packets by the size of the inserted crypto header after it receives them from the IP layer. Thus, resulting packets will have a length 40 bytes more than the Next-Hop MTU reported by the router, and thereby causing the router to drop these packets.

In Windows 2000, when PMTU Discovery is disabled (which is the solution to the problem), an MTU of 576 bytes is used for all non-local destination addresses [MAC00]. Hence, after the CIMD inserts the crypto header into an outbound packet destined to a non-local host, the packet length will not exceed 616 bytes ( 576 bytes, the MTU +40 bytes, the size of the crypto header). This packet length is well below the MTU of intermediate routers that use the security system. Thus, packets having this length will not be fragmented by the intermediate routers. The PMTU Discovery can be disabled by setting the following Windows 2000 Registry value to 0 [MAC00]:
HKEY_LOCAL_MACHINEISYSTEM\CurrentControlSet\Services\Tcpip\Parameters\EnablePMTU Discovery

## SECURITY SYSTEM IMPLEMENTATION AND PERFORMANCE RESULTS

The CIMD was written in C language and using NDIS library support routines, then it was compiled and built using the Windows 2000 DDK (Driver Development Kit). The SSM was developed using Microsoft Visual C++ language.

To measure the performance results, the security system was installed on 5 machines, which were connected as 100BaseTX Fast Ethernet by using Linksys 10/100 dual speed 16-port stackable Hub. The specifications of each machine were as follows:

- Processor:

Intel Pentium III, 866 MHz

- Physical Memory:

128 Mbytes

- Hard Disk: Western Digital Caviar, 20 Gbytes
- LAN Card: Realtek RTL8139(A)
- Operating System: Windows 2000 Advanced Server

Three tests were performed on two machines (from now on, they will be called A and B) during the transfer of a 710-Mbyte file between them: network performance test, memory usage test, and processor usage test. The file was located in A, while B was used to get the file from A. All the results were measured using the Performance tool of Windows 2000. The tests were repeated on the two machines when they used the security system in each of the following cases:
1- The encryption algorithm is Rijndael, and the hash algorithm is SHA-1.
2- The encryption algorithm is Rijndael, and the hash algorithm is MD5.
3- The encryption algorithm is Twofish, and the hash algorithm is SHA-1.
4- The encryption algorithm is Twofish, and the hash algorithm is MD5.

For comparison purposes, the tests were also repeated in the following cases:
1- When the two machines deployed Windows 2000 IPSec with a pre-shared key as the authentication method, ESP as the used IPSec protocol, 3DES as the encryption algorithm, and SHA-1 as the hash algorithm used by the IPSec HMAC.
2- When nothing was used to secure network traffic. This situation will be referred to as: "Normal Case".
The following subsections present and discuss the results of all the performed tests.

## Network Performance Test

The average packets/sec Performance tool counter was used to measure the network performance. Table shows the results of the average packets/sec counter in all the cases.

When the security system is deployed, the degradation in the average packets/sec rate with respect to the Normal Case was about: $31.7 \%$ for (Rijndael,MD5), $35.6 \%$ for (Rijndael,SHA-1), $44.4 \%$ for (Twofish,MD5), and $45.5 \%$ for (Twofish,SHA-1). On the other hand, the use of the IPSec service with a pre-shared key as the authentication method, ESP as the used IPSec protocol, 3DES as the encryption algorithm, and SHA-1 as the hash algorithm caused a degradation of about $30.9 \%$. The degradation in the average packets/sec rate is a normal result because of the delay introduced by the security related processing on the two machines.

Table (1). The Results of the Network Performance Test

| Case | Packets/sec <br> at A | Packets/sec <br> at B |
| :--- | :--- | :--- |
| Normal Case | 10574.911 | 10572.754 |
| IPSec | 7307.058 | 7306.679 |
| Security System (Rijndael,SHA-1) | 6807.960 | 6809.903 |
| Security System (Rijndael,MD5) | 7218.649 | 7217.341 |
| Security System (Twofish,SHA-1) | 5761.566 | 5759.622 |
| Security System (Twofish,MD5) | 5879.617 | 5879.498 |

## Processor Usage Test

Processor usage was measured using the \%Processor Time Performance tool counter, which is the percentage of time the processor is executing a non-Idle thread. This counter was designed as a primary indicator of processor activity. It is calculated by measuring the time that the processor spends executing the thread of the Idle process in each sample interval, and subtracting that value from $100 \%$ (Each processor has an Idle thread, which consumes cycles when no other threads are ready to run) [MSP01].

Notice that the results of this performance measure may not be too accurate because they may be affected by other services and applications that were running on $A$ and $B$ during the file transfer operation. The results of the test are shown in
Table (1. Before the transfer operation started, the \%Processor Time was measured at A and B, and its average was nearly $0.2 \%$ at each one of them.

When either the security system or IPSec is used to secure network traffic, \%Processor Time increases apparently due to the required security related processing. However, the increase in processor usage does not differ much for all the cases that have security processing.
Table ( 1 shows that the processor usage at B is larger than its usage at A in all the cases. This may be due to the fact that B was the machine that initiated and drove the file transfer operation.

Table (1). The Results of the Processor Usage Test

| Case | \%Processor Time <br> at A | \%Processor Time <br> at B |
| :--- | :--- | :--- |
| Normal Case | $41.757 \%$ | $47.903 \%$ |
| IPSec | $84.787 \%$ | $85.212 \%$ |
| Security System (Rijndael,SHA-1) | $84.522 \%$ | $89.804 \%$ |
| Security System (Rijndael,MD5) | $83.674 \%$ | $88.590 \%$ |
| Security System (Twofish,SHA-1) | $85.060 \%$ | $90.825 \%$ |
| Security System (Twofish,MD5) | $86.638 \%$ | $88.600 \%$ |

## Memory Usage Test

Memory usage was investigated using the Available Mbytes counter of the Performance tool. As for the processor usage test, the results of this performance test may not be too accurate because they may be affected by other services and applications that were running on A and B when the file was transferred between them.

Before the file transfer operation started, the memory available at A was: 25.5 Mbytes, while that available at B was: 42 Mbytes. This difference is due to the fact that different services and applications were running on the two machines. Table (3 shows the results of the Available Mbytes counter at A and B when the file was transferred between them in all the cases. The memory used for file transfer at each machine was calculated by subtracting the available memory during the file transfer from the available memory before the file transfer started.

As shown in the table, the memory used at each machine does not differ much for all the cases. It may also be noticed that the memory used at B is more than that used at A in all the cases. This may be because $B$ is the machine that initiated and drove the file transfer operation.

Table (3). The Results of the Memory Usage Test

| Case | Available <br> Mbytes at A | Used <br> Mbytes at A | Available <br> Mbytes at B | Used <br> Mbytes at B |
| :--- | :--- | :--- | :--- | :--- |
| Normal Case | 22.500 | 3 | 36.383 | 5.617 |
| IPSec | 22.680 | 2.8 | 37.030 | 4.97 |
| Security System (Rijndael,SHA-1) | 21.000 | 4.5 | 35.230 | 6.77 |
| Security System (Rijndael,MD5) | 21.000 | 4.5 | 36.770 | 5.23 |
| Security System (Twofish,SHA-1) | 20.090 | 5.41 | 34.000 | 8 |
| Security System (Twofish,MD5) | 21.170 | 4.33 | 33.570 | 8.43 |

## CONCLUSIONS

The most important points concluded throughout the design and implementation of the security system are listed below:

- To provide security to the data exchanged within a network, encryption and message authentication mechanisms must be used. However, these mechanisms impact the average packets/sec rate in the network, which degrades by a percentage depending on the complexity of the used algorithms. Moreover, these security mechanisms increase processor usage on the hosts that perform them approximately to the double.
- The development of an end-to-end cryptographic system that works in layer 2 (data link layer) of the OSI reference model can be made much easier, if the protected protocol that works in layer 3 (network layer) is aware of the existence of the cryptographic system. This may require that the

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protected protocol and the cryptographic system be developed by the same party, or by cooperative parties.

- Windows network drivers represent a powerful and efficient method to transparently intercept and process inbound and outbound network data. Among the well-documented network drivers, the NDIS intermediate driver is the more powerful, and more efficient one.
- If a network driver below the IP layer (such as a NDIS intermediate driver) inserts a number of bytes into outbound packets that will be sent on a certain network interface, the MTU of that interface must be decreased by the number of bytes that will be inserted, so that large packets are not dropped by the network interface.
- If a NIC has its NDIS task offload capabilities enabled, these capabilities may improperly affect the work of installed packet-modifying NDIS intermediate drivers. Hence, these capabilities should be turned off for the modifying intermediate drivers to work properly.


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# EXPERIMENTS ON BIOMASS TRANSPORT INSIDE UPFLOW SLUDGE BLANKET REACTORS INTERMITTENTLY FED 

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#### Abstract

This work describes the experimental activities developed to study the biomass transport phenomena occurring in upflow anaerobic reactor influencing the biomass washout. The experimental investigations have been carried out on pilot UASB fed with the aim to determine the height to which washout is affected by: daily flow distribution; upflow velocity; concentration and sedimentation properties of the biomass. The experiments had shown a considerable influence on the biomass behavior of the time interval between two successive feeds of the reactor. It was found that, if this period is more than 1 hr larger losses of the biomass into the effluent were obtained, independent of the upflow velocity. Shorter time periods give rise to a regular sludge expansion of the interface even with very high upflow velocities (up to $4 \mathrm{~m} / \mathrm{hr}$ ), and accordingly exhibit limited sludge washout.


## KEYWORDS

UASB, sludge washout, solids transport, upflow velocity, intermittently fed.
الخلاصة
يصف البحث الفعاليات المختبرية لار اسة ظاهرة انتقال الكتلة الحية التي تحدث في مفاعل الجريان الصاعد الاهوائي للحمأة وتأثير سرعة الجريان الصاعد على عملية انجراف الكتلة الحية خارج المفاعل، الشيء الأي يودي بدوره الى انخفاض كفاءة الماء المفاعل بسبب هنه الظاهرة. تمت هنه التجارب باستذام منظومة الجريان الصاعد الاهو ائي للحمأة بعد تقليمها بحمأة حبيبية من نفس موقع الار اسة لغرض إيجاد الارتفاع الحرج الذي يؤثر على عملية جرف الكتلة الحية من خلا تغير كل من: كمية الجريان الاذلل الى المفاعل، سرعة


> بالمدة الزمنية الفاصلة بين كل دورة تغذية بمياه الفضلات، وفي الحقيقة إذا كانت هذه الفترة أكثر من ساعة و واحدة فان علئل علية جرف الكتلة الحية خارج المفاعل سيكون كبيرا وبشكل مستقل عن تأثير سرعة الجريان الصاعد. بينما خلا الفترات الزمنية الأقل من ساعة واحدة سبيت تمدد منتظم للحمأة حتى في حالة زيادة سرعة الجريان الصاعا الى (4 متر/ ساعة) مما سبب في تقليل ظاهرة انجراف الكتلة الحية خارج المفاعل.

## INTRODUCTION

The anaerobic biological sludge blanket systems proposed over recent years have been considerable interest because of their good removal efficiencies of organic substrates, their relatively of simple layout and the low capital and operating costs. The most successful systems include the upflow anaerobic sludge blanket (UASB - Lettinga et al., 1980). UASB is consisting of a tank fed from below in which the wastewater to be treated flows vertically upwards: the biomass forms a thick layer of sludge on the bottom under a suspension composed of biologically formed granules (blanket). The granule washout into the final effluent of UASB is obviously a critical feature in the operation of these systems (Barber and Stuckey, 1999). If this were to happen, system performance would drop because of the presence of organic solids in the effluent (Lettinga and Hulshoff Pol, 1991) and the reduction of the biomass in the system (Nachaiyasit and Stuckey, 1997). However, continuously fed systems have shown small washout even with high average upflow velocities, in the order of 1 to $1.5 \mathrm{~m} / \mathrm{hr}$ (Barber and Stuckey, 1999), a result that is essentially attributable to the good sedimentation properties of anaerobic sludge. There is essentially no information available on the washout in systems intermittently fed, which is convivially exist in the wastewater treatment plants of small communities (Garuti et al., 1992).
This work describes the problem of washout in intermittently fed anaerobic systems by referring to experimental tests carried out in a variety of working conditions. These were made possible by using the pilot UASB located at the Al-Mansour company wastewater treatment plant (WWTP) (Baghdad, Iraq). The tests are purposed to determine the extent to which treatment performance is affected by factors such as: daily flow distribution; upflow velocity; concentration and sedimentation properties of biomass.
The work was organised in two phases. Phase 1 analyses of the wastewater characteristic in the anaerobic sections of the Al-Mansour WWTP by monitoring the sludge concentration under different flow conditions.
Phase 2 of the work was carried out in the laboratory using a glass pilot plant UASB inoculated with the sludge from the Al-Mansour WWTP. UASB was fed with a flow having the same organic matter concentration to reproduce operating conditions close to those of the actual system and physically observe sludge dynamics in the system. Repeated measurements of the total suspended solids (TSS) and soluble chemical oxygen demined (COD) content of the effluent made it possible to determine washout and removal efficiencies according to the way the blanket expanding.

## MATERIALS AND METHODS

The experimental activities were carried out at the Al-Mansour WWTP, which consist of an activated sludge biological system with an aeration tank, a settling tank, a thickening tank, a digester for the excess sludge at the end of the treatment processes for an overall volume of $70 \mathrm{~m}^{3}$. The organic substrate content of influent wastewater is partially degraded by the biomass in anaerobic conditions.
The UASB pilot plant was made from a glass tube with a diameter of 0.1 m and a height of 2.5 m , the wastewater enters the reactor from the bottom across distribution system to allow equal contact between granular bacteria and wastewater. The total volume of the reactor is $0.0196 \mathrm{~m}^{3}$. The active volume is $0.0094 \mathrm{~m}^{3}$ (Fig.1). Wastewater is pumped up by a pipeline system, flow meters and valves controlled by a timer system. The system was designed to control discharge and upflow velocity.

The TSS concentration was measured for all sludge samples in compliance with the Standard Methods (1989). The pilot plant was filled up to a height of 1.20 m with $0.0094 \mathrm{~m}^{3}$ of sludge and $7.30 \cdot 10^{-3} \cdot \mathrm{~m}^{3}$ of wastewater from the Al-Mansour WWTP. During the tests, the system was fed generally with a mixture of tap water and glucose having a total COD of $230 \mathrm{~g} / \mathrm{m}^{3}$ (equal to the mean value measured in the influent flow at the Al-Mansour WWTP). In order to check the experimental results, some tests were repeated using wastewater from the Al-Mansour WWTP and these gave acceptable results. In all cases, the temperature and pH of the flow fed to the pilot plant were maintained at almost constant values of $25^{\circ} \mathrm{C}$ and 6.9 , respectively. Experimentation consisted of 10 different tests (Table 1, Figure 1 Schematic representation of the UASB reactor).

## TESTS CARRIED OUT ON THE UASB PILOT PLANT

The results of tests were conducted using the glass pilot UASB set up in the laboratory and varying the duration of the feed interruption phases $\left(\mathrm{D}_{\mathrm{i}}\right)$, the upflow velocity of the flow being treated $(u)$, the duration of the feed phases $\left(D_{f}\right)$, the duration of the cycle $\left(D_{c}\right)$, which is given by the sum of the above two times. The main advantage of this series of experiments consists in observing the expansion of the sludge blanket. Ten tests were carried out with different values of $D_{i}$ : for the first five tests it was less than or equal to 1 hr ; for the others it was $>1 \mathrm{hr}$. The results of the first five tests (Table 1, Columns 7 and 8) show that the sludge blanket almost expanded regularly, regardless of the upflow velocity (some contractor were observed only for $u$ close to $4 \mathrm{~m} / \mathrm{hr}$ or higher). Under these conditions, a clear interface in the sludge blanket was seen to form, a maximum expansion, small TSS concentrations were always measured (Fig.2, for Test 1). Increases in $D_{i}$ (Tests 6 to 10) showed a significantly thickened sludge blanket on the bottom during the feed interruption phases; the formation of many channels in the sludge blanket when the feed started; most of the wastewater flow passing at high speed (much higher than $u$ ) through these channels during the feed phases, with a for impotence 'short circuiting' of the sludge blanket, the formation of an irregular interface which disappeared for $D_{i}$ greater than 3 hr and high TSS concentrations in the effluent. Moreover, increases in $\mathrm{D}_{\mathrm{i}}$ led to a greater volume of biogas trapped in the sludge blanket, which was obviously released in the form of large bubbles at the start of feeding and further contributed to the irregular expansion of the sludge blanket in the form of explosion. The influence of upflow velocity on sludge blanket expansion was assessed on the considerations made above, by referring to regular expansion conditions. In particular, the results of Test 1 were used. These results were obtained with $D_{i}$ equal to 10 min and relative to nine different values of $u$, the determination over time of the height of the sludge blanket interface during four cycles is reported in Figure 3 as can be seen periodic steady-state conditions were reached in all cases after just two cycles. Obviously, the interface reached gradually higher levels as $u$ increased. The height increase was particularly significant when the upflow velocity passed from $2.30 \mathrm{~m} / \mathrm{hr}$ to $3.00 \mathrm{~m} / \mathrm{hr}$. All the curves show a rapid rise in the sludge at constant speed immediately following the start of feeding and as it continues, the curves show indicating the fall in the interface rising speed after the gradual dispersion of the granular, which were less subject to wastewater flow transport effects. The influence of upflow velocity on washout was proved by means of the measurements of suspended solids in the plant effluent (Fig. 2).
As these measurements are held to be coincident with the mean value of TSS concentration in the effluent during five minutes intervals around the moment of maximum sludge blanket expansion. It was possible to calculate sludge mass escaping into the effluent during this interval. This value was held to be significant index of the measurement of overall system washout ( $\mathrm{M}_{\mathrm{w}}$ column 2, Table 2) as it constituted the high percentage of the washout and was generally increasing as $u$ increased.

| M J Mohammed | Experiments on Biomass Transport Inside up flow <br> Sludge Blanket Reactors Intermittently fed |
| :--- | :--- |

Column 3 of Table 2 reports the values indicated with $m_{w}$ and obtained by the ratio of $M_{w}$ with the


Fig(1).: Schematic Diagram of the UASB Pilot Plant

Table (1) Operating conditions and results of tests on the UASB pilot plant.

| Test No. | $\underset{(\mathbf{m i n})}{\text { Df }}$ | $\underset{(\mathbf{m i n})}{\mathbf{D i}}$ | $\underset{(\mathbf{m i n})}{\text { Dc }}$ | $\underset{(\mathbf{m} / \mathbf{h r})}{\mathbf{u}}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 3 | 4 | 2 | 5 | 6 | 7 | 8 |
| 1 | 10 | 10 | 20 | 2.00 | 20 | 20 | 100 |
|  | 10 | 10 | 20 | 2.30 | 20 | 20 | 100 |
|  | 10 | 10 | 20 | 2.50 | 20 | 20 | 100 |
|  | 10 | 10 | 20 | 3.00 | 20 | 20 | 100 |
|  | 10 | 10 | 20 | 3.30 | 20 | 20 | 100 |
|  | 10 | 10 | 20 | 3.45 | 20 | 19 | 95 |
|  | 10 | 10 | 20 | 4.00 | 20 | 19 | 95 |
|  | 10 | 10 | 20 | 4.30 | 20 | 18 | 90 |
|  | 10 | 10 | 20 | 5.15 | 20 | 18 | 90 |
| 2 | 10 | 20 | 30 | 2.00 | 10 | 10 | 100 |
|  | 10 | 20 | 30 | 2.30 | 10 | 10 | 100 |
|  | 10 | 20 | 30 | 4.00 | 10 | 10 | 100 |
|  | 10 | 20 | 30 | 5.15 | 10 | 9 | 90 |
| 3 | 10 | 30 | 40 | 2.30 | 10 | 10 | 100 |
|  | 10 | 30 | 40 | 4.00 | 10 | 10 | 100 |
|  | 10 | 30 | 40 | 5.15 | 10 | 10 | 100 |
| 4 | 10 | 40 | 50 | 2.30 | 10 | 10 | 100 |
|  | 10 | 40 | 50 | 4.00 | 10 | 9 | 90 |
|  | 10 | 40 | 50 | 4.30 | 10 | 9 | 90 |
|  | 10 | 40 | 50 | 5.15 | 10 | 9 | 90 |
| 5 | 10 | 06 | 70 | 2.00 | 10 | 9 | 90 |
|  | 10 | 60 | 70 | 2.30 | 10 | 10 | 100 |
|  | 10 | 60 | 70 | 3.30 | 10 | 9 | 90 |
|  | 10 | 60 | 70 | 3.45 | 10 | 9 | 90 |
|  | 10 | 60 | 70 | 5.15 | 10 | 8 | 80 |
| 6 | 10 | 90 | 100 | 2.30 | 10 | 7 | 70 |
|  | 10 | 90 | 100 | 4.00 | 10 | 4 | 40 |
|  | 10 | 90 | 100 | 4.30 | 10 | 2 | 20 |
|  | 10 | 90 | 100 | 5.15 | 10 | 0 | 0 |
| 7 | 10 | 180 | 190 | 2.30 | 6 | 3 | 50 |
|  | 10 | 180 | 190 | 4.00 | 6 | 2 | 33 |
|  | 5 | 180 | 185 | 4.30 | 6 | 1 | 17 |
|  | 5 | 180 | 185 | 5.15 | 6 | 0 | 0 |
| 8 | 10 | 480 | 490 | 2.30 | 3 | 0 | 0 |
|  | 5 | 480 | 485 | 4.00 | 3 | 0 | 0 |
|  | 5 | 480 | 485 | 4.30 | 3 | 0 | 0 |
|  | 5 | 480 | 485 | 5.15 | 3 | 0 | 0 |
| 9 | 5 | 1440 | 1445 | 2.00 | 3 | 0 | 0 |
|  | 5 | 1440 | 1445 | 2.30 | 3 | 0 | 0 |
|  | 5 | 1440 | 1445 | 4.00 | 3 | 0 | 0 |
| 10 | 5 | 4320 | 4325 | 2.15 | 3 | 0 | 0 |
|  | 5 | 4320 | 4325 | 2.34 | 3 | 0 | 0 |
|  | 5 | 4320 | 4325 | 3.70 | 3 | 0 | 0 |


| M J Mohammed | Experiments on Biomass Transport Inside up flow <br> Sludge Blanket Reactors Intermittently fed |
| :--- | :--- |


$\mathbf{F i g}(\mathbf{2})$. Mean TSS concentrations detected in the effluent of the pilot UASB during Test 1 at the moment of maximum sludge blanket height


Fig(3). The sludge blanket interface height detected in the pilot UASB during Test No. 1
sludge mass present in the plant at the beginning of the test. The value of $m_{w}$ was seen to range between 0.17 and $0.25 \%$ when $u$ was less than $4.00 \mathrm{~m} / \mathrm{hr}$. Moreover, in these conditions the correlation between upflow velocity and washout was second order law (Fig. 4). With values of $u$ higher than $4.00 \mathrm{~m} / \mathrm{hr}$, $\mathrm{m}_{\mathrm{w}}$ exceeded $0.3 \%$ even with regular sludge blanket expansion. This determination was caused by turbulence, which increases separation of the sludge blanket interface. During each investigation in Test 1 the COD of effluent from the pilot plant was determination. The mean values corresponding to each upflow velocity and relative removal efficiencies are reported in Table 2 (column 4 and 5 respectively). Efficiencies are shown in the diagram in (Fig. 5) with a second degree polynomial fitting of the experimental data. It is seen that the best results quadrate to values of $u$ between 3.00 and $4.00 \mathrm{~m} / \mathrm{hr}$ with removal efficiencies values above $60 \%$ with lower values of $u$, the removal efficiencies decrease because of the formation of small channels for the wastewater being treated in the sludge blanket, and although this dose not give rise to the washout that results in the incomplete degradation of organic substrate.

The following observations were obtained:
_If velocity between 3 and $4 \mathrm{~m} / \mathrm{hr}$ then will be not effect on the washout and assures very high removal efficiencies.
_For velocity values below, $3 \mathrm{~m} / \mathrm{hr}$ a negligible blanket expansion will aims, but at the same time results in a channeling phenomenon, which lowers treatment efficiency.
_If velocity is higher than $4 \mathrm{~m} / \mathrm{hr}$, an increase in the washout and reducing in performance in organic substrate removal will be obtained.

Table (2). Washout flows and filtered COD values in the effluent during Test No. 1

| $\boldsymbol{u}$ <br> $(\mathbf{m} / \mathbf{h r})$ | $\mathbf{M}_{\mathbf{w}}$ <br> $(\mathbf{m g})$ | $\mathbf{m}_{\mathbf{w}}$ <br> $(\mathbf{\%})$ | Filtered <br> $\mathbf{C O D}$ <br> $(\mathbf{m g} / \mathbf{l})$ | COD <br> Removal efficiency |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ |
|  |  |  |  |  |
| 2.00 | 52.20 | 0.172 | 129.4 | 41.90 |
| 2.30 | 61.67 | 0.177 | 148.3 | 38.10 |
| 2.50 | 64.00 | 0.184 | 120.8 | 50.00 |
| 3.00 | 71.08 | 0.204 | 76.60 | 66.67 |
| 3.30 | 94.50 | 0.272 | 83.00 | 63.89 |
| 3.45 | 87.17 | 0.205 | 83.00 | 63.60 |
| 4.00 | 79.40 | 0.205 | 76.60 | 61.10 |
| 4.30 | 126.30 | 0.364 | 127.5 | 44.58 |
| 5.15 | 122.50 | 0.358 | 161.0 | 30.00 |
|  |  |  |  |  |


| M J Mohammed | Experiments on Biomass Transport Inside up flow <br> Sludge Blanket Reactors Intermittently fed |
| :--- | :--- |


$\operatorname{Fig}(4)$. Variation of washout with upflow velocity $\left(R^{2}=0.8237\right)$

$\mathbf{F i g}(\mathbf{5})$. Removal efficiency for filtered COD for different upflow velocity $\left(R^{2}=0.8296\right)$

## CONCLUTIONS

The study shows that, when velocity between 3 and $4 \mathrm{~m} / \mathrm{hr}$ the effect on the washout decreased and assures very high removal efficiencies.

The results illustrate that, for velocity values below, $3 \mathrm{~m} / \mathrm{hr}$ a negligible blanket expansion will aims, but at the same time results in a channeling phenomenon, which lowers treatment efficiency.

It seen that, if velocity is higher than $4 \mathrm{~m} / \mathrm{hr}$, an increase in the washout and reducing in performance in organic substrate removal will be obtained.

The results illustrate that the when the feed flow is interrupted for long periods (above 1 h ) considerable losses of biomass into the effluent will be obtained.

From the results it seen that, with shorter periods blanket expansion takes place on a regular basis even with very high upflow velocities (up to $4 \mathrm{~m} / \mathrm{hr}$ ), giving rise to limited washout and high removal efficiencies, especially with velocities ranging between 3 and $4 \mathrm{~m} / \mathrm{hr}$.

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# Stability Issues of Welded Pipe Containing Pulsatile Flows 

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#### Abstract

: This paper deals with the dynamics and stability behavior of a welded pipe containing flowing fluid having a small harmonic component superposed. The equation of motion was derived to represent the motion of a welded pipe conveying a pulsatile flow using a tensioned Euler- Bernoulli beam theory. The finite element analysis was used to simulate the harmonic motion of a welded pipe conveying fluid. It was shown that welded pipes with clamped-clamped and clamped-pinned supports are subject to a multitude of parametric instabilities in all their modes. Stability maps are presented for parametric instabilities of welded pipe with clamped-clamped and clamped-pinned ends. It is found that the extent of the instability regions increases with flow velocity for clamped-clamped and clamped-pinned welded pipes. The most important consideration from a practical point of view is to avoid the onset of parametric resonance.


يتنـاول البحث السلوك الديناميكي و أستقر ارية الأنابيب الملحومـة الناقلـة للمو ائع ذات السرع المتغيرة. تم أشتقاق معادلـة الحركـة

 مدبس خاضعة لعدد من المتغيرات اللامستقرة في جميع أُنماطها. تم رسم خارطة اللاأستقر ارية للأنابيب الملحومة ذات حدود النثبيت الأنفة الذكر . لقد وجد بأن وجود المنـاطق الغير مستقرة يزداد مـع زيـادة سـرعة جريـان المـائع داخل الأنابيب الملحومـة ذات حدود التثبيت المذكورة أنفا.

## KEYWORDS

## Pustule Flow, Stability Regions, Dynamics of Pipes, Parametric Instabilities.

## INTRODUCTION:

Welded pipe conveying fluid are widely used in engineering applications. One of the design challenges is to avoid pipe buckling and flutter under various operation conditions. It's clear that if the velocity of a fluid conveying in pipe is not constant, but has a harmonic fluctuation over and above a constant mean value, then the pipe experiences instability, this phenomenon is similar to a beam
subjected to a periodic axial load [Bolotin, 1964]. The dynamic behavior of the system strongly depends on the different kinds of boundary conditions and on the fact whether the pipe is considered to be inextensible, i.e the cross-sectional area of the pipe is constant.

Many recent researches have been carried out on the vibration of a pipe conveying fluid. Zsolt Szabo et al [Zsolt Szabó, 1997] studied the dynamics of a pipe containing pulsative flow, the stability analyses of the linearized systems were performed in autonomous and nonautonomous (time-periodic) case. Zsolt Szabó [Zsolt Szabó, 2000] investigated the dynamic behavior of a continuum inextensible pipe containing fluid flow having a velocity relative to the pipe has the same but time-periodic magnitude along the pipe at a certain time instant. Wang and Bloom [Wang, 2001] studied the static and dynamic instabilities of submerged and inclined concentric pipes conveying fluid, Zsolt Szabó [Zsolt Szabó, 2003] investigated the nonlinear dynamics of a cantilever elastic pipe that contains pulsatile flow. The equation of motion was derived by using Hamiltonian action function. He used Galerkin's technique to include only finite number of spatial modes in the solution. The stability chart of the time-varying system was computed in the space of the relative perturbation amplitude of the flow velocity and dimensionless forcing frequency using an efficient numerical method based on Chebyshev polynomials. In the near of some critical regions bifurcation diagrams were also computed which show secondary bifurcations and phase locking followed by chaotic motion.

In the industry welded pipe conveying fluid encountered, for example, in the form of exhaust pipes in engines, stacks of fuel gases, air-conditioning ducts, pipes carrying fluid (chemicals) in chemical and power plants, risers in offshore platforms, and tubes in heat exchangers and power plants. The fluid inside the pipe dynamically interacts with the pipe motion, possibly causing the pipe to vibrate.

Also, pipelines play a significant role in the economic and environmental considerations of countries. Some carry water to help irrigate desert areas; others deliver gas over vast distances, and those that carry liquid fuels often unseen as they are buried underground [Lee and Mote, 1997].

In this paper an attempt to study, analytically and numerically, the effect of harmonic fluctuation of the fluid velocity on the dynamic behavior of a welded pipe conveying unsteady flow.

## EQUATION OF MOTION:

The system under consideration consists of a uniform welded pipe conveying unsteady fluid sketched in Fig. (1). the pipe is initially straight, stressed, and finite length.

The equation of motion for pre-stressed single-span pipe conveying unsteady fluid as a function of the axial distance $z$ and time $t$, based on beam theory is given by [Kuiper, 2006]:

Where: EI is the bending stiffness of the pipe, $m=m f+m p, m f$ is the mass of fluid per unit length, $m p$ is the mass of the pipe per unit length, $T_{\text {eff. }}=T \pm A_{i} P_{i}$ so-called effective force, Ai is the internal cross sectional area of the pipe, Pi is the hydrostatic pressure inside the pipe, T is a prescribe axial force due to welding, and $U$ is a fluid velocity.

The left end of the pipe is rigidly support, whereas the right end is assumed to allow no lateral displacement but to provide a restoring moment proportional to the rotation angle of the pipe. The clamped-clamped or clamped-pinned pipe is obtained from this formulation in the limit of the restoring rotational moment going to infinity or zero respectively. Thus, the boundary conditions at ends of the pipe are given as [Paidoussis, 1998]:

$$
\begin{align*}
& y(0, \mathrm{t})=0  \tag{2}\\
& \frac{\square \hat{Y}(0, \mathrm{t})}{\square \dot{Y}}=0  \tag{3}\\
& \operatorname{EI} \frac{\square \hat{Y} \mathrm{y}(\mathrm{~L}, \mathrm{t})}{\square \hat{X}^{2}}=\mathrm{K}_{\mathrm{rs}} \frac{\square \hat{Y}(\mathrm{~L}, \mathrm{t})}{\square \dot{Y}}  \tag{4}\\
& \mathrm{y}(\mathrm{~L}, \mathrm{t})=0 \tag{5}
\end{align*}
$$

Where Krs is the stiffness of the rotational spring at the right end.
The statement of the problem eqs. (1) ~ (5) can be written in a non-dimensional form as follows:

$$
\begin{align*}
& \eta(0, \tau)=0 \\
& \frac{\partial \eta(0, \tau)}{\partial \xi}=0 \tag{8}
\end{align*}
$$

$\frac{\partial^{2} \eta(1, \tau)}{\partial^{2} \xi}=-K \frac{\partial \eta(1, \tau)}{\partial \xi}$
$\eta(1, \tau)=0$
With the following dimensionless variables and parameters:
$\eta=y / L$
$\xi=\mathrm{z} / \mathrm{L}$
$\tau=\mathrm{t} \sqrt{\mathrm{EI} / \mathrm{m}} / \mathrm{L}^{2}$
$\mathrm{V}=\mathrm{LU} \sqrt{\mathrm{m}_{\mathrm{f}} / \mathrm{EI}}$
$\gamma=\mathrm{L}^{2} \mathrm{~T}_{\text {eff. }} / \mathrm{EI}$
$\beta=\sqrt{\frac{\mathrm{m}_{\mathrm{f}}}{\mathrm{m}}}$

$=0$
Fig. (1) Welded pipe conveying fluid $\mathbf{Z}^{=} \mathrm{L}$

## ANALYTICAL ANALYSIS:

It is clear that if a velocity of a fluid conveying in a welded pipe is not constant, but has a harmonic fluctuation under and above a constant mean value, then the pipe experiences instability.

To describe the function of this unsteady flow harmonically, Fourier series with one harmonic for the periodic velocity may be used to obtain [Bolotin, 1964],
$\mathrm{V}=\mathrm{V}_{\mathrm{o}}[1+\Delta \operatorname{Cos}(\mathrm{w} \tau)]$
Where $\Delta$ is an excitation parameter, w is a non-dimensional circular frequency, and $\tau$ is a nondimensional time.

Substituting eq. (11) into eq. (6) yields:

Where

$$
\begin{equation*}
\Phi=(1+\Delta \operatorname{Cos}(\mathrm{w} \tau)) \tag{12}
\end{equation*}
$$

## Regions of Instabilities:

The regions of instability of eq. (12) are separated from the stable region by periodic solution with periods ( T ) and ( 2 T ), where ( $\mathrm{T}=2 \pi / \mathrm{w}$ ) hence there are two solutions of identical periods bound the region of instability, the regions enclosed by the solution having period ( 2 T ) correspond to the "primary instabilities", while the region of "secondary instabilities" are enclosed by the solution having period (T), for example, if a system with natural frequency ( $\mathrm{w}_{\mathrm{n}}$ ), the primary instabilities occurs at ( $\mathrm{w}=2 \mathrm{w}_{\mathrm{n}} / \mathrm{q}$ ) where ( $\mathrm{q}=1,3,5 \ldots$ ) while the secondary instability region occurs at ( $\mathrm{w}=2 \mathrm{w}_{\mathrm{n}} / \mathrm{q}$ ) where ( $\mathrm{q}=0,2,4 \ldots$ ) furthermore, instabilities corresponding to ( $\mathrm{q}=1$ and 2 ) are known as the principal primary and the principal secondary instabilities respectively.

## Primary Instability Regions:

To determine the region of primary instability the displacement $\eta$ may be expressed as follows [Singh, 1979]:

$$
\begin{equation*}
\eta(\xi, \tau)=\underset{q=1,1,, 5, \ldots}{\ddagger}{ }_{q}(\xi) \operatorname{Sin}\left(\frac{1}{2} q w \tau\right)+R_{q}(\xi) \operatorname{Cos}\left(\frac{1}{2} q w \tau\right) \tag{13}
\end{equation*}
$$

Where Hq and Rq are unknowns function of $\xi$, substituting eq. (13) into eq. (12) gives,

$$
\begin{equation*}
\underset{q=1,3,5, \ldots}{\ddagger}>\left[\left\{\frac{d^{4} H_{q}}{d \xi^{4}}+\left(\gamma+V_{0}^{2}+\frac{V_{0}^{2} \Delta^{2}}{2}\right) \frac{d^{2} H_{q}}{d \xi^{2}}-\beta V_{0} q w \frac{d R_{q}}{d \xi}-\left(\frac{q}{2}\right)^{2} w^{2} H_{q}\right] \operatorname{Sin}\left(\frac{q w \tau}{2}\right)\right. \tag{14}
\end{equation*}
$$

$+\left\{\frac{d^{4} R_{q}}{d \xi^{4}}+\left(\gamma+V_{0}^{2}+\frac{V_{0}^{2} \Delta^{2}}{2}\right) \frac{d^{2} R_{q}}{d \xi^{2}}+\beta V_{0} q w \frac{d H_{q}}{d \xi}-\left(\frac{q}{2}\right)^{2} w^{2} R_{q}\right\} \operatorname{Cos}\left(\frac{q w \tau}{2}\right)$
$+\left\{\mathrm{V}_{0}^{2} \Delta \frac{\mathrm{~d}^{2} \mathrm{H}_{\mathrm{q}}}{\mathrm{d} \xi^{2}}-\frac{\beta \mathrm{V}_{0} \Delta \mathrm{qw}}{2} \frac{\mathrm{dR}_{\mathrm{q}}}{\mathrm{d} \xi}-\frac{\beta \mathrm{V}_{0} \Delta \mathrm{w}}{2} \frac{\mathrm{dR}}{\mathrm{q}} \mathrm{q}\right\} \operatorname{Sin}\left(\frac{(\mathrm{q}+2) \mathrm{w} \tau}{2}\right)$
$+\left\{\mathrm{V}_{0}^{2} \Delta \frac{\mathrm{~d}^{2} \mathrm{R}_{\mathrm{q}}}{\mathrm{d} \xi^{2}}+\frac{\beta \mathrm{V}_{0} \Delta \mathrm{qw}}{2} \frac{\mathrm{dH}}{\mathrm{q}} \mathrm{q}\left(\frac{\beta \mathrm{V}_{0} \Delta \mathrm{w}}{2} \frac{\mathrm{dH}_{\mathrm{q}}}{\mathrm{d} \xi}\right\} \operatorname{Cos}\left(\frac{(\mathrm{q}+2) \mathrm{w} \tau}{2}\right)\right.$
$+\left\{\mathrm{V}_{0}^{2} \Delta \frac{\mathrm{~d}^{2} \mathrm{H}_{\mathrm{q}}}{\mathrm{d} \xi^{2}}-\frac{\beta \mathrm{V}_{0} \Delta \mathrm{qw}}{2} \frac{\mathrm{dR}}{\mathrm{q}} \mathrm{d} \xi+\frac{\beta \mathrm{V}_{0} \Delta \mathrm{w}}{2} \frac{\mathrm{dR}_{\mathrm{q}}}{\mathrm{d} \xi}\right\} \operatorname{Sin}\left(\frac{(\mathrm{q} \quad 2) \mathrm{w} \tau}{2}\right)$
$+\left\{\mathrm{V}_{0}^{2} \Delta \frac{\mathrm{~d}^{2} \mathrm{R}_{\mathrm{q}}}{\mathrm{d} \xi^{2}}+\frac{\beta \mathrm{V}_{0} \Delta \mathrm{qw}}{2} \frac{\mathrm{dH}}{\mathrm{q}} \mathrm{d}^{2} \quad \frac{\beta \mathrm{~V}_{0} \Delta \mathrm{w}}{2} \frac{\mathrm{dH}_{\mathrm{q}}}{\mathrm{d} \xi}\right\} \operatorname{Cos}\left(\frac{(\mathrm{q} 2}{2} \mathrm{w} \tau\right)$
$+\frac{\mathrm{V}_{0}^{2} \Delta^{2}}{4} \frac{\mathrm{~d}^{2} \mathrm{H}_{\mathrm{q}}}{\mathrm{d} \xi^{2}}\left\{\operatorname{Sin}\left(\frac{(\mathrm{q}+4) \mathrm{w} \tau}{2}\right)+\operatorname{Sin}\left(\frac{(\mathrm{q} \quad 4) \mathrm{w} \tau}{2}\right)\right\}$
$\left.+\frac{\mathrm{V}_{0}^{2} \Delta^{2}}{4} \frac{\mathrm{~d}^{2} \mathrm{R}_{\mathrm{q}}}{\mathrm{d} \xi^{2}}\left\{\operatorname{Cos}\left(\frac{(\mathrm{q}+4) \mathrm{w} \tau}{2}\right)+\operatorname{Cos}\left(\frac{(\mathrm{q} 4) \mathrm{w} \tau}{2}\right)\right\}\right]=0$

The region of principal primary instability can be obtained by truncating the series in eq. (14) at ( $q=1$ ), now equating the coefficients of $[\operatorname{Sin}(w \tau / 2)]$ and $[\operatorname{Cos}(w \tau / 2)]$ from both sides of eq. (14) yield,

$$
\begin{align*}
& \frac{d^{4} H_{1}}{d \xi^{4}}+\left(\gamma+V_{0}^{2}+\frac{V_{0}^{2} \Delta^{2}}{2}-V_{0}^{2} \Delta\right) \frac{d^{2} H_{1}}{d \xi^{2}}-\frac{w^{2}}{4} H_{1}-\beta V_{0} w \frac{d R_{1}}{d \xi}=0  \tag{15}\\
& \frac{d^{4} R_{1}}{d \xi^{4}}+\left(\gamma+V_{0}^{2}+\frac{V_{0}^{2} \Delta^{2}}{2}+V_{0}^{2} \Delta\right) \frac{d^{2} R_{1}}{d \xi^{2}}-\frac{w^{2}}{4} R_{1}+\beta V_{0} w \frac{d H_{1}}{d \xi}=0 \tag{16}
\end{align*}
$$

Neglecting ( $\beta$ ) results in an accuracy of the order ( $98 \%$ ) furthermore, the effect of neglecting ( $\beta$ ) should not be mean that the effect of fluid mass (mf) is also negligible, this is attributed to the fact that the non-dimensional flow velocity ( V ) and the natural frequency ( w ) are also function to (mf), neglecting ( $\beta$ ) in eqs. (15) and (16) results [Chen, 1971],

$$
\begin{align*}
& \frac{d^{4} \mathrm{H}_{1}}{\mathrm{~d} \xi^{4}}+\left(\gamma+\mathrm{V}_{0}^{2}+\frac{\mathrm{V}_{0}^{2} \Delta^{2}}{2}-\mathrm{V}_{0}^{2} \Delta\right) \frac{\mathrm{d}^{2} \mathrm{H}_{1}}{\mathrm{~d} \xi^{2}}-\frac{\mathrm{w}^{2}}{4} \mathrm{H}_{1}=0  \tag{17}\\
& \frac{\mathrm{~d}^{4} \mathrm{R}_{1}}{\mathrm{~d} \xi^{4}}+\left(\gamma+\mathrm{V}_{0}^{2}+\frac{\mathrm{V}_{0}^{2} \Delta^{2}}{2}+\mathrm{V}_{0}^{2} \Delta\right) \frac{\mathrm{d}^{2} \mathrm{R}_{1}}{\mathrm{~d} \xi^{2}}-\frac{\mathrm{w}^{2}}{4} \mathrm{R}_{1}=0 \tag{18}
\end{align*}
$$

Note that eq. (17) gives the upper limit of the primary instability region, while eq. (18) represents the lower instability region; the solution of eq. (17) may be written as,

$$
\begin{equation*}
\mathrm{H}_{1}=\mathrm{E}_{1} \operatorname{Sin}\left(\mathrm{f}_{1} \xi\right)+\mathrm{E}_{2} \operatorname{Cos}\left(\mathrm{f}_{1} \xi\right)+\mathrm{E}_{3} \operatorname{Sinh}\left(\mathrm{f}_{2} \xi\right)+\mathrm{E}_{4} \operatorname{Cosh}\left(\mathrm{f}_{2} \xi\right) \tag{19}
\end{equation*}
$$

While the solution of eq. (18),

$$
\begin{equation*}
\mathrm{R}_{1}=\mathrm{T}_{1} \operatorname{Sin}\left(\mathrm{k}_{1} \xi\right)+\mathrm{T}_{2} \operatorname{Cos}\left(\mathrm{k}_{1} \xi\right)+\mathrm{T}_{3} \operatorname{Sinh}\left(\mathrm{k}_{2} \xi\right)+\mathrm{T}_{4} \operatorname{Cosh}\left(\mathrm{k}_{2} \xi\right) \tag{20}
\end{equation*}
$$

Where: $\quad \mathrm{f}_{1}=\sqrt{\frac{\mathrm{a}_{1}+\sqrt{\mathrm{a}_{1}^{2}+\mathrm{w}^{2}}}{2}} \quad, \quad \mathrm{f}_{2}=\sqrt{\frac{-\mathrm{a}_{1}+\sqrt{\mathrm{a}_{1}^{2}+\mathrm{w}^{2}}}{2}}$

$$
\begin{gathered}
\mathrm{k}_{1}=\sqrt{\frac{\mathrm{a}_{2}+\sqrt{\mathrm{a}_{2}^{2}+\mathrm{w}^{2}}}{2}}, \quad \mathrm{k}_{2}=\sqrt{\frac{-\mathrm{a}_{2}+\sqrt{\mathrm{a}_{2}^{2}+\mathrm{w}^{2}}}{2}} \\
\mathrm{a}_{1}=\mathrm{V}_{0}^{2}+\gamma+\frac{\mathrm{V}_{0}^{2} \Delta^{2}}{2}-\mathrm{V}_{0}^{2} \Delta, \quad \mathrm{a}_{2}=\mathrm{V}_{0}^{2}+\gamma+\frac{\mathrm{V}_{0}^{2} \Delta^{2}}{2}+\mathrm{V}_{0}^{2} \Delta
\end{gathered}
$$

And E1...E4, T1......T4 are arbitrary constants.
The upper limit can be evaluated by substituting eq. (19) into the boundary conditions eqs. (7)~ (10) to give the following equation in matrix form:
$\left[\mathrm{A}_{\mathrm{i}, \mathrm{j}}\right]\left\{\mathrm{E}_{\mathrm{j}}\right\}=0$
While the lower limit can be evaluated by substituting eq. (20) into the boundary conditions eqs. (7)~ (10) yields.
$\left[\mathrm{B}_{\mathrm{i}, \mathrm{j}}\right]\left\{\mathrm{T}_{\mathrm{j}}\right\}=0$

Both eqs. (21) and (22) are functions of many physical parameter such as (w, $\Delta, \mathrm{V}_{0}$ ) searching for values of any of these parameters which vanish the above determinants gives the appropriate limit of the primary region.

## Secondary Instability Regions:

To determine the regions of secondary instability, the displacement $\xi$, is expressed as [Singh, 1979],

$$
\begin{equation*}
\eta(\xi, \tau)=\underset{q=0,2,4, \ldots}{\ddagger} \neq H_{q}(\xi) \operatorname{Sin}\left(\frac{1}{2} q w \tau\right)+\mathrm{R}_{\mathrm{q}}(\xi) \operatorname{Cos}\left(\frac{1}{2} \mathrm{q} w \tau\right) \tag{23}
\end{equation*}
$$

Substituting eq. (23) into eq. (12) result in eq. (14) with summation over $\mathrm{q}=0,2,4, \ldots$ the region of the principal secondary instability can be prediction by truncated the series in the resulting equation (with $\mathrm{q}=0,2,4, \ldots$ ) at $\mathrm{q}=0,2$ and neglecting ( $\beta$ ) result the following equations:

$$
\begin{align*}
& \frac{d^{4} H_{2}}{d \xi^{4}}+\left(\gamma+V_{0}^{2}+\frac{V_{0}^{2} \Delta^{2}}{2}\right) \frac{d^{2} H_{2}}{d \xi^{2}}-w^{2} H_{2}=0  \tag{24}\\
& \frac{d^{4} R_{0}}{d \xi^{4}}+\left(\gamma+V_{0}^{2}+\frac{V_{0}^{2} \Delta^{2}}{2}\right) \frac{d^{2} R_{0}}{d \xi^{2}}+V_{0}^{2} \Delta \frac{d^{2} R_{2}}{d \xi^{2}}=0  \tag{25}\\
& \frac{d^{4} R_{2}}{d \xi^{4}}+\left(\gamma+V_{0}^{2}+\frac{V_{0}^{2} \Delta^{2}}{2}\right) \frac{d^{2} R_{2}}{d \xi^{2}}-w^{2} R_{2}+V_{0}^{2} \Delta \frac{d^{2} R_{0}}{d \xi^{2}}=0 \tag{26}
\end{align*}
$$

Note that eq. (24) is an uncoupled differential equation related to the upper limit and may have a solution of the form:

$$
\begin{equation*}
\mathrm{H}_{2}=\mathrm{D}_{1} \operatorname{Sin}\left(\mathrm{~g}_{1} \xi\right)+\mathrm{D}_{2} \operatorname{Cos}\left(\mathrm{~g}_{1} \xi\right)+\mathrm{D}_{3} \operatorname{Sinh}\left(\mathrm{~g}_{2} \xi\right)+\mathrm{D}_{4} \operatorname{Cosh}\left(\mathrm{~g}_{2} \xi\right) \tag{27}
\end{equation*}
$$

Where:

$$
g_{1}=\sqrt{\frac{\mathrm{b}_{1}+\sqrt{\mathrm{b}_{1}^{2}+4 \mathrm{w}^{2}}}{2}}, \quad g_{2}=\sqrt{\frac{-\mathrm{b}_{1}+\sqrt{\mathrm{b}_{1}^{2}+4 \mathrm{w}^{2}}}{2}}
$$

$$
\mathrm{b}_{1}=\mathrm{V}_{0}^{2}+\gamma+\frac{\mathrm{V}_{0}^{2} \Delta^{2}}{4}
$$

While eqs. (25) and (26) are coupled differential equations related to the lower limit and can be solved by using the series solution as,

And

$$
\begin{equation*}
R_{2}=\stackrel{8}{\underset{j}{ }=1}{ }^{\prime} d_{2 j} e^{\Lambda, \xi} \tag{29}
\end{equation*}
$$

Where $\Lambda j$ 's are the roots of the polynomial

$$
\begin{array}{cc}
\Lambda^{4}+\left(\gamma+\mathrm{v}_{0}^{2}+\frac{\mathrm{v}_{0}^{2} \Delta^{2}}{2}\right) \Lambda^{2} & \mathrm{v}_{0}^{2} \Delta \Lambda^{2} \\
2 \mathrm{v}_{0}^{2} \Delta \Lambda^{2} & \Lambda^{4}+\left(\gamma+\mathrm{v}_{0}^{2}+\frac{3 \mathrm{v}_{0}^{2} \Delta^{2}}{4}\right) \Lambda^{2}-\mathrm{w}^{2}
\end{array}
$$

Note that d 0 j 's and d 2 j 's are related to each other by,

$$
\mathrm{d}_{0 \mathrm{j}}=\frac{\mathrm{v}_{0}^{2} \Delta \Lambda_{\mathrm{j}}^{2}}{\left[\Lambda_{\mathrm{j}}^{4}+\left(\gamma+\mathrm{v}_{0}^{2}+\frac{\mathrm{v}_{0}^{2} \Delta^{2}}{2}\right) \Lambda_{\mathrm{j}}^{2}\right]} \mathrm{d}_{2 \mathrm{j}}
$$

There are two limits which bound the principal secondary instability regions, the upper and lower limits; the upper limit can be evaluated by substituting eq. (27) into the boundary conditions equations eqs. (7)~ (10) Which gives,
$\left[\mathrm{A}_{\mathrm{i}, \mathrm{j}}\right]\left\{\mathrm{D}_{\mathrm{j}}\right\}=0$
While the lower limit can be evaluated by substituting eqs. (28)\& (29) into the boundary conditions eqs. (7)~ (10) yields,

$$
\begin{equation*}
\left[\mathrm{B}_{\mathrm{i}, \mathrm{j}}\right]\left\{\mathrm{d}_{\mathrm{j}}\right\}=0 \tag{32}
\end{equation*}
$$

Both equations (31) and (32) are functions of many physical parameters such as ( $\mu, \mathrm{w}, \Delta$, and V ) searching for values of any of these parameters which vanishing the above determinants gives the appropriate limit of the secondary region.

## FINITE ELEMENT MODELING PROCEDURE:

The FE analysis was carried out using a general purpose FE package ANSYS V9.0. The approach is divided into five parts: thermal analysis, coupled field thermal-structure analysis, computational fluid dynamics (CFD), coupled field fluid-structure analysis, and modal analysis.

A non- linear transient thermal analysis was conducted first to obtain the global temperature history generated during and after welding process. A stress analysis was then developed with the temperatures obtained from the thermal analysis used as loading to the stress model.

The solutions of the governing Navier-Stokes equations for the axisymmetric geometries modeled are obtained using ANSYS FLOTRAN analysis. The governing flow equations are discretized in space according to the spectral element method. Spectral elements combine high order accuracy with the geometric flexibility of low-order finite element methods. The computational domain is divided into a number of non-degenerate spectral elements within which all information on geometry, flow
initial and boundary conditions and solutions is approximated by high order polynomial expansions. A local mesh is constructed within each element, and points on this mesh are used as interpolate points for the expansion of all dependent variables. All the simulations were performed with no-slip (zero velocity) conditions at all walls and zero pressure at the flow outlet.
The coupled field fluid-structure analysis solved the equations for the fluid and solid domains independently of each other. It transfers fluid forces and solid displacements, velocities across the fluid-solid interface. The algorithm continues to loop through the solid and fluid analyses until convergence is reached for the time step (or until the maximum number of stagger iterations is reached). Convergence in the stagger loop is based on the quantities being transferred at the fluid-solid interface.

Finally used modal analysis to determine the vibration characteristics (natural frequencies and mode shapes) of a welded pipe conveying fluid. The natural frequencies and mode shapes are important parameters in the design of a structure for dynamic loading conditions.

## RESULTS AND DISCUSSIONS:

Study the stability issues for particular single span ASTM214-71 mild steel welded pipe system with ( 1 m ) length, ( 50.8 mm ) outer diameter, $(1.5 \mathrm{~mm})$ thickness. The welded pipe was formed by joining two ( 0.5 m ) pipes by fusion arc welding with a current of 30 A and voltage equal 460 volt using an electrode type E7010-G to make a straight pipe 1m length with welding on its mid span.; the welding procedure was modeled as a single pass in this analysis.
The analytical analysis is performed using Matlab V6.5 software to determine the limits of primary and secondary instability regions. The program was developed to be used for any specified pipe dimensions, length, pipe material stiffness, different flow velocities, and welding specifications. The FE analysis is performed using ANSYS V9.0 software. The parameters used in the calculations are listed in table (1).

Table (1) Parameters used in the calculation

| EI | 1.4122*10 ${ }^{4}$ | $\mathbf{N m}{ }^{2}$ |
| :---: | :---: | :---: |
| $\mathrm{m}_{\mathrm{f}}$ | 1.795 | Kg/m |
| m | 3.608 | Kg/m |
| R | 25.4 | mm |
| $\mathrm{T}_{\text {eff. }}$ | $3.0243 * 10^{5}$ | N |
| L | 1 | m |
| $\rho_{\text {f }}$ | 1000 | $\mathrm{Kg} / \mathrm{m}^{3}$ |
| $\boldsymbol{\beta}$ | 3.264 |  |

## Clamped-Clamped Welded Pipe:

Fig. (2) Shows the regions of parametric instability in the range $0.5<\mathrm{w} / \mathrm{w}_{01}<6.0$ for a clampedclamped welded pipe $\left(\mathrm{V}_{0}=2\right)$, where $\mathrm{w}_{01}$ is the first mode natural frequency at zero flow. If instead of $\mathrm{w} / \mathrm{w} 01$, the ordinate $\mathrm{w} / \mathrm{w}_{\mathrm{n}}$ had been utilized, where $\mathrm{w}_{\mathrm{n}}$ is the actual natural frequency for the mode concerned at $\mathrm{V}_{0}=2$, then the principal primary regions of all the modes would begin at $\mathrm{w} / \mathrm{w}_{\mathrm{n}}=2$, the second primary region at $\mathrm{w} / \mathrm{w}_{\mathrm{n}}=2 / 3$, the principal secondary region at $\mathrm{w} / \mathrm{w}_{\mathrm{n}}=1$, and so on.

With the ordinate used here, associated with the first mode are:
The principal primary region beginning at $\mathrm{w} / \mathrm{w}_{01}=1.8$.
The principal secondary at $\mathrm{w} / \mathrm{w}_{01}=0.9$.
The secondary primary region beginning at $\mathrm{w} / \mathrm{w}_{01}=0.6$.
Similarly, associated with the second mode, the corresponding regions begin at $\mathrm{w} / \mathrm{w}_{01}=5.1,2.6$, and 1.7, respectively. Associated with the third mode are the (1) principal secondary region beginning at $\mathrm{w} / \mathrm{w}_{01}=5.1$, and second primary region at $\mathrm{w} / \mathrm{w}_{01}=3.4$.

Fig. (3) Shows the effect of flow velocity on the principal regions of instability associated with the first mode of a clamped-clamped welded pipe. It is noted that as the flow velocity increases the regions of instability are displaced downwards, which reflects the decrease of the first mode frequency with flow. It is also noted that the regions of instability become broader with increasing flow.

Fig. (4) Shows the effect of $\beta$ on parametric instabilities. It is seen that with increasing $\beta$ the regions of instability become broader and displaced downwards, which reflects the lowering of the natural frequencies as $\beta$ increases for this particular flow velocity.

## Clamped-Pinned Welded Pipe:

Fig. (5) Shows the parametric instability regions for a clamped-pinned welded pipe for $\mathrm{V}_{0}=4.5,5.5$, 6 in the range $\mathrm{w} / \mathrm{w} 02<2.4$. the large regions of instability in the middle of the figure are the principal primary regions associated with the second mode, while at the bottom is a principal secondary region which occurs for $\mathrm{V}_{0}=6$ only. The small regions at the top are principal secondary regions associated with the third mode.
Figures ( $6 \mathrm{a}, \mathrm{b}$ ) show, respectively, the primary and secondary instability regions, for the range of frequencies shown, of a welded pipe. The three uppermost regions of instability in figure (6a), for $\mathrm{V}_{0}=6,7.5,8$ and 9 , are principal primary regions associated with the third mode, while the two large regions in the middle, for $\mathrm{V}_{0}=8$ and 9 , are a mixture of principal primary regions associated with the second and third modes.

Finally, the smaller regions at the bottom of figure (6b) may similarly be divided into the following two groups: (i) the regions for $\mathrm{V}_{0}=6,7.5$, and 8 are mixtures of principal primary regions associated with the second mode and of second primary regions associated with the third mode, (ii) the regions for $\mathrm{V}_{0}=8$ and 9 are mixtures of second primary regions associated with the second and third modes. This fusion of the regions of instability is shown particularly well in the cases of $\mathrm{v} 0=8$ and 9 , where each of the regions is formed of two interlinked distinct zones, the upper of which is related to the second mode and the lower to the third mode.

In figure (6b) the upper region $\left(\mathrm{V}_{0}=6\right)$ is the principal secondary one associated with third mode, while the remaining regions are all mixtures of principal secondary regions associated with the second and third modes. The upper areas of the latter are associated with the third mode and the lower areas with the second, except for $\mathrm{V}_{0}=8$ where no such distinction may be made.

It would be of interest to compare the results of dynamic stability obtained for a pipe conveying unsteady flow without welding by Chen [Chen, 1971]. We can see that the effect of welding is to reduce the range of beginning the principal primary, principal secondary, and second primary regions of instability for clamped-clamped and clamped-pinned boundary conditions.


Fig. (2) Parametric instability boundaries for a clamped-clamped welded pipe $\left(\mathrm{V}_{0}=2\right)$. The system is unstable within the triangular regions


Fig. (3) The effect of flow velocity, $\mathrm{V}_{0}$, on the principal instabilities associated with the first mode of a clamped-clamped welded pipe, for three values of $\mathrm{V}_{0}$


Fig. (4) The effect of $\beta$ on parametric instabilities



Fig. (5) Parametric instability boundaries for a clamped-pinned welded pipe

-b Fig. (6) Parametric instability boundaries for a clamped-pinned welded pipe a- Primary instability regions b- Secondary instability regions

## CONCLUSIONS

Analytical and finite element analyses are used to determine the regions of instability of a welded pipe conveying pulsatile flow with clamped-clamped and clamped-pinned boundary conditions. It was shown that these welded pipes are subjected to a multitude of parametric instabilities in all their modes. It was shown also that the pulsating flow in a welded pipe can cause parametric resonance, resembling a column subjected to periodic axial loads. The onset of instability in engineering systems, such as welded pipes could be catastrophic. The most important consideration from a practical point of view is to avoid the onset of parametric resonance.

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# STUDY OF PERFORMANCE OF S.I.E. FUELED WITH SUPPLEMENTARY HYDROGEN TO GASOLINE 

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#### Abstract

This paper includes study of performance of single cylinder, 4-stroke spark ignition engine Ricardo E6, with variable compression ratio, spark timing and equivalence ratio, fueled with supplementary hydrogen to gasoline.

The speed of 25 rps and higher useful compression ratio were chosen in studying the effect of wide range of equivalence ratios and spark timing.

The results showed that HUCR for mixture of two fuels was (9:1). The brake power when operated with gasoline was higher than when it was fueled with hydrogen alone, but when mixing two fuels the brake power increased and became higher than that when working with gasoline to a certain limit (the hydrogen volumetric ratio in the mixture reached $80 \%$ ), after this limit the brake power reduced by increasing hydrogen volumetric ratio.

The equivalence ratio at which the brake power reach its highest value was between ( $\varnothing=1-1.1$ ) when mixing the two fuels. The results showed that the engine can work with very lean equivalence ratios with supplementary hydrogen, the indicated thermal efficiency increased also, and the brake specific fuel consumption reduced when hydrogen volumetric ratio increased.


## الخلاصة

(Ricardo تضمن هذا البحث در اسة أداء محرك أحادي الاسطوانة رباعي الأشو اط يعمل بالشر ارة، نوع (E6)، ذي نسبة انضغاط ونوقيت شرر ونسبة مكافئة متغيرة عند عمله بإضافة الهيدروجين للجازولين. نركزت الار اسة على بحث تأثثر متغيرات رئيسية في أداء المحرك، وهي نسبة الانضغاط و النسبة المكافئة وتوقيت الثشرر و اللسرعة، أظهرت النتائج أن نسبة الانضغاط النافعة العليا لخليط من الوقودين هــي (1: 9)، وان القدرة المكبحية كانت تزداد بزيادة نسبة الانضغاط، كما ان القدرة المكبحية في حالة الجازولين تزيد عن تلك اللناتجة باستخدام الهيبروجين، ولكن عند خلط الوفودين تزداد القـــر رة المكبحيــة عــن حالـــة اســتخدام الجازولين الى حد معين، (نسبة الهيدروجين الحجمية في الخليط 80\%) بعدها تقل بزيادة هذه النسبة. وان النسبة المكافئة التي تم الحصول عندها على أعلى قدرة مكبحبة نتر اوح بين (1.1-0=1.0 ( ) عند خلط الوقودين، كما بينت الار اسة ان المحرك يمكن أن يعمل عند نسب مكافئة ضعيفة جدا" بإضـافة الهيـــرووجين،


النسبة الحجمية للهيدروجين المضاف.

## KEY WORDS

Hydrogen, gasoline, equivalence ratio, compression ratio, spark timing, speed, brake power, specific fuel consumption, indicated thermal efficiency, exhuast gas temperature.

## INTRODUCTION

There is no room for doubt that the world's convenantiol source of fossil fuel are being exhuasted at an alarming rate. The transportation sector is one of the most important areas which has been badly hit by the energy crisis, which is basicaly a fuel crisis. It is certain that the demand of indeividual transport will continue to grow despite the decline in petroleum production, because autimobiles have become an integral part of the present day life style. With the growing use of the individual transporttion system, the need for spark ignition engine is rapidly growing.

Internal combustion engines provide $85 \%$ of the energy needed by mankind, and it is supposed that in populated areas their shear of air pollution reaches up to $70 \%$. It is supposed that for a period of $60-80$ years thay will remain the basic converter of heat energy from the combustion of fuels in mechanical work (Mathur and Das, 1991).

Compared to the fuels now in use or under considration, for future application, hydrogen offers many advantages. Its use in spark ignition engine will not only eliminate the present day proplem of dependence on petrolium fuel, but it will also reduce vehicular pollution as hydrogen is a clean burning fuel. It offers the unique advantage of being a fuel, the basic resourse of which is recycable in a short time cycle by completely normal means. It starts with the molecule of water being split and upon combustion produces water vapour as the prencipal exhuast. Water is available in plenty every where. So, looking at the future, hydrogen has a practically unlimited supply potential (Chaichan, 1989).

As a fuel gas, hydrogen possesses significant invironmantal advantages that compensate for preliminary reservation as asociated with the controversial issue of unproven safety. In comparission with natural gas, hydrogen possesses a higher burning velocity, greater flash back tendency, lower relative density, wider limits of flammability and lower ignition energies, selected combustion characteristics are reported in Table (1) (Petkov and Parazev, 1987).

There is general agreement that the hydrogen enrichment concept permets very lean combustion of hydrocarbon fuels with attendant increase in engine efficiency and reduction of engine emissions. It is an opportunity to achieve now adays standards of toxic components content in the exhaust gases of automobile engines, considerably lowering gasoline consumption.

Another advantage of this method is that it requires a smaller quantity of hydrogen to be fed to the engine which considerably lessens the problems connected with hydrogen storage in the automobile (Frances, 1981).

It has been well established that burning lean mixtures results in improved fuel economy and higher engine thermal efficiency. Moreover, the lean operation of gasoline fueled spark ignition engines can result in the reduction of exhaust emissions without the addition of emission control devices (Hoen and Dowdy, 1973).

Recently much attention has been focussed on the use of hydrogen as a supplementary fuel, to extend the engine operation in range to equivalence ratios beyound the lean operating limit of gasoline, as hydrogen exhibits a significantly lower flammability limit (around 0.1 equivalence ratio). Comparasion with other hydrocarbon fuels (around 0.6 equivalence ratio). However, no conventional engine system has been developed that can operate with gasoline at equivalence ratios leaner than 0.85 or so, while the lean limit of gasoline- air combustion is about 0.6 . There are
several reasons for this but perhaps the two most important are non-homogenity of the mixture and poor cylinder to cylinder distribution (Hoen and Baisly, 1973).

The presence of hydrogen during the ignition and initial phases of the combustion process provides a source of enthalpy release and active species of equivalence ratio where gasoline fuel alone isn't readily reacted and for these reasons hydrogen is the prime candidate for gasoline supplementation to obtain ultralean burning. Table (2) (Bansal and Mathur, 1980) shows a comparison of flammability limit of hydrogen with other commenly used hydrocarbon fuels.

## EXPERIMANTAL TECHNIQUE

Experiments were conducted on single cylinder, variable compression ratio Ricardo E6/US engine, to assess the effect of hydrogen supplemintation on the operation of SIE.

Tests were also conducted to determine the engine output and fuel economy with gasoline and with various degrees of hydrogen supplementation. Mixture equivalence ratios were varid over a wide range while hydrogen volumatric fraction (defined as the ratio of the hydrogen volume to the total volume of hydrogen and gasoline used, that's mean $\mathrm{HVF}=\mathrm{V}_{\mathrm{H} 2} / \mathrm{V}_{\mathrm{H} 2}+\mathrm{V}_{\text {gasoline }}$ ) varid from $20 \%$ to $100 \%$ hydrogen. HUCR and OST were used in studing wide range of equivalence ratios. All tests were carried out at wide open throttle and at engine speed 25 rps , except those for studying speed effect. In all experiments bottled hydrogen was used as a supplemantary fuel.

## DISCUSSION

## Compression ratio effect

Supplimentation of different volume fracters was studied, the different fractions were used to know which percentage was the best one to mix the two fuels, the CR was studied also to assess the HUCR. The experiments was started at $\mathrm{CR}=6: 1$ untill $\mathrm{CR}=9.5: 1$.

Fig. (1) shows the relation between the brake power and equivalence ratio $\left[(A / F)_{\text {stoichiometric }}\right.$ $/(\mathrm{A} / \mathrm{F})_{\text {actual }}$ for different mixing volume fractions from 0 to $100 \%$ hydrogen at HUCR for each fuel, OST and 25 rps speed.

The experiment showed that brake power increased with HVF increase from 0 to $80 \%$ for compression ratios $(6,7,8,8.5,9)$, and for volumatric fraction ( $0-60 \%$ ) at $\mathrm{CR}=9.5$, this increase in brake power was expected because hydrogen presence in combustion chamber gives significant improvment in energy release.

Also, it increase burning rate and gives better and more complete combustion. The brake power was reduced when HVR was increased above $80 \%$, that's because a higher fraction of gasoline-air mixture was replaced with hydrogen that caused decreasing in combustion energy released, where hydrogen energy on volume basis is less than the gasoline heating value. This is obvious when hydrogen was used alone, it gave brake power less than that produced when using gasoline alone, as appear from the figure. The mixture behaviour at $\mathrm{CR}=9.5$ was different from other compression ratios, because at this CR the combustion was rough and severe knock happened with increased load.

Fiq. (2) distincts realation between HVF and the highest brake power of the engine at different compression ratio in the experments done. Fig. 2 shows that HUCR for mixtures of hydrogen and gasoline is 9 while it was 8 only for gasoline-air mixture. The highest brake power happened at $80 \%$ mixture rate.

Fig. (3) shows the effect of different mixture rates and the studied CR on OST.
It appeared that ther OST retarted with HVF and compression ratio increase. This is because of high hydrogen burning velocity in comparable with gasoline, also burning velocity increase with CR increase, because the mixture temperature increased in combustion chamber.

## Equivalencr ratio effect

From Fig. 1 the highest brake power when gasoline was used alone was at $\varnothing=1.1$, with hydrogen supplemintation it was approach to $\emptyset=1.0$. The hydrogen addition effect was bigger in the lean side, where the flammability limit for gasoline was at $\emptyset=0.79$ but with hydrogen addition it reached $\emptyset=0.34$.

Fig. (4) shows the relation between brake power and HVR in mixture for five equivalence ratios at OST and 25 rps engine speed and HUCR for each fuel.

The figure shows that the brake power increased at $\emptyset=0.7$ when HVF was increased from 0 to 80 is very large, the brake power was increased about $300 \%$ compared with gasoline alone, the same thing can be said about $\emptyset=0.8$, where the brake power increased about $40 \%$, this is because of three facters: precence of enough oxygen for reaction, precence of hydrogen which improves the combustion, and increase its burning velocity, and the precence of high heating value of gasoline.

The effect of addition of hydrogen at richer equivalence ratio is limited, because the intering air quantity decreased, while the intering hydrogen-gasoline mixtue removed developed volume from air. This is obvious at $\emptyset=1.0$, where brake power increased with $10 \%$, also, at $\varnothing=1.1$ the increase was about $3.5 \%$.

From the above it is appeared that hydrogen supplementation improves engine brake power for lean equivalence ratios in great manner.

The relation between equivalence ratio and OST is shown in fig. (5) for different mixing rates, at HUCR and 25 rps , where fig. (6) shows the effect of HVF on OST for difined equivalence ratios.

The OST retarted with hydrogen addition for all equivalence ratios, it was about 20 degree BTDC with $80 \%$ volume hydrogen, at stochiometric equivalence ratio about 10 degrees BTDC.

The effect of HVF addition to gasoline on bsfc was studied in fig. (7) for wide range of equivalence ratios at HUCR, 25 rps and OST.

From the figure, the bsfc decreased to a concedarable extent, especiely for lean equvilence ratios with hydrogen supplemintation, for example, at $\emptyset=0.7$ with $\mathrm{HVF}=80 \%$, bsfc reduction was about $67 \%$, and at $\varnothing=1.0$ for the same HVF the reduction was $17 \%$.

Fig. (8) shows the effect of hydrogen addition on indicated thermal efficiencyat HUCR and OST, for three chosen HV fractions.

The indicated thermal efficiency increased highly with hydrogen supplementation at lean side to reach its highest value at this side, then it decreased quickly with mixture enrichment, the rise of indicated thermal efficiency in the lean side presents important and obvious improvement in combustion at this side with hydrogen adittion. The high reduction in indicated thermal efficiency at rich equivalence ratios after it reached its highest value is because of combustion difficulties in this side, so, the hydrogen supplementation in the rich side didn't improve the combustion nor the indicated thermal efficiency.

The highest value of indicated thermal efficiency was at lean equivalence ratios, this ratio decreased with hydrogen addition to gasoline-air mixture, as an example, the highest indicated thermal efficiency was at $\varnothing=0.9$ when using gasoline, then it became at equivalence ratios ( $\varnothing=0.83,0.8,0.77$ ) for supplying ratios ( $\mathrm{HVF}=0.3,0.6,0.8$ ) respectively, also, when using hydrogen it was at $\varnothing=0.4$.

Fig. (9) indicates the relation between exhuast gas temperatures and equivalence ratio, when adding different hydrogen volumatric fractions ( $\mathrm{HVF}=0.3,06,0.8$ ), engine was operated at HUCR and 25 rps .

Hydrogen supplimantation decreases exhaust gas temperature for all equivalence ratios, and we got the minimum exhust gas for the whole range of equivalence ratios temperature when hydrogen was used. This was explained by (Al-Alousi, 1982), that the hydrogen heating value on volume basis is low, so it cuases this reduction in temperature, also it can be explained in another way, where the burning velocity for hydrogen is fast, and the mixture combusted in very high speed, especialy when engine operated at OST, so when expansion stroke takes place the whole mixture will be burned and became combusted gases, and it will be cooled in this stroke, and when exhuast
valve opened these gases will get out cooler than any hydrocarbon fuels may be used, also the heat transfer from cylinder wall increased because of the reduction of unburned gases in the inner film thickness, which are near the cylinder walls as sugested by (Chaichan, 1989).

## SPEED EFFECT

Fig. (10) represents the relation between the highest engine brake power and HVF in mixture, to obtain different speed effects at HUCR and OST.

It is appeared that the effect of engine speed is invariable when using any fuel alone. The brake power increased with speed increase, for all experiment speeds, although the increase rate is different this increase was too large when engine speed accelerate from low to meduim speeds, then this rate lessened when engine run from meduim to high speeds. This is because of the inlarged friction power with engine speed.

Fig. (11) shows the effect of supplementary hydrogen on OST when the engine run at different speeds. Hydrogen supplementation caused retarding OST about 20 degrees BTDC, for all experiment speeds. Also, the speed increase cuased advancing of OST, as it is familiar when working with any fuel alone, and the optimum spark timing at any speed and equivalence ratio is the resultant of these two parameters.

## SPARK TIMING EFFECT

Figs. (12 to 14) represent the relation between engine brake power and equivalence ratio for three different spark timings $(10,15,20)$ degree BTDC, with hydrogen addition to gasoline in three different volumatric percentage ( $\mathrm{HVF}=.3, .6, .8$ ), the engine operated at HUCR and 25 rps .

Spark timing 10 degrees BTDC is very late for gasoline as appears from Fig. (12), where engine brake power went down, but with hydrogen supplementation the brake power became larger in very obvious manner, especiely for equivalence ratios from $\emptyset=0.7$ to $\emptyset=1.1$, where this timing is neer the OST.

Spark timing 15 degrees BTDC is a better timing for gasoline, so the brake power increased for all equivalence ratios as appears in Fiq. (13), also brake power increased clearly with hydrogen added to mixturs at $30 \%$ volumatric fraction for equivalence ratios from $\emptyset=0.7$ to $\emptyset=1.3$. The brake power increased also with hydrogen supplied to system at $60 \%$ by volume, but a smaller increase for the same equivalence ratios mitioned above, that is because the timing is advanced compared with OST for these equivalence ratios, but when hydrogen was supplied to system in $80 \%$ volume, the brake power increased in lean side, and decreased for equivalence ratios between ( $\varnothing=0.75-1.3$ ), and the curves take another figures. This was expected because this timing is highly advanced timing from OST for these equivalence ratois.

Brake power figures take another style from their relatives in Fig. (14). Gasoline brake power became better, that's because the timing ( 20 degrees BTDC) close to OST, and the equivalence ratios which gave the highest brake power were between $\varnothing=1.0-1.15$. Brake power decreased with hydrogen addition in $30,60 \%$ by volume for range of ( $\varnothing=0.85-1.35$ ), and engine operation was not available for $\mathrm{HVF}=80$, at this fraction and for this spark timing, because it considerd very advanced from OST for these equivalence ratios, so it caused reduction in brake power for $\mathrm{HVF}=0.3-0.6$, and caused the phenomenant of the high pressure rate before top dead centre to occur, which cause negative work on engine.

## CONCLUSIONS

1-The HUCR for a mixture of gasoline and hydrogen is 9:1.
2-The OST retards with hydrogen supplementation for all equivalence ratios.
3-The OST retards with CR increase for all kind of fuels.
4-The OST advanced with speed increase for all kinds of fuels.

5-With hydrogen supplied in volumatric fractions to gasoline-air mixture the brake power increased to extend limit ( $\mathrm{HVF}=80 \%$ ) then it started to fall down if HVF continue increasing above this percentage.
6-With hydrogen supplementation engine can operate with very lean equivalence ratios, can't be reached with gsoline operation.
7-Indicated thermal efficiency increased with hydrogen supplementation, it's highest value when using hydrogen alone, at very lean equivalence ratio.
8 -Exhaust gas temperature reduced with hydrogen supplementation.
9 -Brake specific fuel consumption reduced with hydrogen supplimantation to gasoline.

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## NOMENCLATURE

TDC top dead centre
BDC bottom dead centre
BMEP brake mean effictive pressure
BSFC brake specific fuel consumption
BTE brake thermal efficiency
CA crank angle
CR compression ratio
HUCR higher usful compression ratio
OST optimum spark timing
SIE spark ignition engine

Table (1)

## Combustion characteristics for gasous hydrogen

| Ignition energies ( at 1 atm and 298 K ) |  |
| :---: | :---: |
| $\mathrm{E}_{\text {min at stoicheometric }}$ | 0.019MJ |
| Critical $\mathrm{E}_{\text {min }}$ | 0.0185 MJ |
| Auto-ignition temperature ( at 1 atm and room temperature) | 847-864 K |
| Quinching distance (at 1 atm and 298 K ) |  |
| Critical port at stoichiometric | 0.64 mm |
| Slotted point at stoichiometric | 0.81 mm |
| Limit of flammability (at 1 atm and 298K) |  |
| Lower limit | 4.0\% |
| Upper limit in air | 75.0\% |
| Upper limit in oxygen | 94.0\% |
| Limit of detonability (at 1 atm and room temperature) |  |
| In air | 18.3-59.0\% |
| In oxygen | 15.0-90.0\% |
| Detonation velocity (at 1 atm and 291K) |  |
| In air | 2055 m/s |
| In oxygen | $2819 \mathrm{~m} / \mathrm{s}$ |
| Maximum flame temperature ( at 1 atm and room temp) |  |
| In air | 2318 K |
| In oxygen | 2933 K |

Table (2)
Lean flammability limits for gases and vapors in air

| Compound | formula | Lean flammibality limit |  |
| :--- | :---: | :---: | :---: |
|  |  | $\mathrm{Vol} \%$ |  |
| $\emptyset$ |  |  |  |
| Paraffins <br> Methane <br> Propane <br> Pentane <br> octane | $\mathrm{CH}_{4}$ | 5.3 | 0.53 |
| Aromatics <br> Benzene | $\mathrm{C}_{3} \mathrm{H}_{8}$ | 2.2 | 0.54 |
| Alcohols <br> Meathanol | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 1.5 | 0.58 |
| Inorganic <br> CO+ $\mathrm{H}_{2} \mathrm{O}$ vapor |  |  |  |
| at 18 |  |  |  |
| Hydrogen | $\mathrm{CO}_{6} \mathrm{H}_{6}$ | 1.0 | 0.60 |
| Indoline 30 gasoline | $\mathrm{CH}_{3} \mathrm{OH}$ | 1.4 | 0.51 |



Fig. (1). The relation between the brake power and equivalence ratio for different mixing volume fractions from 0 to $100 \%$ hydrogen at OST and 25 rps speed


Fig. (2). The realation between HVF and the highest brake power of the engine at every compression ratio in the experments done


Fig. (3).The effect of different mixture rates and the satudied CR on OST


Fig. (4). The relation between brake power and HVR in mixture, for five different equivalence ratios at OST and 25 rps engine speed, and HUCR for each fuel


Fig. (5). The relation between equivalence ratio and OST, for different mixing rates, at HUCR and 25 rps


Fig. (6). The effect of HVF on OST for difined equivalence ratios


Fig. (7). The effect of HVF addition to gasoline on bsfc was studied for wide range of equivalence ratios at HUCR, 25 rps and OST


Fig. (8). The effect of hydrogen addition on indicated thermal efficiency, at HUCR and OST, for three chosen HV fractions


Fig. (9).The relation between exhuast gas temperature and equivalence ratio when adding different hydrogen volumatric fractions ( $\mathrm{HVF}=0.3,06,0.8$ )


Fig. (10). The relation between the highest engine brake power and HVF in mixture, to obtain different speed effects at HUCR and OST


Fig. (11). The effect of supplementary hydrogen on OST, when the engine run at different speeds


Fig. (12). The relation between engine brake power and equivalence ratio for spark timing 10 degrees BTDC


Fig. (13). The relation between engine brake power and equivalence ratio for spark timing 15 degrees BTDC


Fig. (14), The relation between engine brake power and equivalence ratio for spark timing 20 degrees BTDC

# FRICTION AND WORN SURFACE TOPOGRAPHICAL FEATURES OF AS-CAST, MODIFIED AND HOMOGENIZED ALUMINUM-SILICON ALLOYS 

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#### Abstract

The coefficient of friction was experimentally calculated for aluminum-silicon alloys by connecting a strain gauge to the arm of pin-on-disc wear machine in order to take microstrain readings from the strain-meter. As-cast and modified aluminum-silicon alloys were thermally homogenized for long periods of time (1-40hr) in order to study the effect of homogenization on friction. Scanning electron microscopy was successfully used to build up the mechanism of surface damage during sliding. The results showed that the coefficient of friction was increased with increasing bearing pressure for as-cast, modified and homogenized aluminum-silicon alloys. Thermal homogenization led clearly to remarkable changes in the frictional behavior of as-cast and modified aluminum-silicon alloys. Many mechanisms were responsible for aluminum-silicon alloys surface damage during sliding.


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تم حساب معامل الاحتكاك عمليا لسبائك الالمنيوم-سليكون من خاله ربط مقياس الانفعال بجهاز
البلى الالتصاقي لغرض تسجيل قر اءات الانفعال المايكروية . اجريت المجانسة الحرارية لسبائك الالمنيوم-
سليكون المصبوبة والمحورة لفترات زمنية طويلة (1-40 ساعة) لغرض در اسة ناثير ها على الاحتكاك.
استخدم الهجهر الالكتروني الماسح بنجاح لغرض دراسة تضرر المنطقة السطحية اثثاء الانز لاق. اوضحت
النتائج زيادة معامل احتكاك بزيادة ضغط التحميل لجميع السبائك المصبوبة والمحورة والمجانسة. ادت
اللجانسة الحرارية الى تغيرات واضحة في السلوك الاحتكاكي لسبائك الالمنيوم-سليكون المصبوبة
    و المحورة. اسهوت العديد من الاليات في تضرر سطح سبائك الالمنيومهسليكون اثثاء الانز لاق.
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Key Words: Friction and Worn Surfaces, Al-Si Alloy, Topographical Features, As-Cast

## INTRODUCTION

Friction can be defined as a resistance to motion occurring during tangential displacement of contact surfaces in the real area of contact under applied force (Halling 1979 and Rigney 1981). Components used in tribological applications are exposed to friction during their work (Nayak 2004 and Zhang 2004). One of the mostly used alloys in tribological applications is aluminumsilicon because of its good wear resistance, high strength to weight ratio, good corrosion resistance
and good castability and machinability (Granger 1988 and Polmear 1989). Many investigators studied the friction property not only for aluminum-silicon alloys but also for other materials. (Sarkar and Clarke 1980 and 1982) found that the frictional resistance fluctuated violently for most as-cast and age hardened aluminum-silicon alloys, indicated stick-slip and suggested plastic interaction but correlation between surface damage and magnitude of friction could not be found. (Sakamoto and Tsukizoe 1978) found that the metal transfer from the soft metal to hard asperities in contact with it caused significant changes in the shape, size and height distribution of the asperities which led to reduce the effect of the initial surface roughness of the hard metal during friction. Consequently the friction force became less dependent on the surface roughness than it did when no metal transfer occur. (Mahdavian and Mai 1984) studied the variation in friction coefficient with sliding distance for similar and dissimilar metals. They found that for similar metals sliding on each other there was a significant contribution to friction owing to severe ploughing while for dissimilar metal, the coefficient of fiction was determined primarily by the way metal transfer occurred between sliding surfaces. (Prasad and Mecklenburg 1993) found that no significant differences in the friction behavior of the $\mathrm{Al}_{2} \mathrm{O}_{3} \cdot \mathrm{SiO}_{2}$ and $\mathrm{Al}_{2} \mathrm{O}_{3}$ fiber-reinforced aluminum metal-matrix composite (MMC) and unreinforced alloy when metallugraphically polished samples were used. They also found that when the surface of the MMC was etched, the friction coefficient dropped to a low value of 0.18 and the stick-slip type behavior disappeared. The addition effect of different lead percentages to aluminum-silicon alloys on friction properties was studied by (Pathak et al. 1997). They found that the addition of lead was reduced the interfacial friction and improved the ability of aluminum-silicon alloys to resist seizure. A lower friction coefficient and higher seizure load were obtained for Al- $\mathrm{Si}-\mathrm{Pb}$ alloys bearing in semi-dry sliding conditions compared with those observed for dry conditions.

The aim of this work is to study the frictional behavior of as-cast and modified aluminumsilicon alloys with titanium. The effect of thermal homogenization with different time periods for aluminum-silicon alloys on frictional behavior is also studied.

## MATERIALS AND METHODS

Binary $\mathrm{Al}-12 \% \mathrm{Si}$ alloy was prepared by adding small quantity of pure aluminum to $\mathrm{Al}-13 \% \mathrm{Si}$ master alloy. Titanium was added to $\mathrm{Al}-12 \% \mathrm{Si}$ alloy in different percentages ( 0.05 and $0.1 \% \mathrm{Ti}$ ) after putting it in an aluminum foil and inserting it to the molten $\mathrm{Al}-12 \% \mathrm{Si}$ alloy with good mixing ( 10 min in time) to ensure solubility and distribution of titanium in the alloy matrix. All alloys were melted in an alumina crucible by using a gas fired furnace. Then these alloys were poured in a preheated carbon steel die ( $300 \mathrm{C}^{\circ}$ ) to ensure no chilling occurring to these alloys after solidification. The ingots samples produced from casting process have 15 mm diameter and 100 mm length. The chemical composition of pure aluminum, master alloy and prepared aluminumsilicon alloys are illustrated in Table 1. All alloys were thermally homogenized at $525 \mathrm{C}^{\circ}$ with different time periods ( $1-40 \mathrm{hr}$ ) to increase the coherency between silicon particles and aluminum matrix.

Coefficient of friction was measured by taking the microstrain readings from the strain-meter. The strain-meter was connected to the arm of pin-on-disc wear machine through a strain gauge, in which the specimen has been supported. The time of each test was 30 min , in in which the coefficient of friction for each test represents the average value during the test. All specimens were dry slided on a 45 HRC carbon steel disc to make contact with other material.

## RESULTS AND DISCUSSION

The frictional behavior of as-cast and modified Al-Si alloys
The relationship between bearing pressure and coefficient of friction ( $\mu$ ) Fig. 1 reveals that the coefficient of friction increases with increasing bearing pressure due to increased interaction and
cold welding between the asperities of pin surface and counterface. This means that the surface damage is greater due to tangential traction. Since, strong welds and interaction between the asperities should also mean a high value of friction coefficient because the shear force required to distangle the interaction and cold welding between these asperities is greater in order to make sliding continuous. Fig. 1 also shows that $\mathrm{Al}-12 \% \mathrm{Si}$ alloy has a lower coefficient of friction in comparison with the other alloys containing titanium, while the coefficient of friction of the alloy containing $0.1 \% \mathrm{Ti}$ approached the coefficient of friction of $\mathrm{Al}-12 \% \mathrm{Si}$ at high bearing pressure. This approach relies on the wear rate, in which the coefficient of friction increases linearly with wear rate (Mitchell 1976). The wear rate of Al-12\%Si alloy is lower in comparison with the other alloys containing titanium (Subhi 2000)., therefore Al-12\%Si alloy has a lower coefficient of friction. Fig. 2 shows the relationship between sliding distance and coefficient of friction of aluminum-silicon alloys. The figure shows that all alloys have two types of friction coefficient. The first is static and the other is dynamic coefficient of friction. Generally, the static coefficient of friction was greater than the dynamic coefficient of friction for all aluminum-silicon alloys. This is because the asperities are interacted before sliding under applied bearing pressure, and when sliding begins, they need high shear forces to distangle them to make sliding continuous. After increasing the coefficient of friction in the early stage of sliding, its magnitude gradually decreases due mainly to reduction in ploughing action by transfer of material from the aluminum-silicon alloy pin surface to the counter asperities, leading to an increase in the tip angle of the asperities. Under steady state sliding, the dynamic coefficient of friction becomes approximately constant with fluctuation in its magnitude. (Mitchell and Osgood 1976) found that this fluctuation depends on the fluctuation in friction force resulted from changes in the number of contacts as well as from changes in the proportion of the welded contacts. (While Blau 1981) introduced a comprehensive picture to this fluctuation in which it coincides with the present work. Blau found that the friction depends on many processes as (1) metal transfer (2) film formation and removal (3) debris generation and (4) cyclic surface deterioration. It has bean also shown from Fig. 2 that $\mathrm{Al}-12 \% \mathrm{Si}$ alloy has a lower static and dynamic coefficient of friction compared with other alloys containing titanium. This is because the coefficient of friction depends on the wear rate (Mitchell 1976).

## The frictional behavior of homogenized Al-Si alloys

Thermal homogenization affected the magnitude of friction coefficient and this effect is dependent on the thermal homogenization time. The relationship between bearing pressure and coefficient of friction of homogenized aluminum-silicon alloys Figs.3-5 showed that the homogenization for 1 hr led to increasing the coefficient of friction for all homogenized aluminumsilicon alloys in comparison with its magnitude in the as-cast and modified aluminum-silicon alloys. This is because the ductility of homogenized aluminum-silicon alloys for 1 hr was increased as a result of internal stresses relief, led to increase the interaction and cold welding between the asperities of pin surface and counterface. Since, the wear mechanism appeared with increasing bearing pressure as interaction between the asperities, and galling as a result of incomplete cold welding during sliding [Subhi 2000]. This demonstrates our explanation in which the increasing coefficient of friction accompany with increasing bearing pressure. With increasing thermal homogenization greater than $1 \mathrm{hr}(5-40 \mathrm{hr})$, the coefficient of friction decreased. This is because the coefficient of friction depends on the wear rate (Mitchell 1976). Decreasing in the wear rate occurred with increasing thermal homogenization time greater than 1 hr (Subhi 2000), therefore, coefficient of friction decreases with increasing thermal homogenization time in comparison with its magnitude at 1 hr . The frictional behavior of homogenized alloys was similar to that of as-cast and modified aluminum-silicon alloys in which the two types of friction coefficient were present regardless of its magnitude, therefore, there is no need to re-explain the frictional behavior during sliding of homogenized alloys at constant bearing pressure.

## The study of worn surface

Fig. 6 shows the worn surface of as-cast and modified aluminum-silicon alloys where different mechanisms contributed in surface damage during sliding. The predominant mechanism is dependent on the alloy composition and bearing pressure. The worn surface of $\mathrm{Al}-12 \% \mathrm{Si}$ alloy revealed that there were many mechanisms responsible for material removal. It has been shown that there was spalling in the worn surface, leading to a large pit formation, as well as there were many subsurface cracks sheared to the surface which were responsible for wear particles formation. These wear particles can be recognized clearly in the worn surface of the alloy containing $0.05 \% \mathrm{Ti}$. It has been shown that there were many wear small particles on the surface removed from the surface during sliding. The same wear particles can be shown in the worn surface of the alloy containing $0.1 \% \mathrm{Ti}$. These small particles were removed by secondary delamination. Secondary delamination is distinguished by craze cracking. (Clarke and Sarkar 1981) found that this secondary delamination may be a function of surface forces only and may have nothing to do with probable subsurface cracking responsible for primary delamination.

The wear mechanisms remained the same for homogenized aluminum-silicon alloys, but in different degrees. The worn surface of homogenized Al-12\%Si alloy Fig. 7 shows that there were many surface cracks due to surface traction. These surface cracks were responsible for material removal by secondary delamination. The worn surface of homogenized alloy containing $0.05 \% \mathrm{Ti}$ shows advanced stage in subsurface crack growth sheared to the surface. There are many surface cracks in the worn surface of homogenized alloy containing $0.1 \% \mathrm{Ti}$, as well as many small particles compacted on the surface due to the action of bearing pressure in which these small particles delaminated by secondary delamination.

## CONCLUDING REMARKS

1-The coefficient of friction was increased with increasing bearing pressure for as-cast, modified and homogenized aluminum-silicon alloys.
2-Two types of friction coefficient were present, static and dynamic regardless of the magnitudes of these two coefficient types.
3-Thermal homogenization at 1 hr led to an increase in the coefficient of friction in comparison with its magnitude for as-cast and modified aluminum-silicon alloys, while increasing thermal homogenization time greater than $1 \mathrm{hr}(5-40 \mathrm{hr})$ led to a decrease in the coefficient of friction in comparison with its magnitude at 1 hr .
4-Many mechanisms were responsible for surface damage during sliding. The predominant mechanism was dependent on the alloy composition, bearing pressure and thermal homogenization time.

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Table. 1 Chemical composition of pure aluminum, master alloy and prepared aluminumsilicon alloys.

| Materials |  | Composition (\%) |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathbf{C u}$ | $\mathbf{M g}$ | $\mathbf{T i}$ | $\mathbf{A 1}$ |  |
| A 1 | 0.113 | 0.008 | 0.008 | 0.008 | Remainder |  |
| $\mathrm{A} 1-13 \% \mathrm{Si}$ | 13.00 | 0.02 | 0.007 | 0.004 | Remainder |  |
| $\mathrm{A} 1-12 \% \mathrm{Si}$ | 12.23 | 0.02 | 0.005 | 0.035 | Remainder |  |
| $\mathrm{A} 1-12 \% \mathrm{Si}-0.05 \% \mathrm{Ti}$ | 12.10 | 0.02 | 0.007 | 0.045 | Remainder |  |
| $\mathrm{A} 1-12 \% \mathrm{Si}-0.1 \% \mathrm{Ti}$ | 13.33 | 0.02 | 0.007 | 0.108 | Remainder |  |



Fig.(1). The relationship between bearing pressure and coefficient of friction of as-cast and modified aluminum-silicon alloys.


Sliding distance, $\mathbf{c m \times 1 0}{ }^{-4}$
`Fig. 2 The relationship between sliding distance and coefficient of friction of as-cast and modified aluminum-silicon alloys.


Fig. 3 The relationship between bearing pressure and coefficient of friction of homogenized Al-12\%Si alloy.


Bearing pressure, $\mathrm{N} \mathrm{m}^{-2} \times 10^{-3}$

Fig. 4 The relationship between bearing pressure and coefficient of friction of homogenized Al-12\%Si-0.05\%Ti alloy.


Fig. 5 The relationship between bearing pressure and coefficient of friction of homogenized Al-12\%Si-0.1\% Ti alloy.

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| :--- | :--- | :--- |



Al-12\%Si-0.05\% Ti

$\mathrm{Al}-12 \% \mathrm{Si}-\mathbf{0 . 1} \% \mathrm{Ti}$

Fig.(6). Secondary electron images of freshly worn surfaces of as-cast and modified aluminum-silicon alloys. Bearing pressure, 168.6 kPa ; sliding speed, $160.2 \mathrm{~m} \mathrm{~min}^{-1}$. Arrow indicates sliding direction.


Fig.(7). Secondary electron images of freshly worn surfaces of homogenized aluminum-silicon alloys at 40 hr . Bearing pressure, 168.6 kPa ; sliding speed, $160.2 \mathrm{~m} \mathrm{~min}^{-1}$. Arrow indicates sliding direction.

# STRATIFIED WATER-OIL-GAS FLOW THROUGH HORIZONTAL PIPES 

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#### Abstract

Stratified three-phase flow through horizontal pipe has been studied experimentally. The fluids used in the system are water, kerosene, and air. A closed loop flow system, which composed of 0.051 m inside diameter and 4 m length test pipe, is designed with facilities for measuring flow rate, pressure drop and thickness of each phase.

The effects of gas, liquid flow rates and water liquid ratio (WLR) have been experimentally observed. It was found that liquid (water, and oil) thickness decreased when the gas flow rate is increased with constant liquid flow rate, and increased when the liquid flow rate is increased at constant gas flow rate. Pressure drop increased when the gas and/or liquid flow rate is increased.


Three equations have been formulated, using the experimental data of the present work, to predict liquid, water thickness and system pressure drop in stratified three-phase flow in horizontal pipe. High correlation coefficients are obtained for these equations.

The experimental results are compared with the results obtained from three-phase model of Taital, Barnea, \& Brill (1995). The comparison showed that the predicted data which obtained from three-phase flow model Taital et al. (1995) is in good agreement with experimental data.

## الجريـان الطباقي للماء والنفط والغاز خلال الانابيب الافقية

الاكتورة سميرة محمد حمد الله

الاستاذ الاكتور زياد عبد الرزاق اسود
اللبيد فانز هادي رشيد الزبيدي
الخلاصة

تمـت در اسـة الجريـان الطبقي ثلاثـي الأطوار خـلال الأنابيب الأفقــة مختبريـا. الموائـع المستخدمة فـي المنظومة هي : الماء, النفط الأبيض و الهواء وباستخدام أنبوب فحص قطره 0.05 م وطولـه 4 م ليتم حساب: معدل جريان الموائع , هبوط الضغط في المنظومة , و سمك كل طور .

تأثنيرات معدل جريان الغـاز و السـائل هي المدروسـة لمعرفـة تأثثير هـا على سـك الأطوار السـائلّة حيث وجد أن سمك أي طور من الأطوار السائلة (ماء - نفط) يقل عند زيادة معدل جريـان الغـاز عنـد ثبوت جريـان السائلل , ور
 عندما يزداد معدل جريان الغاز و/ أو يزداد معدل جريان السائل.

تم صـياغة ثلاثـة معادلات لتمثيـل النتائج المختبريـة : معادلـة تقوم بحساب سـك السائل الكلـي ومعادلـة لحساب سمك الماء و معادلة لحساب هبوط الضغط للجريان الطبقي ثلاثي الأطوار في الأنابيب الأفقيـة و هذه المعـادلات أظهرت تمثيلا جيدا للنتائج المختبرية .


## INTRODUCTION

Three-phase gas-oil-water flow commonly occurs in the petroleum industry. Perhaps the most relevant practice is the transportation of natural gas-oil-water mixtures through pipelines. Three-phase flow may also be encountered in pumping system, especially in surface gathering lines, and in well-bores and gas lift wells which produce water along with oil and gas. In off-shore and remote well sites, it is often intractable to separate oil and gas there. The transportation of oil and gas in multiphase pipelines is therefore becoming more common. The oil-water-gas mixtures produced are transported many kilometers to platform or central gathering stations where the fluids are separated.

Water production often increases significantly during the latter stage of a well and use of the conventional approximations of a two-phase oil-gas system neglecting the water, or combining the oil and water into a liquid phase, often becomes inaccurate.

There have been numerous investigations of two-phase flow regimes; in contrast, threephase flow regimes have not been studied thoroughly. Because of the abundance of three-phase flow applications in the petroleum and chemical industries, a better understanding of this complex flow phenomenon is needed.

## PURPOSE OF STUDY

The main purpose of this study is to investigate the pressure drop of the system and the levels of the liquid layers (water and oil) and the gas layer experimentally. Flow pattern map have been constructed for $50 \%$ water liquid ratio (WLR). Three empirical correlations have been developed for predicting liquid, and water thicknesses and pressure drop in three-phase stratified flow in horizontal pipes. The experimental data have been compared with the theoretical data of three-phase model of Taital et al. (1995).

## FLUID PHYSICAL PROPERTIES

The physical properties of the liquid and gas phases are determined from laboratory measurements at atmospheric pressure and temperature of $12^{\circ} \mathrm{C}$. These properties are shown in Table (1): -

Table (1): physical properties of water, oil, and gas

|  | Water | Oil (kerosene) | Gas (air) |
| :---: | :---: | :---: | :---: |
| $\rho\left(\frac{K g}{m^{3}}\right)$ | 1000 | 775 | 1.22 |
| Viscosity <br> $\mu($ Pa.s $)$ | 0.001141 | 0.00127875 | 0.000018 |

## EXPERIMENTAL FACILITIES AND TEST PROCEDURE

The experiments were conducted in horizontal three-phase flow loop as shown in Fig (1). Three kinds of phases are used in this study (water, kerosene and air). The individual phase of oil and water are pumped from their individual tank $\left(0.15 \mathrm{~m}^{3}\right)$ into 1 inch ID pipe. A two centrifugal pumps with maximum flow of ( $4 \mathrm{~m}^{3} / \mathrm{hr}$.) is used to pump the two immiscible liquid (oil and water) to the mixing tee (mixing tank) at the up stream of test section. The water and oil flow rate are measured by flow meter. The gas from compressor with maximum flow rate of $\left(16 \mathrm{~m}^{3} / \mathrm{hr}\right.$.) is also passed into the mixing tank. Its flow rate is measured by flow meter.

The gas-oil-water mixture from the mixing tank flow into a ( 0.051 mm ) internal diameter, and ( 4 m ) long Plexiglas pipeline (transparent pipe), where the flow patterns are observed visually. The water and oil film thickness are measured by using a rule which was parallel with vertical diameter. The multiphase mixture is discharged into a $\left(0.768 m^{3}\right)$ separator. The gas is discharged from the top to the atmosphere. The oil-water mixtures settle and separate into individual phases and return to their respective tank. The majority of the experiments were carried out in the system which operated at atmospheric pressure and temperature of $\left(12^{\circ} \mathrm{C}\right)$. It should be noted that because of the waves at the gas-oil interface, the measurements obtained from these experiments did not provide a precise estimate of the film thickness. Only a range for the film thickness could be determined.


Fig. (1) Three-Phase Flow Loop

## RESULTS

In this study, the effect of liquid (oil \& water) and gas flow rates, and pressure drop have been studied experimentally. Flow pattern maps have been constructed for $50 \%$ WLR. Then experimental results are compared with Three-phase mechanistic model of Taital et al. (1995) for predicting liquid, water, and oil thickness and system pressure drop.

## The Effect of Gas Flow Rate on Dimensionless Thickness

Figure (2) show the effect of liquid and gas flow rates on dimensionless liquid thickness $\left(h_{L} / D\right)$. For constant liquid flow rate there is an inversely proportional relationship between dimensionless liquid thickness $\left(h_{L} / D\right)$ and gas flow rate (vsg). A proportional relationship is observed between ( $h_{L} / D$ ) and liquid flow rate (vsl) for constant gas flow rate.

The same results are obtained when plotting $\left(h_{w} / D\right)$ or $\left(h_{o} / D\right)$ instead of $\left(h_{L} / D\right)$ as shone in Figs. (3) and (4) respectively.


Fig . 2 Relationship between vsg and hl/D for different vsl \{WLR=50\%\}


Fig. 3 Relationship between vsg and hw/D for different vsl $\{\mathrm{WLR}=\mathbf{5 0 \%}\}$


Fig. 4 Relationship between vsg and ho/D for different vsl \{WLR=50\%\}

The values of $\left(h_{L} / D\right),\left(h_{w} / D\right),\left(h_{o} / D\right)$ are plotted on the same figure versus (vsg) for a constant (vsl). Several figures are obtained for different velocities (Fig. 5 for vsl= 0.065, Fig. 6 for vsl $=0.089$, Fig. 7 for vsl=0.11. The water level is usually quit high and the liquid consists mostly of water. This is logical since the oil being closer to the fast moving gas, i.e., the oil is dragged by the gas at higher velocities compared with the water layer at bottom.


Fig. 5 Relationship between vsg and $h / D(v s l=0.065 \mathrm{~m} / \mathrm{s})\{\mathrm{WLR}=50 \%\}$


Fig. 6 Relatioship between vsg and $h / D(v s l=0.089 \mathrm{~m} / \mathrm{s})\{\mathrm{WLR}=50 \%\}$


Fig. 7 Relationship between vsg and $h / D(v s l=0.11 \mathrm{~m} / \mathrm{s})\{W L R=50 \%\}$

## The Effect of Gas Flow Rate on Pressure Drop

The effects of liquid and gas flow rate on pressure drop are presented in Fig.8. In general the pressure drop increased when the gas and/or liquid flow rate increased.


Fig. 8 Relationship between vsg and pressure drop for different vsl $\{W L R=50 \%\}$

## Flow Pattern Maps

Fig. 9 depict the flow pattern map for the stratified three-phase flow through horizontal pipes


Fig . 9 Relationship between vsg and vsl $\{W \mathrm{LR}=50 \%\}$

## THE FORMELATED EQUATIONS

Three empirical correlations for estimating dimensionless liquid, and water thicknesses and system pressure drop in three-phase stratified flow in horizontal pipe are developed. The diameter of the pipe used is 0.051 m and the length is 4 m . Constant fluid physical properties (table.1) are used in these correlations. As shown below the dimensionless thickness and pressure drop are correlated as a function of liquid flow rate, gas flow rate, and water liquid ratio (WLR):-

The correlated dimensionless liquid film thickness equation is: -
$\frac{h_{L}}{D}=a_{1}+a_{2} *\left(W L R * Q_{L}\right)^{a_{3}}+a_{4} *\left((1-W L R) * Q_{L}\right)^{a_{5}}+a_{6} * Q_{G}{ }^{a_{7}}$
Where,
$a_{1}=-0.116227 \quad a_{2}=0.451614 \quad a_{3}=0.850409 \quad a_{4}=0.48286$
$a_{5}=0.981403 \quad a_{6}=0.364976 \quad a_{7}=-0.193155$
$Q_{L} \& Q_{G}: m^{3} / h r$.
WLR: fraction
The correlation coefficient for Eq. (5-1) is 0.96
The formulated dimensionless water film thickness equation is shown below: -
$\frac{h_{w}}{D}=b_{1}+b_{2} *\left(W L R * Q_{L}\right)^{b_{3}}+b_{4} *\left((1-W L R) * Q_{L}\right)^{b_{5}}+b_{6} * Q_{G}{ }^{b_{7}}$
Where,
$b_{1}=-0.117454 \quad b_{2}=0.620129 \quad b_{3}=0.590837 \quad b_{4}=0.047055$
$b_{5}=0.805945 \quad b_{6}=0.173923 \quad b_{7}=-0.375791$
Here, the correlation coefficient equal to 0.99

The pressure drop equation is formulated as follows: -
$\Delta P=c_{1} *\left(\left(W L R * Q_{L}+(1-W L R) * Q_{L}\right) * Q_{G}\right)^{c_{2}}$
Where,
$c_{1}=0.000863 \quad c_{2}=0.409815$
The correlation coefficient for the above Eq. is 0.91
Figs.10, 11, and 12 show that there is a good agreement between experimental and predicted data obtained from Eqs.1, 2, and 3 for dimensionless liquid, and water thickness and pressure drop respectively.


Fiq. 10 Relationship between $\mathrm{hl} / \mathrm{D}$ predicted vs. $\mathrm{h} / \mathrm{D}$ observed Values


Fiq. 11 Relationship between hw/D predicted ve. hw/D observed Values

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| :--- | :--- | :--- |



Fiq. 12 Relationship between dp predicted vs. dp observed values

## THREE-PHASE FLOW MECHANISTIC MODEL

Several three-phase flow models were found. All of the models are developed from the three-phase momentum equations with few changes from one to the other.

Taital et al. (1995) developed a three-phase model for horizontal and near-horizontal threephase flow. The model starts with the momentum balance equatins for each phase.
$-A_{W}\left(\frac{d p}{d x}\right)-\tau_{W} S_{W}+\tau_{i} S_{i}-\rho_{W} A_{W} g \sin \beta=0$
$-A_{o}\left(\frac{d p}{d x}\right)-\tau_{o} S_{o}-\tau_{i} S_{i}+\tau_{j} S_{j}-\rho_{o} A_{o} g \sin \beta=0$
$-A_{G}\left(\frac{d p}{d x}\right)-\tau_{G} S_{G}-\tau_{j} S_{j}-\rho_{G} A_{G} g \sin \beta=0$
Summing Eqs. 4 and 5 yields:

$$
\begin{equation*}
-\left(\frac{d p}{d x}\right)-\frac{\tau_{L} S_{L}}{A_{L}}+\frac{\tau_{i} S_{i}}{A_{L}}-\rho_{L} g \sin \beta=0 \tag{7}
\end{equation*}
$$

Where;

$$
\begin{gather*}
\tau_{L} S_{L}=\tau_{W} S_{W}+\tau_{o} S_{O}  \tag{8}\\
\rho_{L}=\frac{\rho_{W} A_{W}+\rho_{O} A_{O}}{A_{L}} \tag{9}
\end{gather*}
$$

And;

$$
\begin{equation*}
A_{L}=A_{W}+A_{O} \tag{10}
\end{equation*}
$$

Note that Eq. 7 is the combined momentum equation for the liquid phase, which composed, of water and oil layers. Therefore, Eqs. 8 and 9, have the same form as two-layer momentum equations for liquid and gas as derived by classical Taital and Dukler model (1976).

The pressure drop can be eliminated by adding Eqs. 6 to 7 to yield:
$-\frac{\tau_{L} S_{L}}{A_{L}}+\frac{\tau_{G} S_{G}}{A_{G}}+\tau_{j} S_{j}\left(\frac{1}{A_{L}}+\frac{1}{A_{G}}\right)-\left(\rho_{o}-\rho_{G}\right) g \sin \beta=0$
In the same way the pressure drop is eliminated from Eqs. 4 and 5 to yield:
$-\frac{\tau_{W} S_{W}}{A_{W}}+\frac{\tau_{o} S_{o}}{A_{o}}-\frac{\tau_{j} S_{j}}{A_{o}}+\tau_{i} S_{i}\left(\frac{1}{A_{W}}+\frac{1}{A_{o}}\right)-\left(\rho_{W}-\rho_{o}\right) g \sin \beta=0$
Eqs.11and 12 must be solved simultaneously to yield the liquid level $\left(h_{L}\right)$, and the water level, ( $h_{W}$ ).

In this study, Taitel et al (1995) model is used for comparison with the experimental data of this study.

## Comparison with Mechanistic Model

The results of the Three-phase mechanistic model of Taital et al. (1995) are plotted against the experimental data $\left(\frac{h_{L}}{D}, \frac{h_{W}}{D}, \frac{h_{O}}{D}, \& \Delta P\right)$ as shown in Fiqs. 13 through 16.

It is clear that the good agreement is obtained between the experimental results of the presented study and that of Taital et al. (1995) model.


Fiq. 13 Relationship between hi/D Observed vs. hl/D Predicted \{by Taital et al. model (1995)\}


Fiq. 14 Relationship between hw/D Observed vs. hw/D Predicted $\{\mathbf{b y}$ Taital et al. model (1995)\}


Fiq. 15 Relationship between ho/D Observed vs. ho/D Predicted \{by Taital et al. model (1995) \}


Fiq. 16 Relationship between dP Observed vs. dP Predicted \{by Taital et al. model (1995) \}

## Conclusions

1. Three equations have been developed by correlating the experimental data. These equations can be used to predict liquid, and water thicknesses and system pressure drop for the conditions specified in the present work.
2. Three-phase flow model Taital et al. (1995) gave good prediction for liquid, water thicknesses, and pressure drop.
3. In three-phase flow (water, oil, and gas) the water level is usually quit high and the liquid consists mostly of water for equal rate of water and oil (WLR=50\%).

## SYMMOLS AND ABBREVIATIONS

| Symbol | Definition | Unit |
| :--- | :--- | :---: |
| $A$ | Pipe area | $\mathrm{m}^{2}$ |
| $h$ | Film thickness | m |
| $P$ | Pressure | Pa |
| $Q$ | Flow rate | $\mathrm{m}^{3} / \mathrm{s}$ |
| $S$ | Perimeter | m |
| $V_{S}$ | Superficial velocity | $\mathrm{m} / \mathrm{s}$ |
| $\beta$ | Inclination of pipe | deg. |
| $\rho$ | Density | $\mathrm{kg} / \mathrm{m}^{3}$ |
| $\tau$ | Shear stress | Pa |


| Subscript | Definition |
| :---: | :--- |
| W | Water |
| O | Oil |
| G | Gas |
| L | Liquid |
| i | interface between oil and water |
| j | interface between gas and oil |
| K | Water, Oil, or Gas |
| Abbreviation | Definition |
| WLR | water liquid ratio |
| Exp. | Experimental |
| Pre. | Predicted |
| SS | smooth stratified flow |
| SW | wavy stratified flow |

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# OPTIMUM SATELLITE LAUNCHER TRAJECTORY GUIDED WITH PROPORTIONAL NAVIGATION PLUS GRAVITY COMPENSATION GUIDANCE 

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#### Abstract

The optimum trajectory of a single or multi-stage satellite launcher guided with proportional navigation guidance (PNG) is addressed. The PNG is extended to compensate for the gravity effect. For the trajectory optimization problem, the launcher is modeled as a mass point flying around the center of the Earth. To provide a completely valid analysis, all known influences on the launcher trajectory have been considered; Empirical equations have been used in order to model the Earth standard atmosphere in SI units. A computer program had been constructed in order to simulate the trajectory of such launcher from the available initial conditions. Pegasus launcher is used as a hypothetical example. The simulator results show that the proportional navigation plus gravity compensation guidance gives fairly accurate results.


الخلاصة
في هذا البحث, تمت دراسة المسار الأمثل لناقل أقمار صناعية (مرحلة واحدة أو متعدد المر احل ) موجه بطريقة الملاحة التناسبية وتم تطوير قانون الملاحة التتاسبية للتعويض عن تأثّثر الجاذبية الأرضية على مسار الناقل. لغرض ايجاد المسار الامثلـ, تم فرض الناقل كجزيئة تطبر حول مركز الكرة الارضية. ولغرض توفير تحليل رصين, تم اعتبار كل العوامل المؤثرة على مسار الناقل بما فيها تأثير دوران الكرة الأرضية ، وكذلك تم وضع معادلات تجريبية عالية الاقة لوصف تغير خصائص الغلاف الجوي للأرض مع ارتفاع الناقل بالوحدات العالمية الموحدة. لقد تم أعداد برنامج لمحاكاة مسار هكذا ناقل من خلال توفير المعلومات الأوليةلاطلاق الناقل ، وقل تم استخدام بيغاسوس كمثال لتطبيق موضوع البحث. وقد اضهرت النتائج آن استخدام طريقة الملاحة التناسبية مع التنويض عن الجاذبية الأرضية يعطي نتائج مقبولة الدقة.

## KEYWORDS

Modeling of Flight System, Proportional Navigation Guidance Law, Gravity Compensation, Linearization, and Optimization.

## INTRODUCTION

New concept for space transportation are proposed and investigated in various countries as a means for improving the space transportation capability and for reducing costs. The main task of guidance process is to determine the vehicle position and velocity, computation of control actions necessary to properly adjust position and velocity, and delivery of a suitable adjustments command to the vehicle control system to achieve the correct trajectory. (Zarchan, 1990 and Bong Wie 1998).

PNG is accepted as a celebrated guidance law for many guided missile applications like the surface-to-air, air-to-air, air-to-surface missile encounters, standoff weapon delivery, and space
rendezvous. The guided point (launcher) is assumed to move towards a target point in a plane containing the velocity vectors of the two points. The PNG technique is defined such that the
velocity vector (heading) of the launcher is turned at a rate proportional to the rotation rate of the line joining the launcher and the target, which is the line of sight (LOS). The PNG principle helps to estimate the magnitude of the lateral acceleration that is perpendicular to LOS as a function of LOS turn rate (Zarchan, 1990 and Asher \& Yaesh 1998).

The trajectories of rocket vehicle have three successive phases. In the first phase, which is called the boost phase (initial phase), the rocket engine (or engines if the rocket is multi-stage) provide the precise amount of propulsion required to place the rocket on a specific trajectory. Then the engine quits, and the final stage of the rocket (payload) coasts in the second phase that is called midcourse phase, and finally the terminal phase (or gravity turn trajectory)

Guidance operations may occur in the initial, midcourse, or terminal phase of flight. Ballistic missiles are commonly guided only during the initial flight phase, while the rocket engines are burning. A cruise type of missile, such as the Shark or Matador, uses midcourse guidance, operating continuously during cruising flight. Air-to-air missile such as Sidewinder employ terminal guidance systems that lead the missile directly to the target on the basis of measurements on the target itself.
Errors in accuracy for rocket vehicles trajectories are generally expressed as launch point errors, guidance en-route errors or aim point error. Both launch and aim-point errors can be corrected by surveying the launch and the target areas more accurately. Aim errors on the other hand, must improve the rocket's design particularly its guidance systems. A missile's circular error probability (CEP) and bias usually measure aim errors. CEP uses the mean point of impact of missile test firings, usually taken at maximum range, to calculate the radius of a circle that would take in 50 percent of the impact points. Bias measures the deviation of the mean impact point from the actual aim point. An accurate missile has both a low CEP and low bias (Encyclopedia Britannica, 2002).

There are no single set of initial conditions required to arrive at a specified target, but rather there are an infinite number of possible free flight paths originating at points in space in the vicinity of some nominal starting point which terminate at the desired destination. For each such point there is a corresponding proper velocity. It is the task of the guidance system to cause the rocket to take up any one of these free flight paths.

## LAUNCHER DYNAMIC MODEL

For the trajectory optimization problem the usual mass point modeling is applied for describing the flight system dynamics. With reference to the rotating spherical Earth, the equations of motion can be expressed as Fig.(1) (Mayrhofer \& Sachs 1997)

$$
\begin{align*}
\dot{V}= & \left(\frac{T \cos (\alpha+\delta)-D}{m}\right)-g \sin \gamma+\omega_{E}^{2}\left(R_{E}+h\right) \cos \Phi(\sin \gamma \cos \Phi-\cos \gamma \sin \Phi \cos \psi)  \tag{1}\\
\dot{\gamma}= & \left(\frac{T \sin (\alpha+\delta)+L}{m V}\right) \cos \varphi+\left(\frac{V}{R_{E}+h}-\frac{g}{V}\right) \cos \gamma+2 \omega_{E} \cos \Phi \sin \psi+\frac{\omega_{E}^{2}\left(R_{E}+h\right)}{V} \cos \Phi  \tag{2}\\
& (\cos \gamma \cos \Phi+\sin \gamma \sin \Phi \cos \psi)
\end{align*}
$$

$$
\begin{equation*}
\ddot{\psi}=\left(\frac{T \sin (\alpha+\delta)+L}{m V \cos \gamma}\right) \sin \varphi+\left(\frac{V}{R_{E}+h}\right) \cos \gamma \sin \psi \tan \Phi-2 \omega_{E}(\tan \gamma \cos \Phi \cos \psi-\sin \gamma) \tag{3}
\end{equation*}
$$

$$
+\left(\frac{\omega_{E}^{2}\left(R_{E}+h\right)}{V \cos \gamma}\right) \sin \Phi \cos \Phi \sin \psi
$$

$\dot{\Phi}=\frac{V \cos \gamma \cos \psi}{\left(R_{E}+h\right)}$
$\dot{\Lambda}=\frac{V \cos \gamma \sin \psi}{\left(R_{E}+h\right) \cos \Phi}$
$\dot{h}=V \sin \gamma$
The aerodynamic model can be described as:
$L=C_{L} q S$
$D=C_{D} q S$
Where $C_{L}$ and $C_{D}$ are function of $\alpha$ and $M$
The model of the main rocket propulsion is described as
$T=\dot{m} g_{0} I_{S P}$

## PROPORTIONAL NAVIGATION GUIDANCE LAW

This guidance method is based on the requirement (Zarchan, 1990)
$\frac{d \gamma}{d t}=N^{\prime} \frac{d \lambda}{d t}$
And the command acceleration will be
$a_{c}=V_{c} \dot{\gamma}=V_{c} N^{\prime} \dot{\lambda}$

## Guidance Equations

According to (Asher \& Yaesh 1998).
$\dot{r}_{T M}=V_{c}=V_{T} \cos \varepsilon_{T}-V \cos \varepsilon$
$\dot{\lambda}=\frac{1}{r_{T M}}\left(V_{T} \sin \varepsilon_{T}-V \sin \varepsilon\right)$
$\dot{\gamma}=N^{\prime} \dot{\lambda}$
But for satellite launcher, the target is a fixed point in the space, so $\left(V_{T}=0\right)$. Therefore, command acceleration expressed as
$a_{c}=\frac{N^{\prime} V^{2}}{2 r_{T M}} \sin 2 \varepsilon=\frac{N^{\prime} V^{2}}{2 r_{T M}} \sin 2(\lambda-\gamma)$
The target can be defined as a fixed point in the missile local plane $(\rho, z)$ as shown in Fig.(2) measured from the launcher, then the calculations of related quantities gives
$\rho_{M}=\int_{t_{0}}^{t_{f}} V \cos \gamma d t$
$z_{M}=\int_{t_{0}}^{t_{f}} V \sin \gamma d t$
$\rho_{T M}=\rho_{T}-\rho_{M}$
$z_{T M}=z_{T}-z_{M}$
$r_{T M}=\sqrt{\rho_{T M}^{2}+z_{T M}^{2}}$
$\lambda=\tan ^{-1}\left(\frac{z_{T M}}{\rho_{T M}}\right)$

## LINEARIZATION

In order to allow better ways of analyses and optimization of the guidance command acceleration it is important to leave the non-linear missile target simulation and find a simpler model, as it is usual in engineering practice. We are going to linearize the acceleration command equations allowing the application of powerful analytical techniques (Zarchan, 1990).
As defined previously $z_{T M}$ is the relative separation between the rocket and the target in local vertical plane, then the relative acceleration can be expressed as
$\ddot{z}_{\text {TM }}=-a_{c} \cos \lambda$
And the expression for the LOS angle will be
$\sin \lambda=\frac{z_{T M}}{r_{T M}}$
If we assume that the LOS angle is small, then eq.(22) and eq.(23)
$\ddot{z}_{T M}-a_{c}$
$\lambda=\frac{z_{T M}}{r_{T M}}$
In linearized analyses we treat the closing velocity as a positive constant and equal to the missile velocity. Since closing velocity has also been previously defined as the negative derivative of the range from the missile to target, and since the missile-target separation distance must go to zero at the flight, we can also linearized the range equation with the time varying relationship (Zarchan, 1990 and Asher \& Yaesh 1998).

$$
\begin{equation*}
r_{T M}=V_{c}\left(t_{f}-t\right) \tag{26}
\end{equation*}
$$

Since the missile-target separation distance goes to zero at the end of flight by definition, the linearized miss distance is taken to be the relative separation between missile and target $z_{T M}$, at the end of flight:

$$
\begin{equation*}
\text { Miss }=z_{T M}\left(t_{f}\right) \tag{27}
\end{equation*}
$$

This linearized model will give very high accuracy, where its results are the same as those obtained from the non-linear model for fixed or non-maneuvering targets (the case of our search), and for heading error case, and will give overestimations from the non-linear model in the case of maneuvering targets (Zarchan, 1990).

## Linearization of PNG Law

Substituting eq.(26), into eq.(24) we get
$\lambda=\frac{z_{T M}}{V_{c}\left(t_{f}-t\right)}$
The derivative of eq.(28) will give the LOS rate by
$\dot{\lambda}=\frac{z_{T M}+\dot{z}_{T M}\left(t_{f}-t\right)}{V_{c}\left(t_{f}-t\right)^{2}}=\frac{z_{T M}+\dot{z}_{T M} t_{g o}}{V_{c} t_{g o}^{2}}$
Thus we can express the PNG law as
$a_{c}=N^{\prime} V_{c} \dot{\lambda}=\frac{N^{\prime}\left(z_{T M}+\dot{z}_{T M} t_{g o}\right)}{t_{g o}^{2}}$
The expression in the parentheses of eq.(30) represents the future separation between missile and target. More simply, the expression in parentheses is the miss distance that would result if the missile made no further corrective acceleration and the target did not maneuver. This expression is referred to as the zero effort miss (ZEM). Therefore, we can also think of PN as a
guidance law in which commands acceleration are issued inversely proportional to the square of time to go and directly proportional to the ZEM (Zarchan, 1990 and Asher \& Yaesh 1998).

## OTMIZATION OF PNG LAW

We seek to find a guidance law that is a function of the system states. There are an infinite number of possible guidance laws; thus, it is necessary to state in mathematical terms what the guidance law should do. Certainly we would like to hit the target; therefore, one feature of the guidance law should be a zero miss distance requirement. In addition, we would like to hit the target in an efficient manner. In other words, we desire to use minimal total acceleration. A poplar and mathematically convenient way of stating the guidance problem to be solved is that we desire to achieve zero miss distance and to minimize the integral of the square of the command acceleration (Zarchan, 1990 and Asher \& Yaesh 1998) i.e.

$$
\begin{equation*}
z_{T M}\left(t_{f}\right)=0 \tag{31}
\end{equation*}
$$

Subject to minimizing
$\int_{0}^{t_{f}} a_{c}^{2}(t) d t$
Unfortunately, if we minimize a more meaningful performance index such as the integral of the absolute value of $a_{c}$, the solution would be mathematically intractable. Typically this type of problem with a quadratic performance index is solved using techniques from optimal control theory. However, this class of problems can be solved more easily using Schwartz inequality (Zarchan, 1990).

Now, we will construct from the previous equations the satellite launcher flight in state space form as
$\left[\begin{array}{l}\dot{\mathbf{z}}_{\mathrm{TM}} \\ \ddot{\mathbf{z}}_{\mathrm{TM}}\end{array}\right]=\left[\begin{array}{ll}\mathbf{0} & \mathbf{1} \\ \mathbf{0} & \mathbf{0}\end{array}\right]\left\{\begin{array}{l}\mathbf{z}_{\mathrm{TM}} \\ \dot{\mathbf{z}}_{\mathrm{TM}}\end{array}\right\}+\left[\begin{array}{c}\mathbf{0} \\ -\mathbf{1}\end{array}\right] \mathbf{a}_{\mathbf{c}}$
Before going in any further analyses, we must first check the controllability of the state space that we had performed. The general state space form
$\dot{\mathbf{x}}=\mathbf{A x}+\mathbf{B u}$
by comparing eq.(33) and eq.(34) we find that
$A=\left[\begin{array}{ll}0 & 1 \\ 0 & 0\end{array}\right]$
$\mathbf{B}=\left[\begin{array}{c}\mathbf{0} \\ -\mathbf{1}\end{array}\right]$
We must find the matrix $[\mathbf{B}: \mathbf{A B}]$
$[\mathbf{B} \vdots \mathbf{A B}]=\left[\begin{array}{cc}0 & -1 \\ -1 & 0\end{array}\right]=$ nonsigular
The system is therefore completely state variable (Ogata, 2002).
The solution of the state space vector deferential equation is given at the final time $t_{f}$ by the vector relationship (Zarchan, 1990).
$\mathbf{x}(\mathbf{t})=\boldsymbol{\Phi}\left(\mathbf{t}_{\mathrm{f}}-\mathbf{t}\right) \mathbf{x}(\mathbf{t})+\int \boldsymbol{\Phi}\left(\mathbf{t}_{\mathrm{f}}-\boldsymbol{\tau}\right) \mathbf{B u}(\boldsymbol{\tau}) \mathbf{d} \boldsymbol{\tau}$
Where $\boldsymbol{\Phi}(\mathbf{t})=\left[\begin{array}{ll}\mathbf{1} & \mathbf{t} \\ \mathbf{0} & \mathbf{1}\end{array}\right]$
Using the above fundamental matrix in the solution for the state space vector deferential equation and only looking at the first state, we get

$$
\begin{equation*}
z_{T M}\left(t_{f}\right)=z_{T M}(t)+\dot{z}_{T M}(t)\left(t_{f}-t\right)-\int_{t}^{t_{f}}\left(t_{f}-\tau\right) a_{c}(\tau) d \tau \tag{36}
\end{equation*}
$$

For convenience, let us define the terms

$$
\begin{align*}
& f_{1}\left(t_{f}-t\right)=z_{T M}(t)+\dot{z}_{T M}(t)\left(t_{f}-t\right)  \tag{37}\\
& h_{1}\left(t_{f}-\tau\right)=t_{f}-\tau
\end{align*}
$$

Then we can say that

$$
\begin{equation*}
z_{T M}\left(t_{f}\right)=f_{1}\left(t_{f} t\right)-\int_{t}^{t_{f}} h_{1}\left(t_{f}-\tau\right) a_{c}(\tau) d \tau \tag{39}
\end{equation*}
$$

For the conditions in which we have zero miss distance $z_{T M}\left(t_{f}\right)=0$, we can rewrite eq.(39)
$f_{1}\left(t_{f}-t\right)=\int_{t}^{t_{f}} h_{1}\left(t_{f}-\tau\right) a_{c}(\tau) d \tau$
If we apply the Schwartz inequality to eq.(40) we get the relationship (Zarchan, 1990).
$f_{1}^{2}\left(t_{f}-t\right) \leq \int_{t}^{t_{f}} h_{1}^{2}\left(t_{f}-\tau\right) d \tau \int_{t}^{t_{f}} a_{c}^{2}(\tau) d \tau$
Then $\int_{t}^{t_{f}} a_{c}^{2}(\tau) d \tau \geq \frac{f_{1}^{2}\left(t_{f}-t\right)}{\int_{t}^{t_{f}} h_{1}^{2}\left(t_{f}-\tau\right) d \tau}$
The integral of the square of the command acceleration will be minimized when the equality sign holds in the preceding inequality. According to the Schwartz inequality, the equality sign holds when

$$
\begin{equation*}
a_{c}(\tau)=k h_{1}\left(t_{f}-\tau\right) \tag{42}
\end{equation*}
$$

This means that the integral of the squared acceleration is minimized when

$$
\begin{equation*}
k=\frac{f_{1}\left(t_{f}-t\right)}{\int_{t}^{t_{f}} h_{1}^{2}\left(t_{f}-\tau\right) d \tau} \tag{43}
\end{equation*}
$$

Therefore, the command acceleration is given by
$a_{c}=\left[\frac{f_{1}\left(t_{f}-t\right)}{\int_{t}^{t_{f}} h_{1}^{2}\left(t_{f}-\tau\right) d \tau}\right] h_{1}\left(t_{f}-t\right)$
Substituting yields to the feedback control guidance law

$$
\begin{equation*}
a_{c}=\frac{3\left(z_{T M}+\dot{z}_{T M} t_{g o}\right)}{t_{g o}^{2}} \tag{45}
\end{equation*}
$$

By comparing eq.(30) with eq.(45) we find that the optimum value of effective navigation ratio for the satellite launcher is $N^{\prime}=3$.

## PNG LAW WITH GRAVITY COMPENSATION

One of the major effects that prevent to obtain a straight-line missile's trajectory is the gravity effect. Changes in the missile velocity due to gravity caused the LOS to rotate. The PNG law responds to the apparent LOS rate with command acceleration. If we have knowledge of
gravitational acceleration, it seems reasonable that it might be possible to compensate for unnecessary acceleration via the guidance law. (Zarchan, 1990).
Fortunately in our particular case the target did not have gravitational acceleration. The launcher gravitational acceleration can be expressed as (Meriam, \& Kraige, 1998).
$g=\frac{G m_{o}}{r^{2}}$
The component of the gravity acceleration perpendicular to the LOS for the launcher is
$g_{M_{\text {PLOS }}}=g \cos \lambda$
And the component of the gravity acceleration perpendicular to the LOS for the target is zero.
The gravitational acceleration difference between the target and the missile can be treated as an additional terms in the ZEM. Therefore, we can modify the PNG law to account for gravity. The resultant law is (Zarchan, 1990 and Asher \& Yaesh 1998).

$$
\begin{equation*}
a_{c}=N^{\prime} V_{c} \dot{\lambda}+\frac{N^{\prime}}{2}\left(g_{T_{P L O S}}-g_{M_{P L O S}}\right) \tag{48}
\end{equation*}
$$

For the case of the satellite launcher, eq.(48) can be reduced to
$a_{c}=N^{\prime} V_{c} \dot{\lambda}-\frac{N^{\prime} g \cos \lambda}{2}$

## HYPOTETICAL EXAMPLE

Pegasus is used for showing PNG and PN plus gravity compensation guidance. Pegasus is a small commercial launch vehicle developed by orbital science. It is provided with solid propellant booster and wings, and is lunched from an aircraft. Pegasus mission is to inject the satellite at altitude of ( 123 km ), with velocity of ( $7790 \mathrm{~m} / \mathrm{sec}$ ), and zero flight path angle (FPA). Pegasus is released from its carrier with an initial velocity of about ( 0.8 Mach) and zero initial FPA with free flight duration of $(5 \mathrm{sec})$. At the free flight, delta wing of the Pegasus is capable of achieving a zero FPA at the start of the first stage burning. (Isakowitz, \& Hopkins Jr, \& Hopkins, 1999).

## RESULTS AND DISCUSSION

Three cases are simulated. The first case when Pegasus launched without guidance, the second when Pegasus guided with optimum PNG, and the third Pegasus guided with PN plus gravity compensation guidance. The altitude, velocity, and FPA are shown in Figs.(3), Figs.(4), and Figs.(5) respectively.

Pegasus without guidance is rapidly falling due to negative values of the FPA, which cause the thrust force to push down. This means that Pegasus cannot fly without guidance.
For the second case the large drop in altitude, and FPA during the second stage flight lead the rocket be unable to reach its target which is very far from the rocket, although the altitude and FPA increase, the velocity continue to decrease then starts to increase before the end of flight.
For the third case, the altitude of this case is highly accurate, and we can see from Figs.(5) that launcher is exceed the target and return to it because of the guidance, i.e. the launcher is reach to altitude of $(136 \mathrm{~km})$ at $(267 \mathrm{sec})$ then return to attitude of $(132 \mathrm{~km})$ at the end of flight. At the end of flight for this case the launcher velocity about ( $5.62 \%$ ) less than the required velocity and the FPA is about ( $-3.9^{\circ}$ ).

From comparing the Pegasus trajectory and the final mission requirements as given in (Isakowitz, \& Hopkins Jr, \& Hopkins, 1999), and that obtained from the PN plus gravity compensation guidance, we can say that the PN plus gravity compensation guidance is fairly applicable for satellite launcher case.

## CONCLUSION

The following concluding remarks are drawn from the present work:

1. The optimum value of the effective navigation ratio of the proportional navigation guidance for a satellite launcher application is $N^{\prime}=3$.
2. The proportional navigation plus gravity compensation guidance advised to use for the satellite launcher application.

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## NOMENCLATURE

(SI units are used, unless otherwise stated)

| $a_{c}$ | Command acceleration |
| :--- | :--- |
| $C_{D}$ | Drag coefficient |
| $C_{L}$ | Lift coefficient |
| $D$ | Drag force |
| $G$ | Universal constant |
| $g$ | Local Earth gravitational acceleration |
| $g_{o}$ | Earth gravitational acceleration at sea level |
| $g_{P L O S}$ | Gravitational acceleration component perpendicular to LOS |
| $h$ | Altitude of the launcher vehicle |
| $I_{S P}$ | Specific impulse |
| $L$ | Lift force |
| $M$ | Mach number |
| $m$ | Total launcher vehicle mass |
| $\dot{m}$ | Fuel mass flow rate |
| $m_{o}$ | Mass of the Earth |
| $N^{\prime}$ | Proportional navigation constant |
| $q$ | Dynamic pressure |
| $r$ | Radial distance between the center of the Earth and the launcher center |
| $R_{E}$ | Mean radius of the Earth |


| $r_{T M}$ | Target-Missile separation distance |
| :--- | :--- |
| $S$ | Launcher reference area |
| $T$ | Total thrust of the launcher |
| $t_{f}$ | Final flight time |
| $t_{g o}$ | Time to go |
| $t_{0}$ | Initial flight time |
| $V$ | Launcher vehicle velocity |
| $V_{c}$ | Closing velocity between the missile and the target |
| $z_{T M}$ | Target-Missile separation distance in local z direction |
| $\alpha$ | Attack angle |
| $\psi$ | Azimuth angle |
| $\varepsilon$ | Launcher lead angle |
| $\Phi$ | Geocentric latitude angle |
| $\varphi$ | Roll (Bank) angle |
| $\phi$ | Sight angle |
| $\gamma$ | Flight path angle |
| $\Lambda$ | Geographic longitude |
| $\lambda$ | Local line of sight angle |
| $\omega_{E}$ | Angular velocity of the Earth rotation |
| $(\rho, z)$ | Local coordinates of launcher vehicle |
| $\theta$ | Pitch or (Elevation) angle |



Fig.(1)



Time (sec.)


Time (sec.)


Figs.(3a,b,c) respectively Launcher without guidance


Time (sec.)



Figs.(4a,b,c) respectively
Launcher with PN guidance


Time (sec.)


Time (sec.)


Time (sec.)
Figs.(5a,b,c) respectively
Launcher with PN plus gravity compensation guidance

